

Particle Cosmology

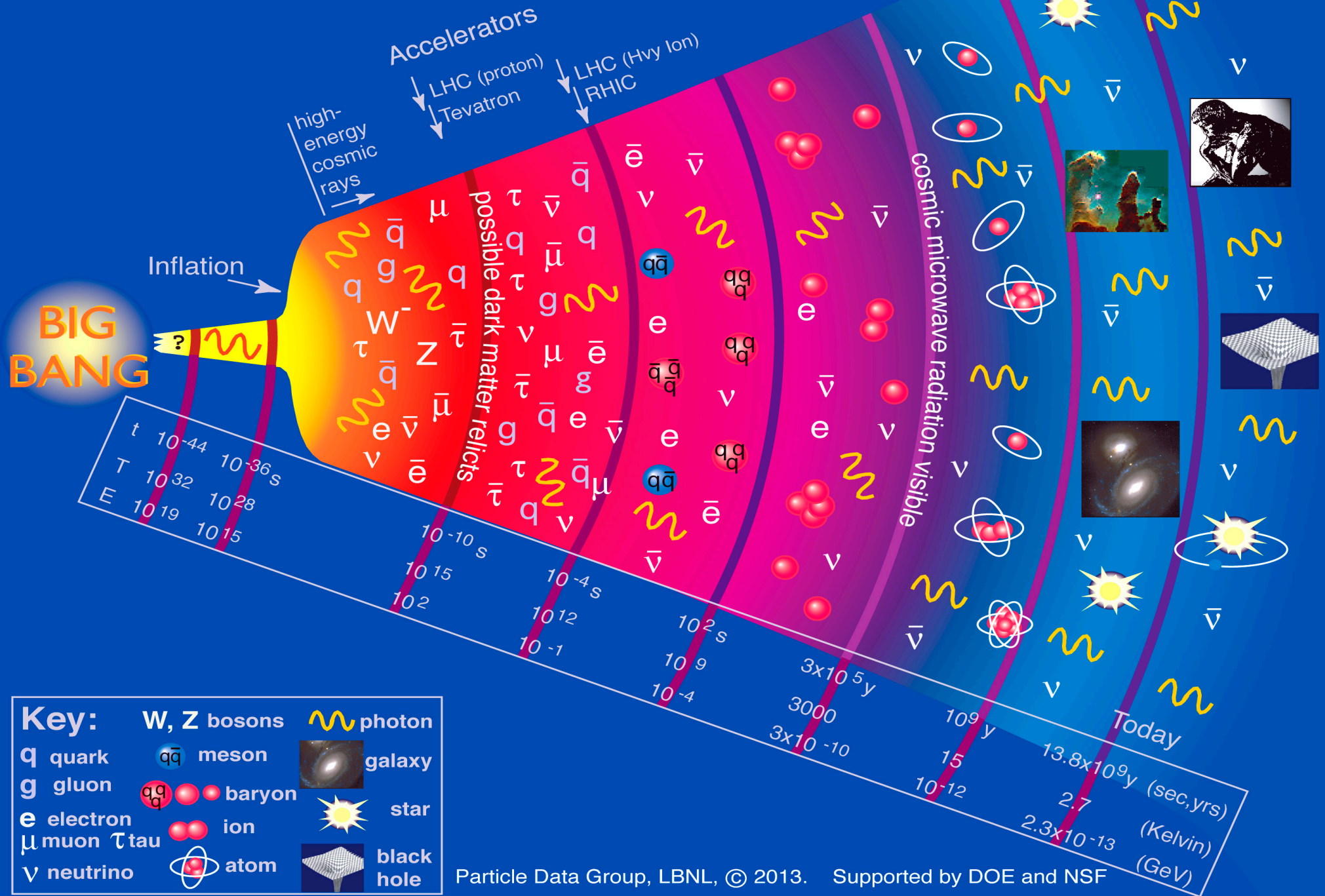
FRW Cosmology

Inflation

Baryogenesis

Big Bang Nucleosynthesis

History of the Universe



Big Bang Nucleosynthesis

- BBN and the WMAP/Planck determination of η , $\Omega_B h^2$
- Input cross sections
- Observations and Comparison with Theory
 - D/H - ^4He - ^7Li
- Neutrinos
- Constraints on BSM physics
- The Future (CMB)

Foundations of Big Bang Cosmology: Nucleosynthesis and the CMB

Big Bang cosmology grew from the work of Gamow, Alpher, and Hermann in their attempts to explain the observed element abundances.

They predicted the existence of the 3K background which was discovered 16 years later.

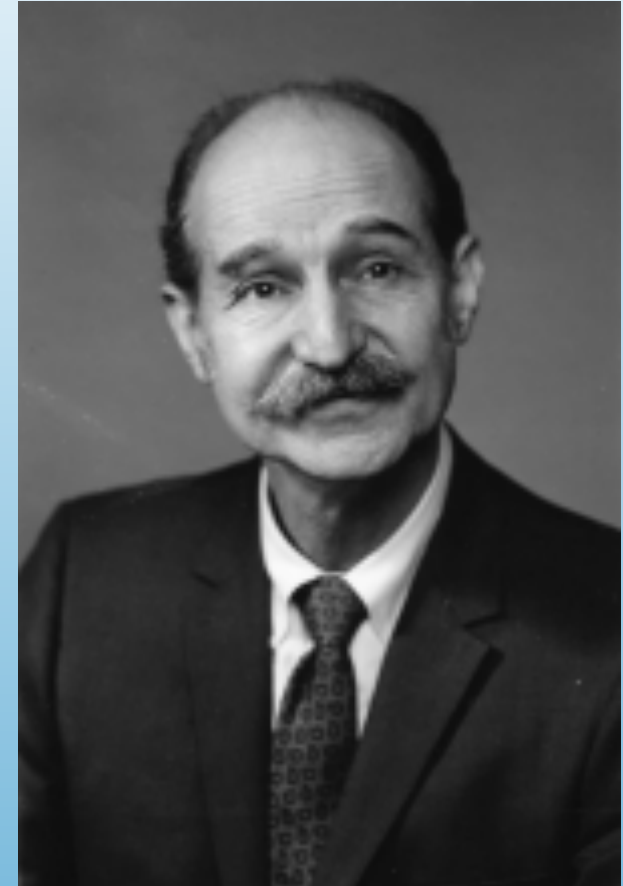
It all started with:



George Gamow



Ralph Alpher

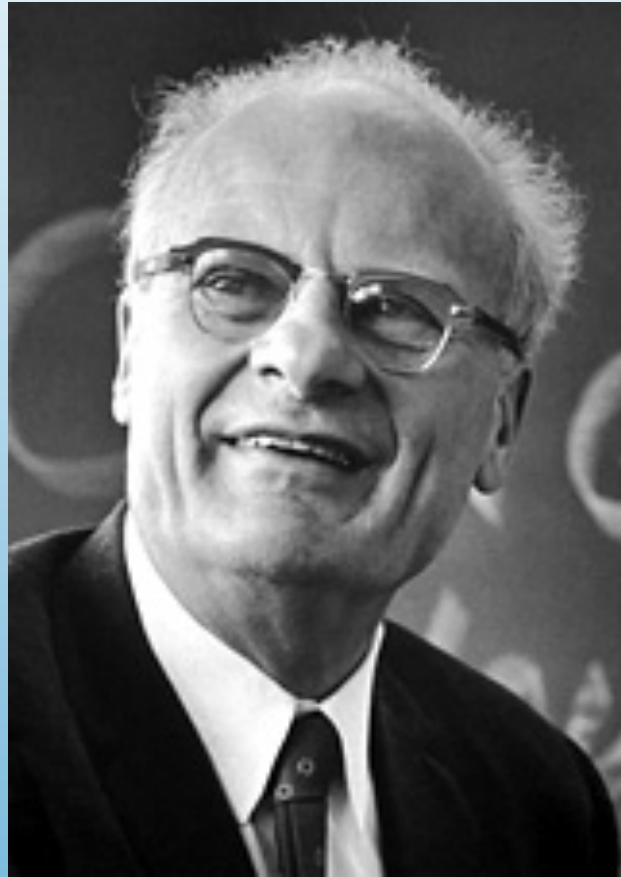


Robert Herman

It all started with:



Ralph Alpher



Hans Bethe



George Gamow

Letters to the Editor

PUBLICATION of brief reports of important discoveries in physics may be secured by addressing them to this department. The closing date for this department is five weeks prior to the date of issue. No proof will be sent to the authors. The Board of Editors does not hold itself responsible for the opinions expressed by the correspondents. Communications should not exceed 600 words in length.

The Origin of Chemical Elements

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*Applied Physics Laboratory, The Johns Hopkins University,
Silver Spring, Maryland*

AND

H. BETHE

Cornell University, Ithaca, New York

AND

G. GAMOW

The George Washington University, Washington, D. C.

February 18, 1948

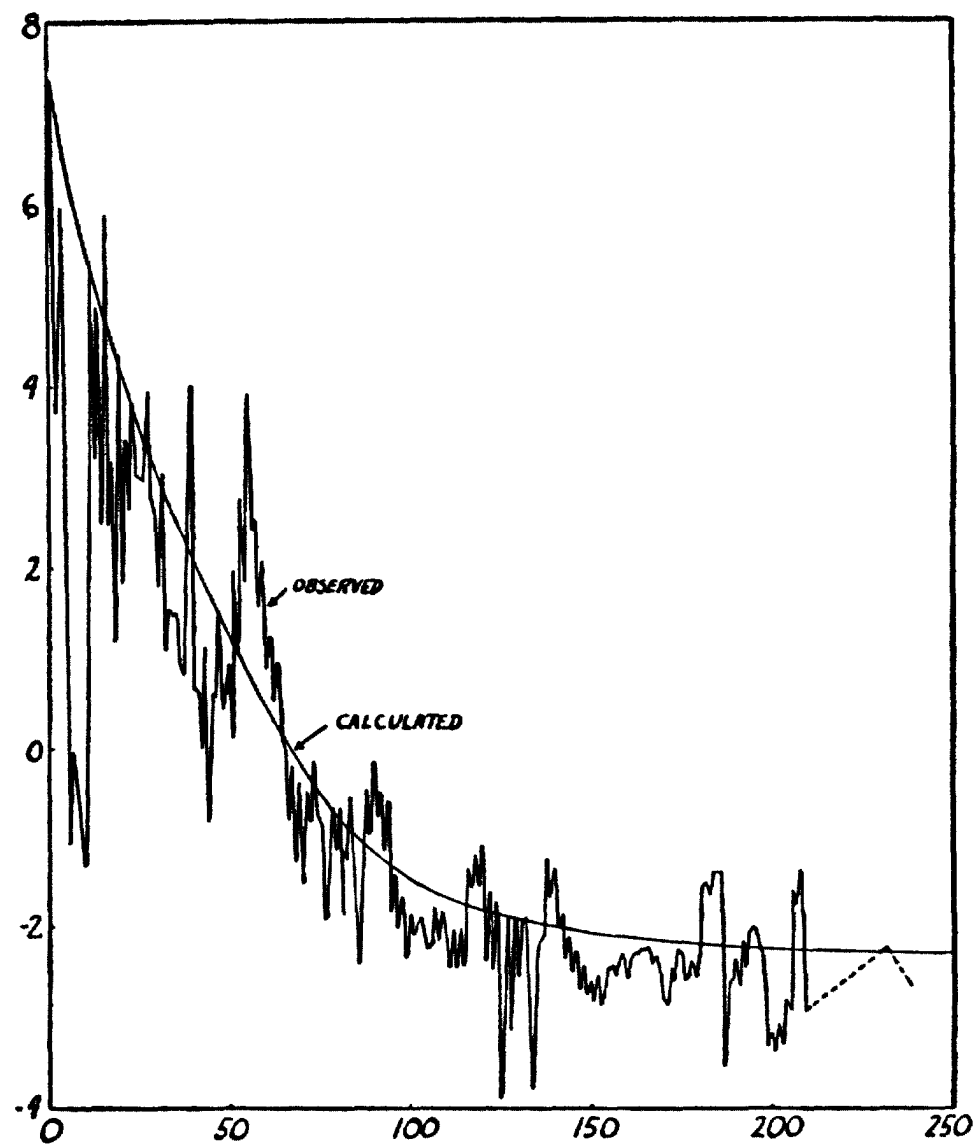
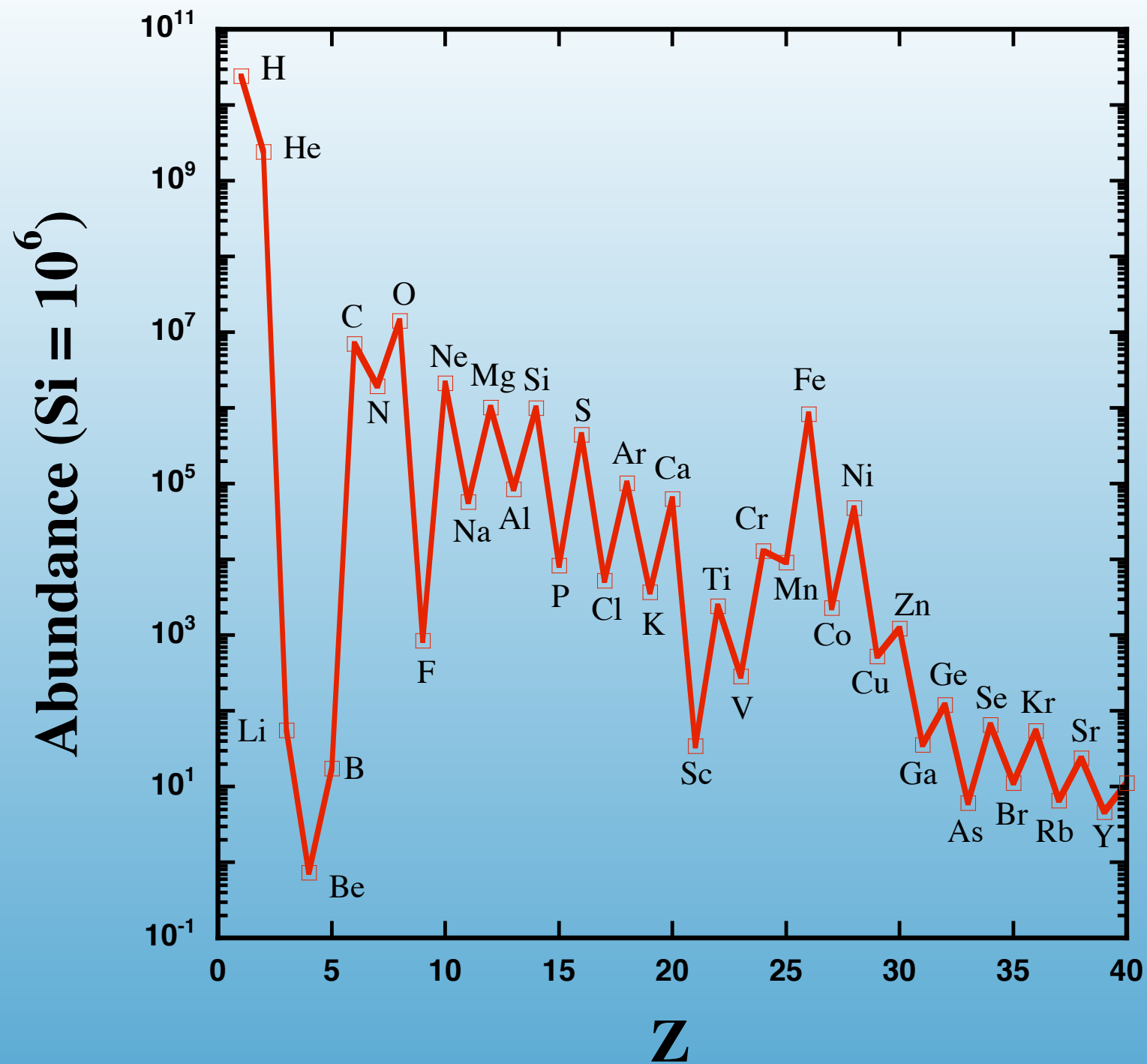


FIG. 1.

Log of relative abundance
Atomic weight



Historical Perspective

Intimate connection with CMB

Alpher
Herman
Gamow

Conditions for BBN:

Require $T > 100 \text{ keV} \Rightarrow t < 200 \text{ s}$

$$\sigma v(p + n \rightarrow D + \gamma) \approx 5 \times 10^{-20} \text{ cm}^3/\text{s}$$

$$\Rightarrow n_B \sim 1/\sigma v t \sim 10^{17} \text{ cm}^{-3}$$

Today:

$$n_{B0} \sim 10^{-7} \text{ cm}^{-3}$$

and

$$n_B \sim R^{-3} \sim T^3$$

Predicts the CMB temperature

$$T_o = (n_{B0} / n_B)^{1/3} T_{\text{BBN}} \sim 10 \text{ K}$$

Remarks on the Evolution of the Expanding Universe*,†

RALPH A. ALPHER AND ROBERT C. HERMAN

Applied Physics Laboratory, The Johns Hopkins University, Silver Spring, Maryland

(Received December 27, 1948)

Because of Eq. (4) a knowledge of ρ_m' and ρ_r' during the element forming period together with ρ_m'' fixes a value for ρ_r'' , the present radiation density, which is perhaps the least well-known quantity.

In accordance with Eq. (4), the specification of ρ_m'' , ρ_m' , and ρ_r' fixes the present density of radiation, ρ_r'' . In fact, we find that the value of ρ_r'' consistent with Eq. (4) is

$$\rho_r'' \cong 10^{-32} \text{ g/cm}^3, \quad (12d)$$

which corresponds to a temperature now of the order of 5°K. This mean temperature for the universe is to be interpreted as the background temperature which would result from the universal expansion alone. However, the thermal energy resulting from the nuclear energy production in stars would increase this value.

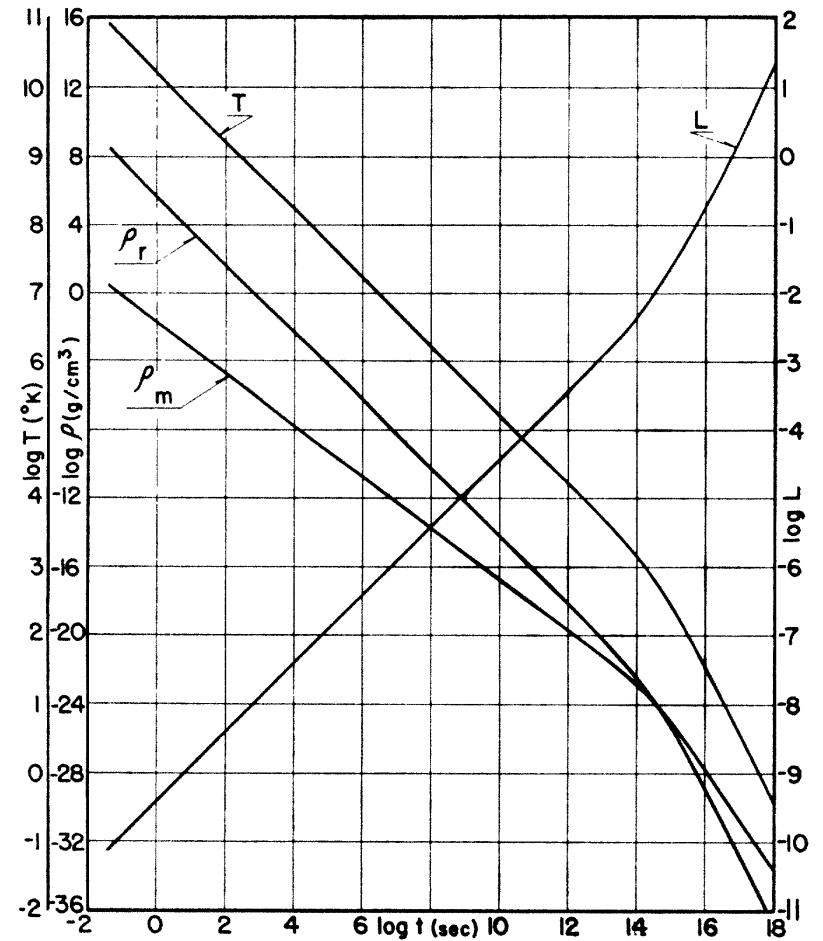


FIG. 1. The time dependence of the proper distance L , the densities of matter and radiation, ρ_m , and ρ_r , as well as the temperature, T , are shown for the case where $\rho_m'' \cong 10^{-30} \text{ g/cm}^3$, $\rho_r'' \cong 10^{-32} \text{ g/cm}^3$, $\rho_m' \cong 10^{-6} \text{ g/cm}^3$, and $\rho_r' \cong 1 \text{ g/cm}^3$. [See Eq. (12).]

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Because of Eq. (4) a knowledge of ρ_m' and ρ_r' during the element forming period fixes a value for ρ_r'' , the density, which is perhaps the quantity.

In order to study how sensitive this model is to the choice of densities, we have considered the following additional set of density values which satisfy Eq. (4):

$$\begin{aligned}\rho_m' &\cong 1.78 \times 10^{-4} \text{ g/cm}^3, \\ \rho_r' &\cong 1 \text{ g/cm}^3, \\ \rho_m'' &\cong 10^{-30} \text{ g/cm}^3, \\ \rho_r'' &\cong 10^{-35} \text{ g/cm}^3.\end{aligned}\tag{15}$$

In accordance with Eq. (4) and ρ_m'' , ρ_m' , and ρ_r' fixes the present density, ρ_r'' . In fact, we find that consistent with Eq. (4) is

$$\rho_r'' \cong 10^{-32} \text{ g/cm}^3, \tag{12d}$$

which corresponds to a temperature now of the order of 5°K. This mean temperature for the universe is to be interpreted as the background temperature which would result from the universal expansion alone. However, the thermal energy resulting from the nuclear energy production in stars would increase this value.

The value obtained for ρ_r'' in this case corresponds to a present mean temperature of about 1°K. The

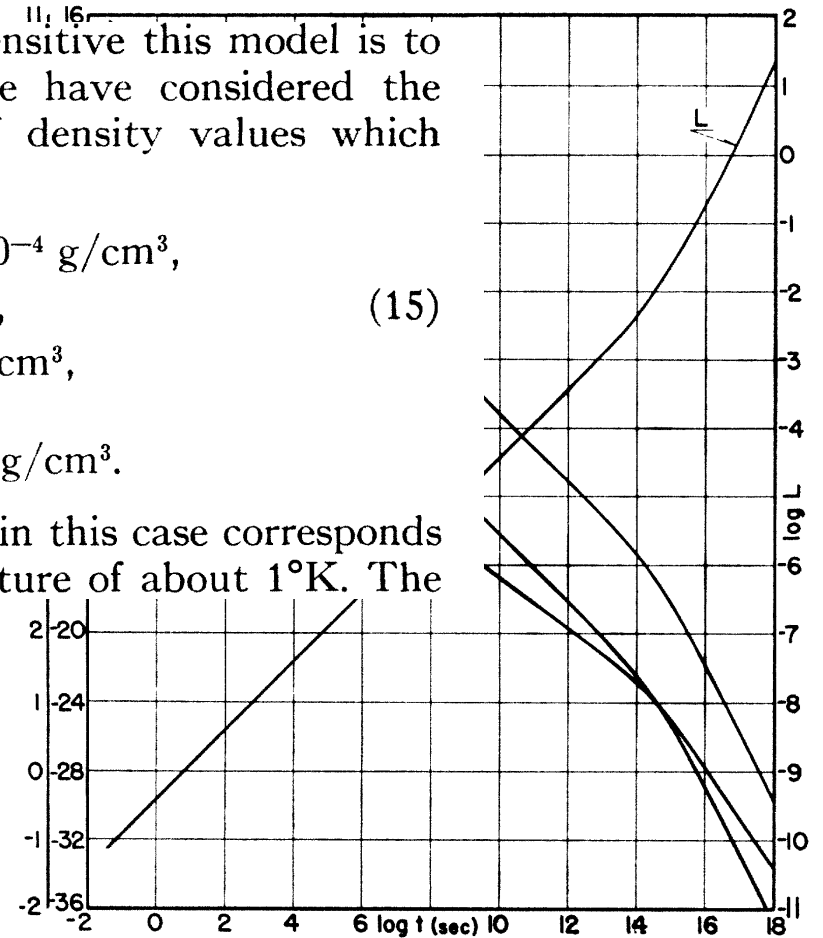
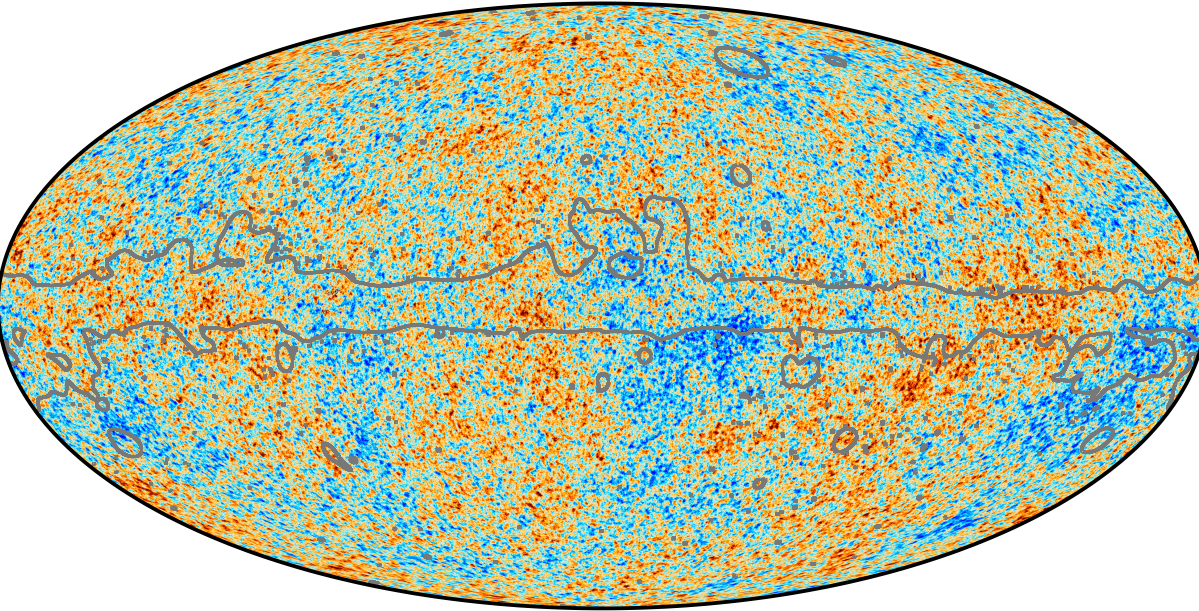


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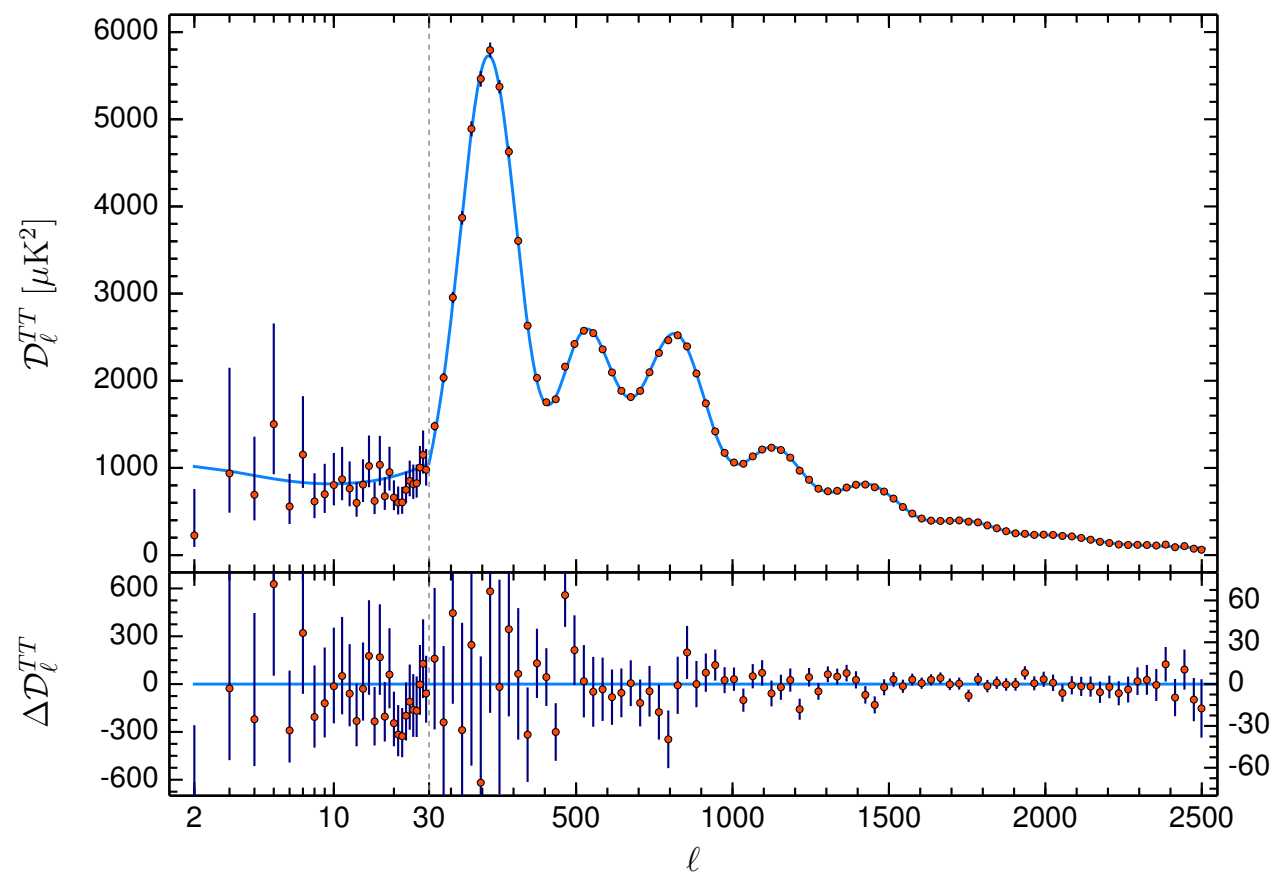
Planck best fit

$$\Omega_B h^2 = 0.02237 \pm 0.00015$$

$$\eta_{10} = 6.12 \pm 0.04$$

-300  300 μK

$$T = 2.7255 \pm 0.0006 \text{ K}$$



Conditions in the Early Universe:

$$T \gtrsim 1 \text{ MeV}$$

$$\rho = \frac{\pi^2}{30} \left(2 + \frac{7}{2} + \frac{7}{4} N_\nu \right) T^4$$

$$\eta = n_B/n_\gamma \sim 10^{-10}$$

β -Equilibrium maintained by weak interactions

Freeze-out at $\sim 1 \text{ MeV}$ determined by the competition of expansion rate $H \sim T^2/M_p$ and the weak interaction rate $\Gamma \sim G_F^2 T^5$

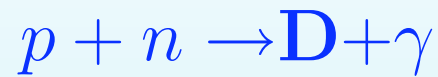
$$n + e^+ \leftrightarrow p + \bar{\nu}_e$$

$$n + \nu_e \leftrightarrow p + e^-$$

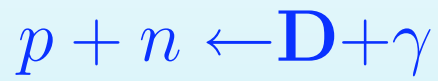
$$n \leftrightarrow p + e^- + \bar{\nu}_e$$

At freezeout n/p fixed modulo free neutron decay, $(n/p) \simeq 1/6 \rightarrow 1/7$

Nucleosynthesis Delayed (Deuterium Bottleneck)



$$\Gamma_p \sim n_B \sigma$$



$$\Gamma_d \sim n_\gamma \sigma e^{-E_B/T}$$

Nucleosynthesis begins when $\Gamma_p \sim \Gamma_d$

$$\frac{n_\gamma}{n_B} e^{-E_B/T} \sim 1 \quad @ \quad T \sim 0.1 \text{ MeV}$$

All neutrons \rightarrow ${}^4\text{He}$

$$Y_p = \frac{2(n/p)}{1 + (n/p)} \simeq 25\%$$

Remainder:

\mathbf{D} , ${}^3\text{He} \sim 10^{-5}$ and ${}^7\text{Li} \sim 10^{-10}$ by number

BBN could not explain the abundances (or patterns) of all the elements.

⇒ growth of stellar nucleosynthesis

But,

Questions persisted:

25% (by mass) of ^4He ?
D?

Resurgence:

BBN could successfully account for the abundance of

D, ^3He , ^4He , ^7Li .

1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18
1 H 1.008																	2 He 4.0026
3 Li 6.94	4 Be 9.0122											5 B 10.81	6 C 12.011	7 N 14.007	8 O 15.999	9 F 18.998	10 Ne 20.180
11 Na 22.990	12 Mg 24.305											13 Al 26.982	14 Si 28.085	15 P 30.974	16 S 32.06	17 Cl 35.45	18 Ar 39.948
19 K 39.098	20 Ca 40.078	21 Sc 44.956	22 Ti 47.867	23 V 50.942	24 Cr 51.996	25 Mn 54.938	26 Fe 55.845	27 Co 58.933	28 Ni 58.693	29 Cu 63.546	30 Zn 65.38	31 Ga 69.723	32 Ge 72.630	33 As 74.922	34 Se 78.971	35 Br 79.904	36 Kr 83.798
37 Rb 85.468	38 Sr 87.62	39 Y 88.906	40 Zr 91.224	41 Nb 92.906	42 Mo 95.95	43 Tc 96.906	44 Ru 101.07	45 Rh 102.91	46 Pd 106.42	47 Ag 107.87	48 Cd 112.41	49 In 114.82	50 Sn 118.71	51 Sb 121.76	52 Te 127.60	53 I 126.90	54 Xe 131.29
55 Cs 132.91	56 Ba 137.33	71 Lu 174.97	72 Hf 178.49	73 Ta 180.95	74 W 183.84	75 Re 186.21	76 Os 190.23	77 Ir 192.22	78 Pt 195.08	79 Au 196.97	80 Hg 200.59	81 Tl 204.38	82 Pb 207.2	83 Bi 208.98	84 Po 208.98	85 At 209.99	86 Rn 222.02
87 Fr 223.02	88 Ra 226.03	103 Lr 262.11	104 Rf 267.12	105 Db 270.13	106 Sg 269.13	107 Bh 270.13	108 Hs 269.13	109 Mt 278.16	110 Ds 281.17	111 Rg 281.17	112 Cn 285.18	113 Nh 286.18	114 Fl 289.19	115 Mc 289.20	116 Lv 293.20	117 Ts 293.21	118 Og 294.21

57 La 138.91	58 Ce 140.12	59 Pr 140.91	60 Nd 144.24	61 Pm 144.91	62 Sm 150.36	63 Eu 151.96	64 Gd 157.25	65 Tb 158.93	66 Dy 162.50	67 Ho 164.93	68 Er 167.26	69 Tm 168.93	70 Yb 173.05
89 Ac 227.03	90 Th 232.04	91 Pa 231.04	92 U 238.03	93 Np 237.05	94 Pu 244.06	95 Am 243.06	96 Cm 247.07	97 Bk 247.07	98 Cf 251.08	99 Es 252.08	100 Fm 257.10	101 Md 258.10	102 No 259.10



η vs $\Omega_B h^2$

baryon density

$$\rho_B = m_N n_N = \Omega_B \rho_c \left(\frac{T}{T_0} \right)^3$$

then

$$\eta = \frac{n_B}{n_\gamma} = \Omega_B \frac{\rho_c}{m_N n_\gamma}$$

$$\rho_c = 1.05 \times 10^{-5} h^2 \text{GeV}/\text{cm}^3$$

$$n_\gamma = 411 \text{cm}^{-3}$$

$$\eta = 2.73 \times 10^{-8} \Omega_B h^2$$

$$\Omega_B h^2 = 3.66 \times 10^7 \eta$$

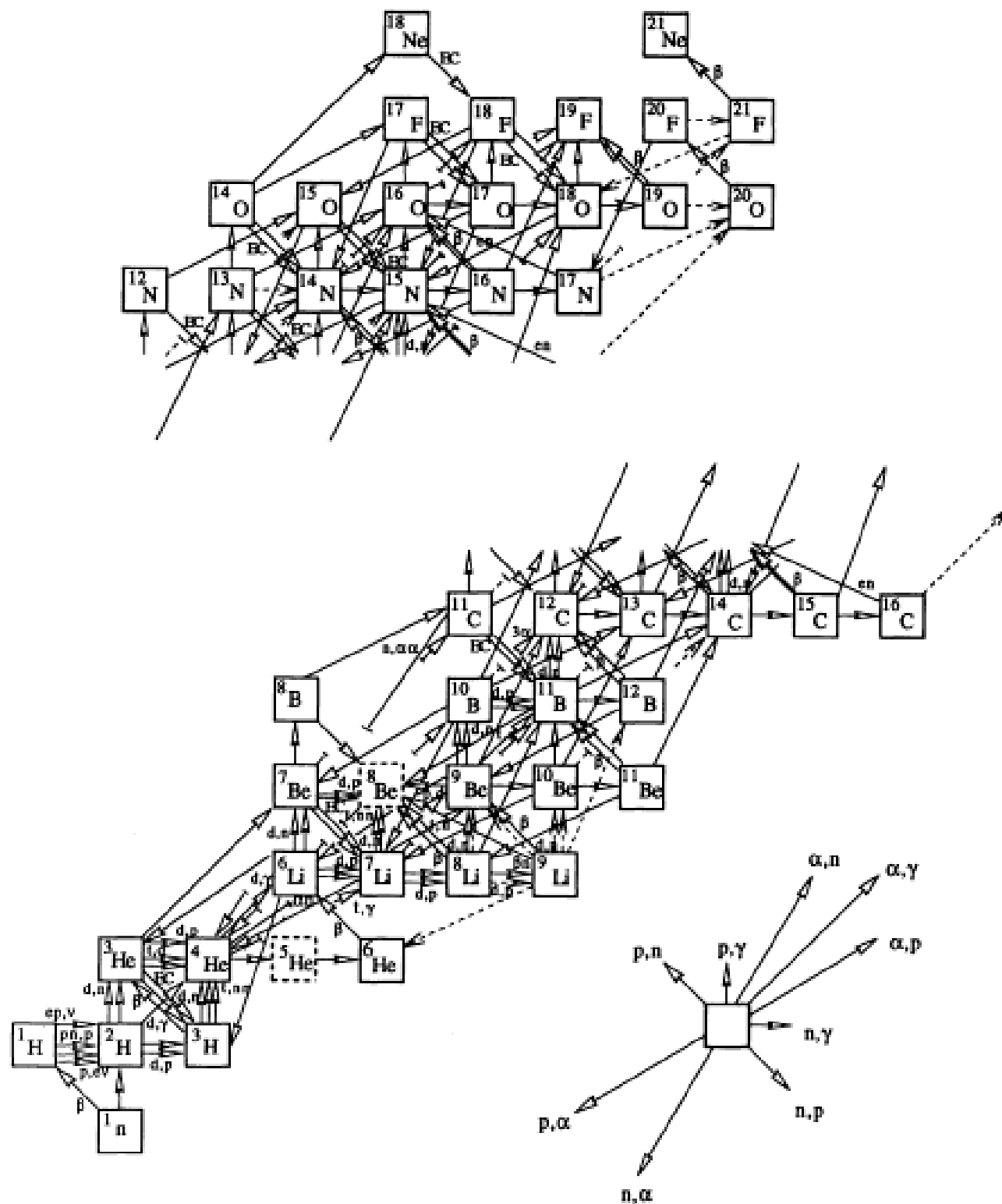
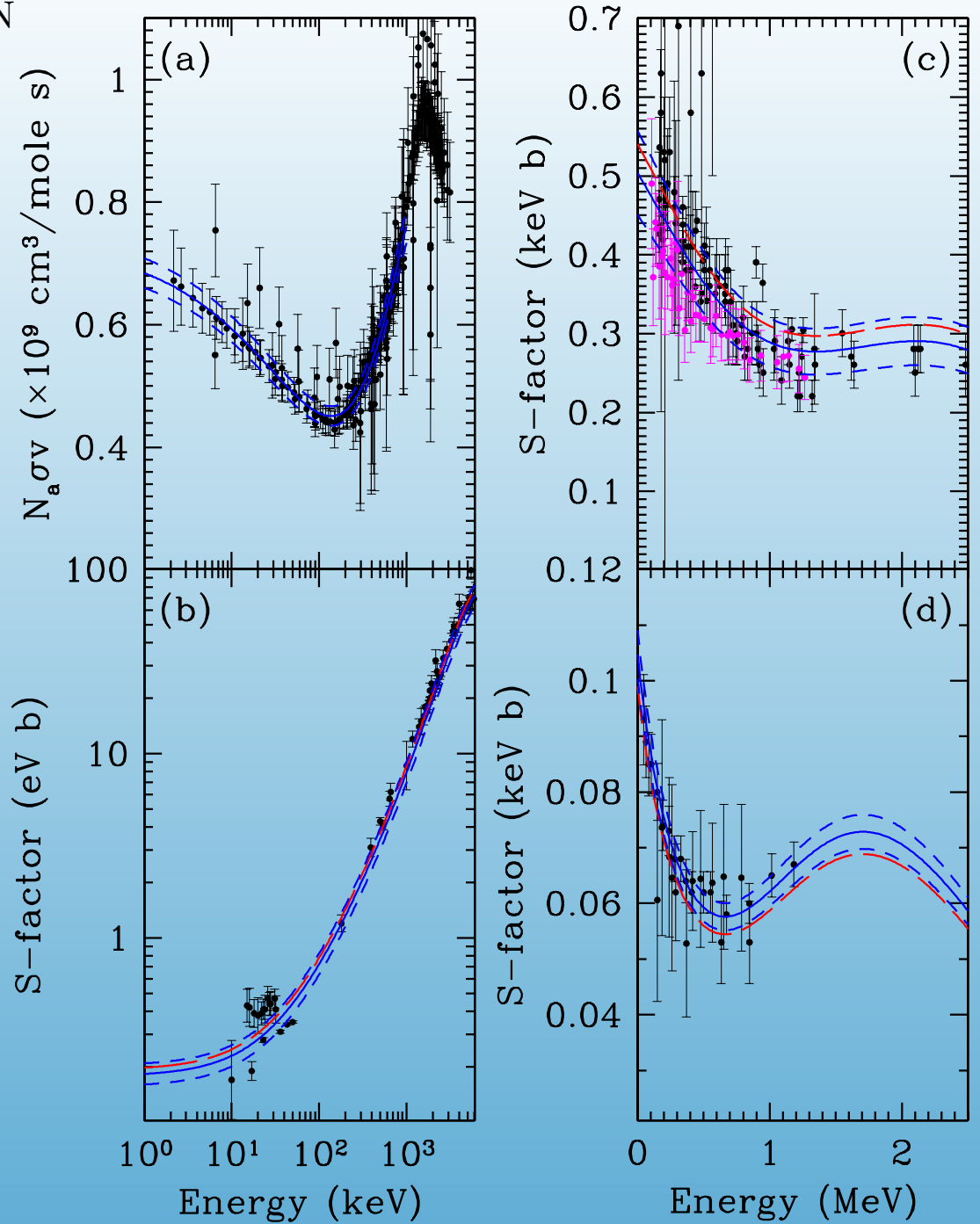


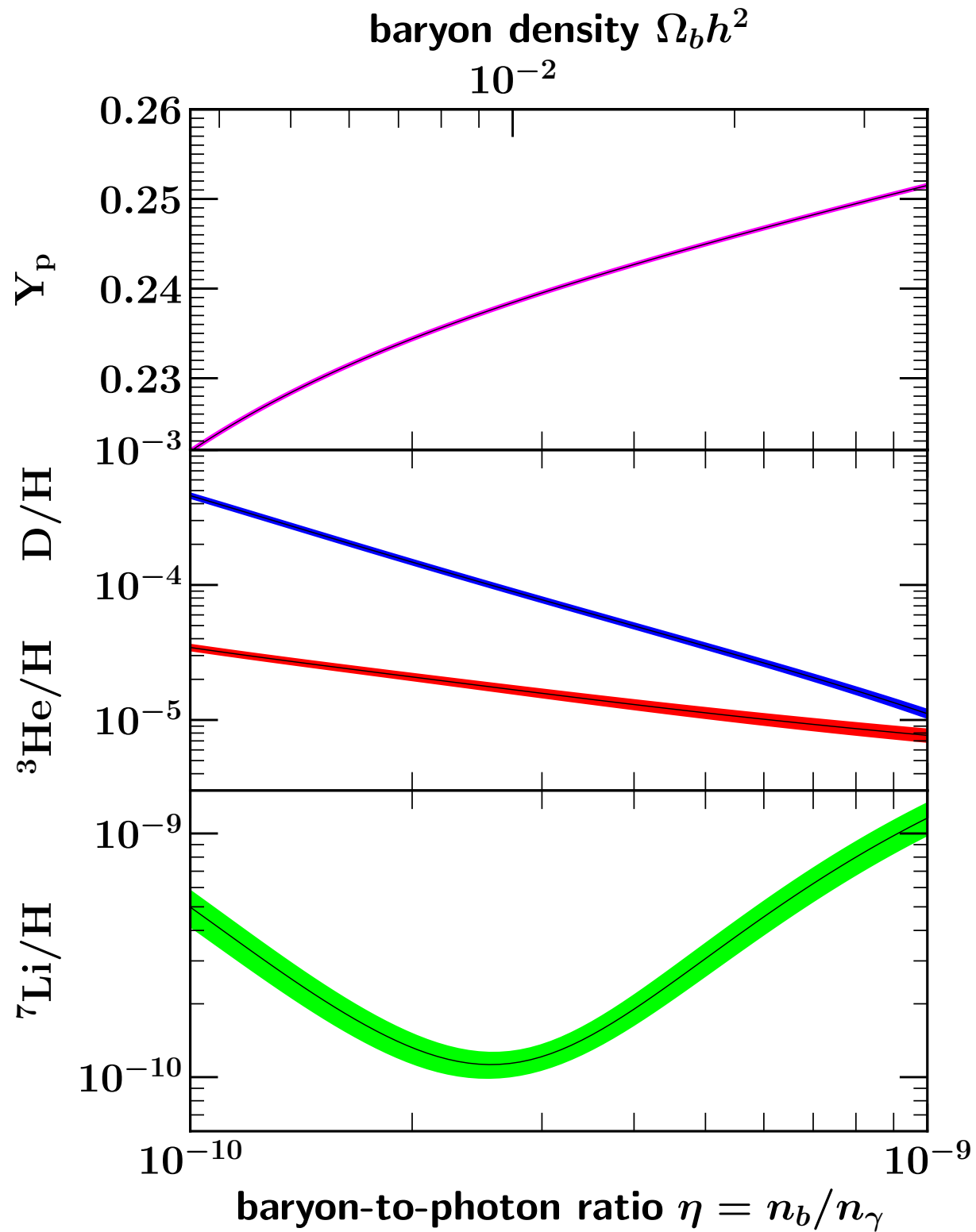
FIG. 1.—Reaction network used in the code. Estimated reactions are shown with dashed lines.

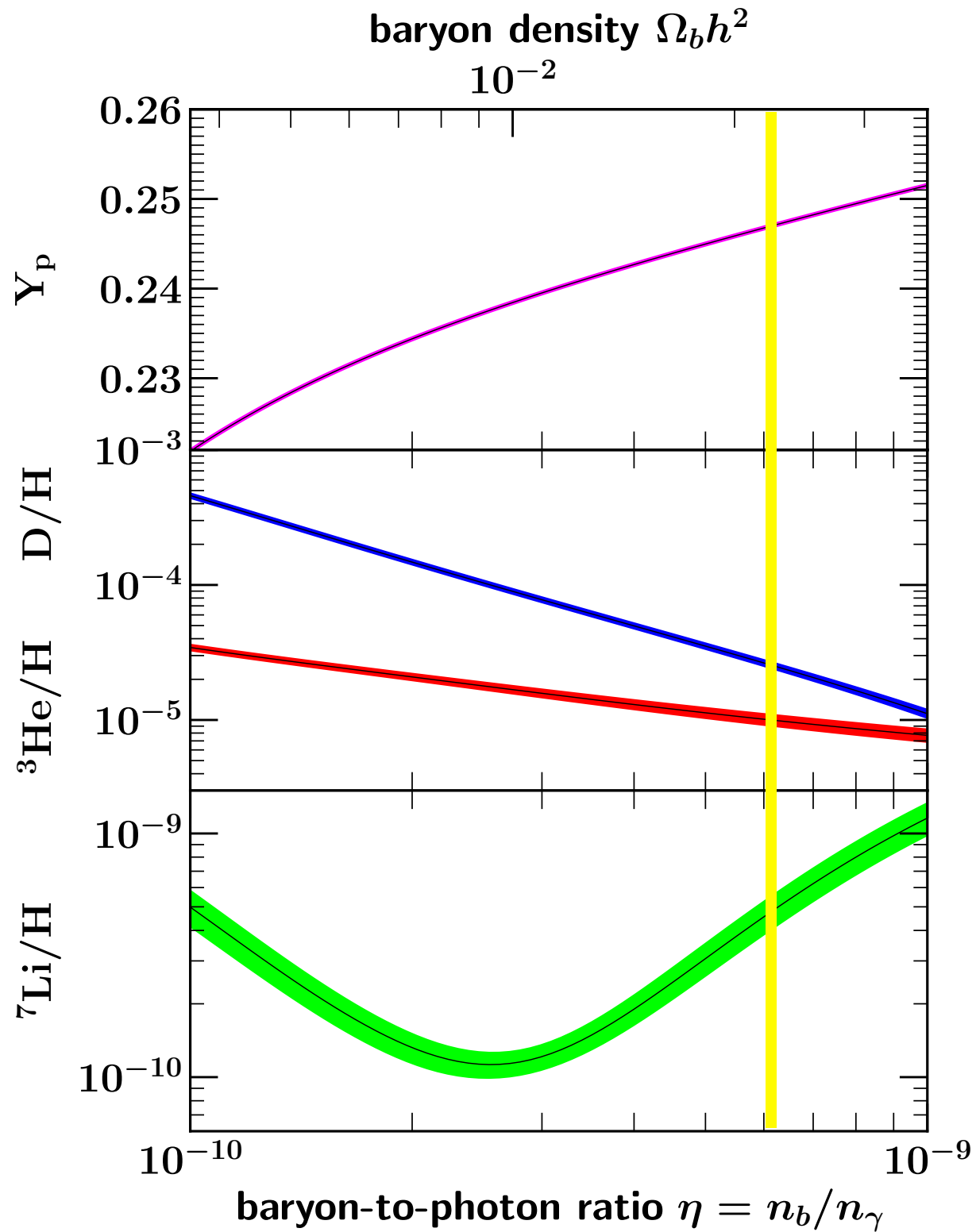
Table 1: Key Nuclear Reactions for BBN

Source	Reactions
NACRE	$d(p, \gamma)^3\text{He}$ (b)
	$d(d, n)^3\text{He}$
	$d(d, p)t$
	$t(d, n)^4\text{He}$
	$t(\alpha, \gamma)^7\text{Li}$ (d)
	$^3\text{He}(\alpha, \gamma)^7\text{Be}$ (c)
SKM	$^7\text{Li}(p, \alpha)^4\text{He}$
	$p(n, \gamma)d$
	$^3\text{He}(d, p)^4\text{He}$
This work	$^7\text{Be}(n, p)^7\text{Li}$ (See below)
	$^3\text{He}(n, p)t$ (a)
PDG	τ_n

NACRE
Cyburt, Fields, KAO
Nollett & Burles
Coc et al.







Observations

- Production of the Light Elements: D, ^3He , ^4He , ^7Li
 - ^4He observed in extragalactic HII regions:
abundance by mass = 25%
 - ^7Li observed in the atmospheres of dwarf halo stars:
abundance by number = 10^{-10}
 - D observed in quasar absorption systems (and locally):
abundance by number = 3×10^{-5}
 - ^3He in solar wind, in meteorites, and in the ISM:
abundance by number = 10^{-5}

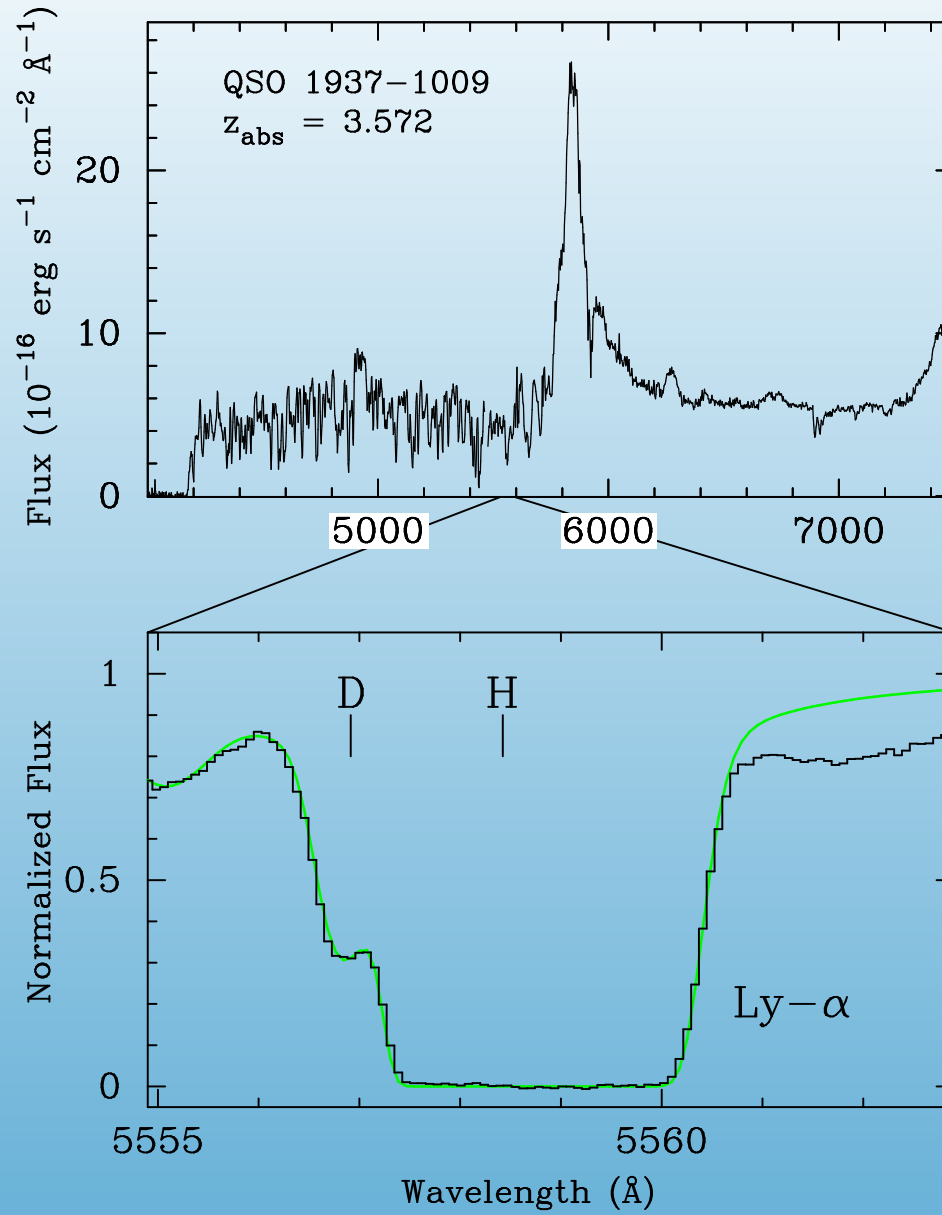
D/H

- All Observed D is Primordial!
- Observed in the ISM and inferred from meteoritic samples (also HD in Jupiter)
- D/H observed in Quasar Absorption systems

Table 3. PRECISION D/H MEASURES CONSIDERED IN THIS PAPER

QSO	z_{em}	z_{abs}	$\log_{10} N(\text{H I})/\text{cm}^{-2}$	$[\text{O}/\text{H}]^{\text{a}}$	$\log_{10} N(\text{D I})/N(\text{H I})$
HS 0105+1619	2.652	2.53651	19.426 ± 0.006	-1.771 ± 0.021	-4.589 ± 0.026
Q0913+072	2.785	2.61829	20.312 ± 0.008	-2.416 ± 0.011	-4.597 ± 0.018
Q1243+307	2.558	2.52564	19.761 ± 0.026	-2.769 ± 0.028	-4.622 ± 0.015
SDSS J1358+0349	2.894	2.85305	20.524 ± 0.006	-2.804 ± 0.015	-4.582 ± 0.012
SDSS J1358+6522	3.173	3.06726	20.495 ± 0.008	-2.335 ± 0.022	-4.588 ± 0.012
SDSS J1419+0829	3.030	3.04973	20.392 ± 0.003	-1.922 ± 0.010	-4.601 ± 0.009
SDSS J1558-0031	2.823	2.70242	20.75 ± 0.03	-1.650 ± 0.040	-4.619 ± 0.026

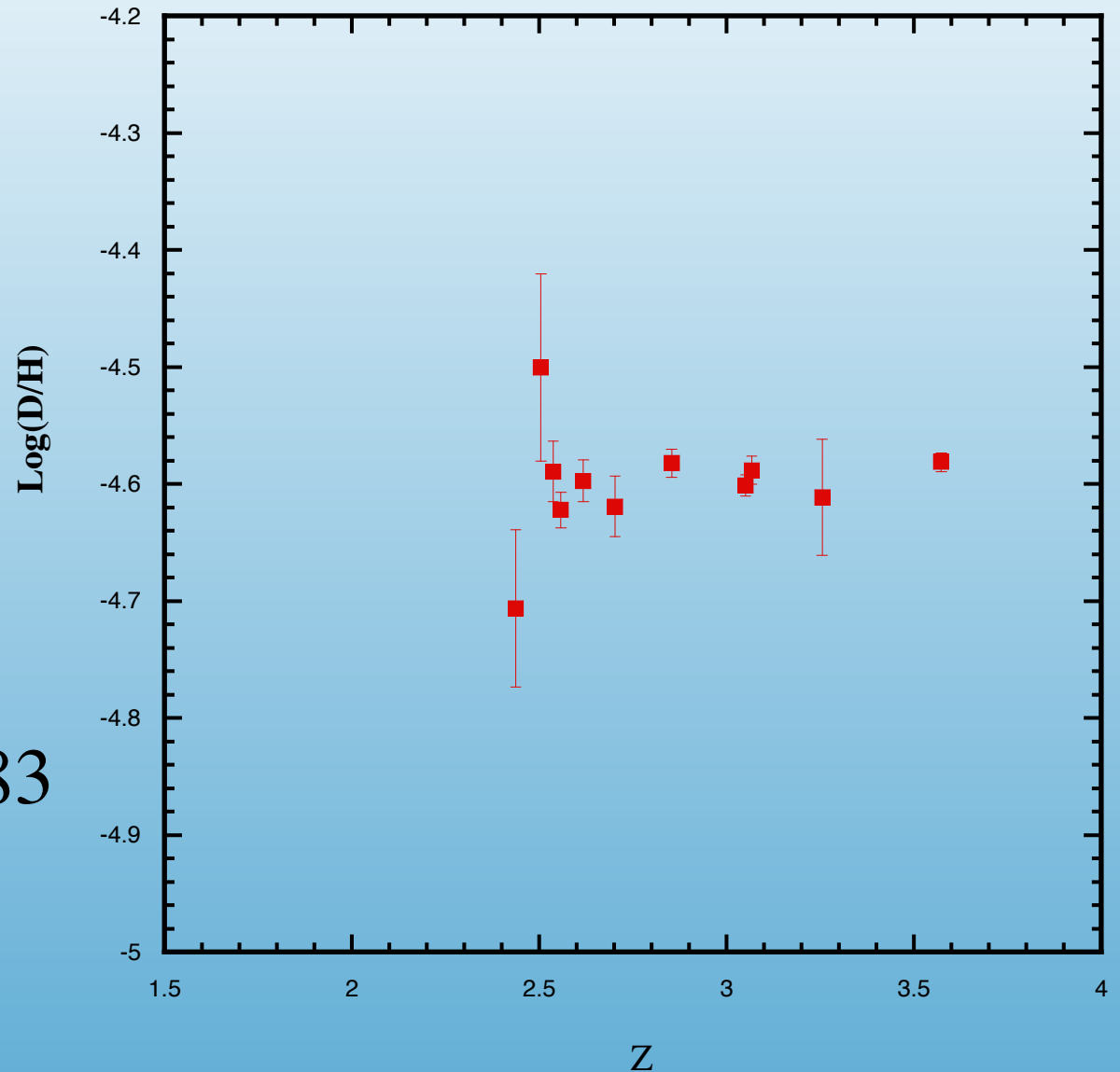
^aWe adopt the solar value $\log_{10} (\text{O}/\text{H}) + 12 = 8.69$ ([Asplund et al. 2009](#)).



Updated D/H abundances in Quasar absorption systems

BBN Prediction:
 $10^5 \text{ D/H} = 2.506 \pm 0.083$

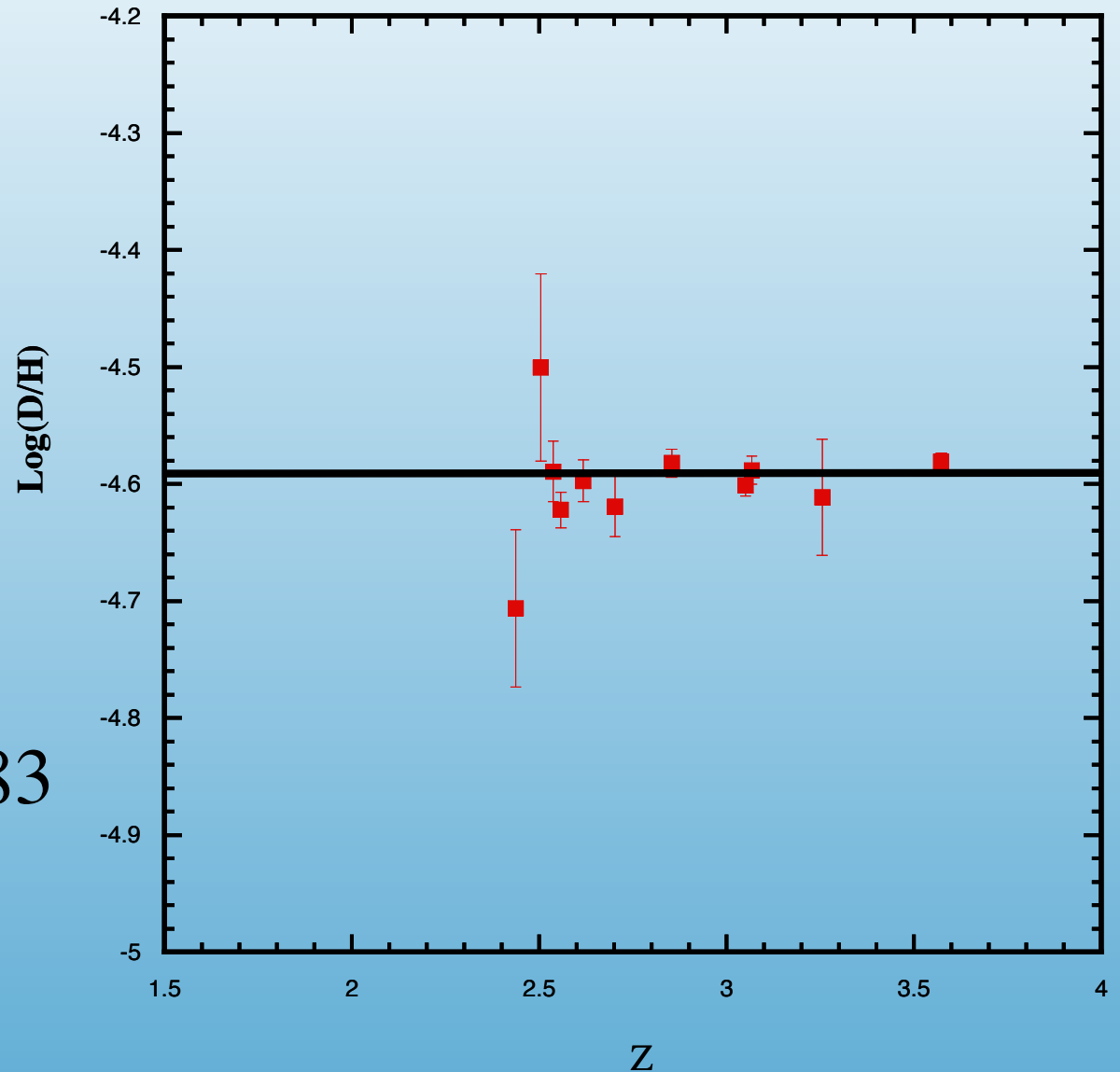
Obs Average:
 $10^5 \text{ D/H} = 2.55 \pm 0.03$

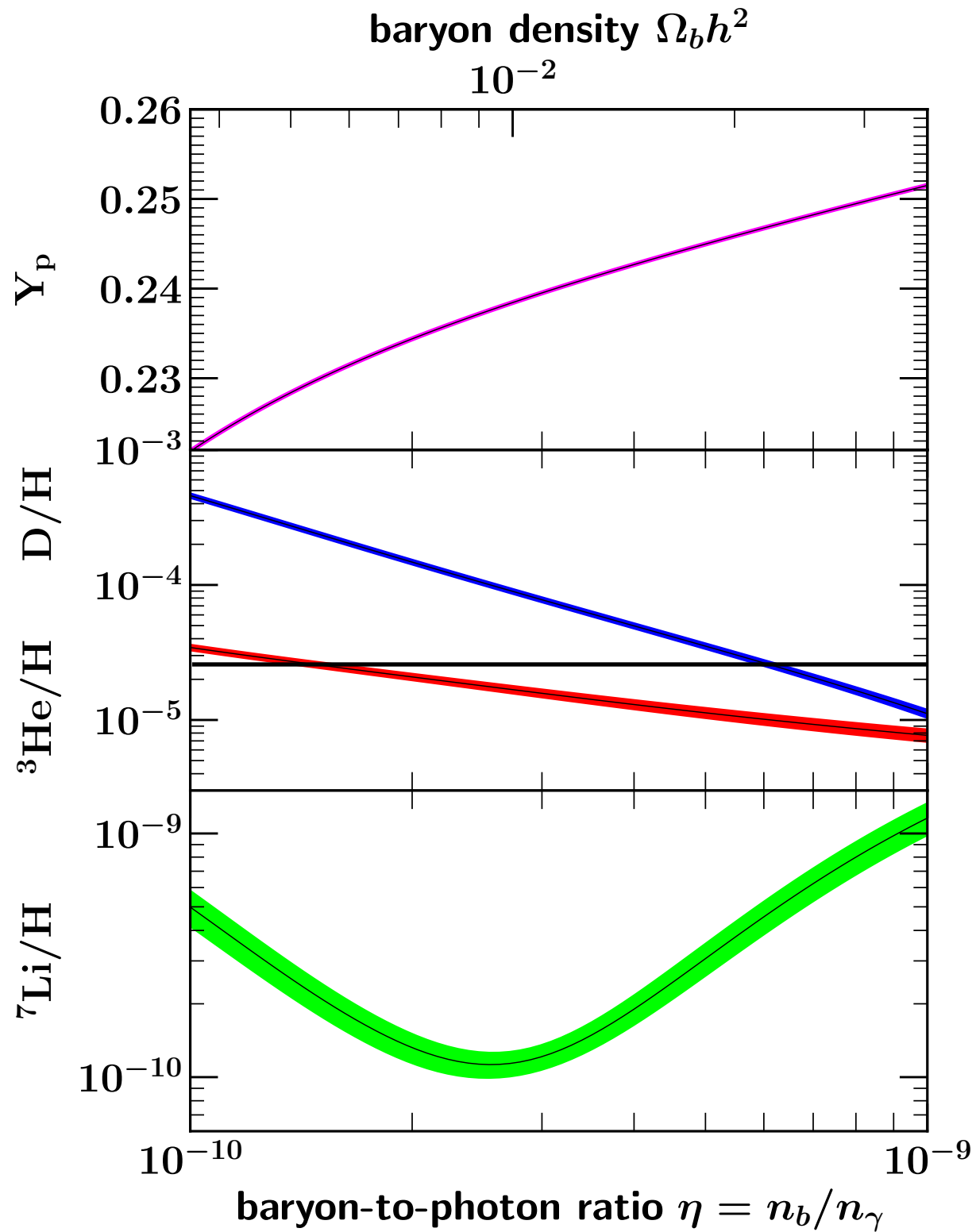


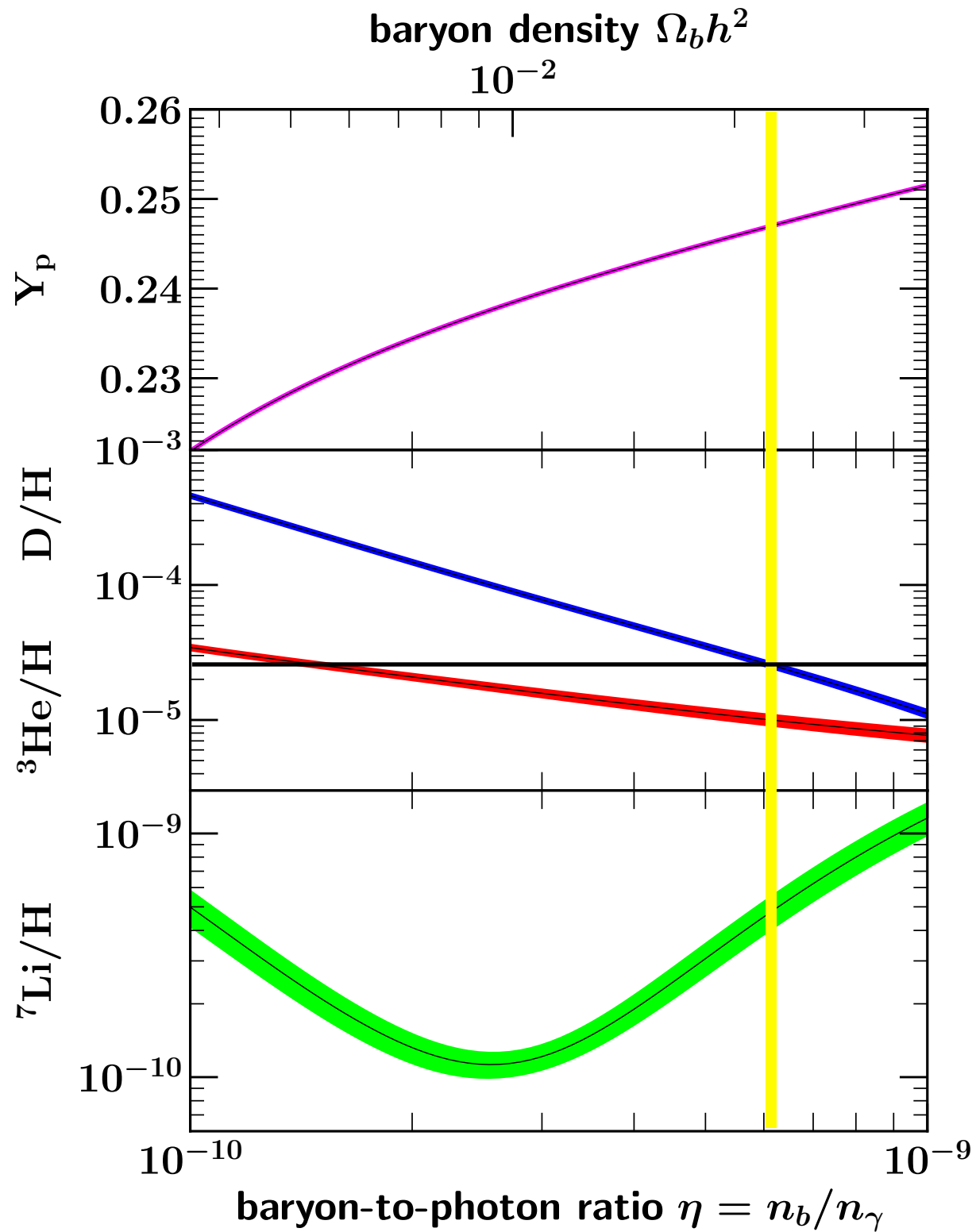
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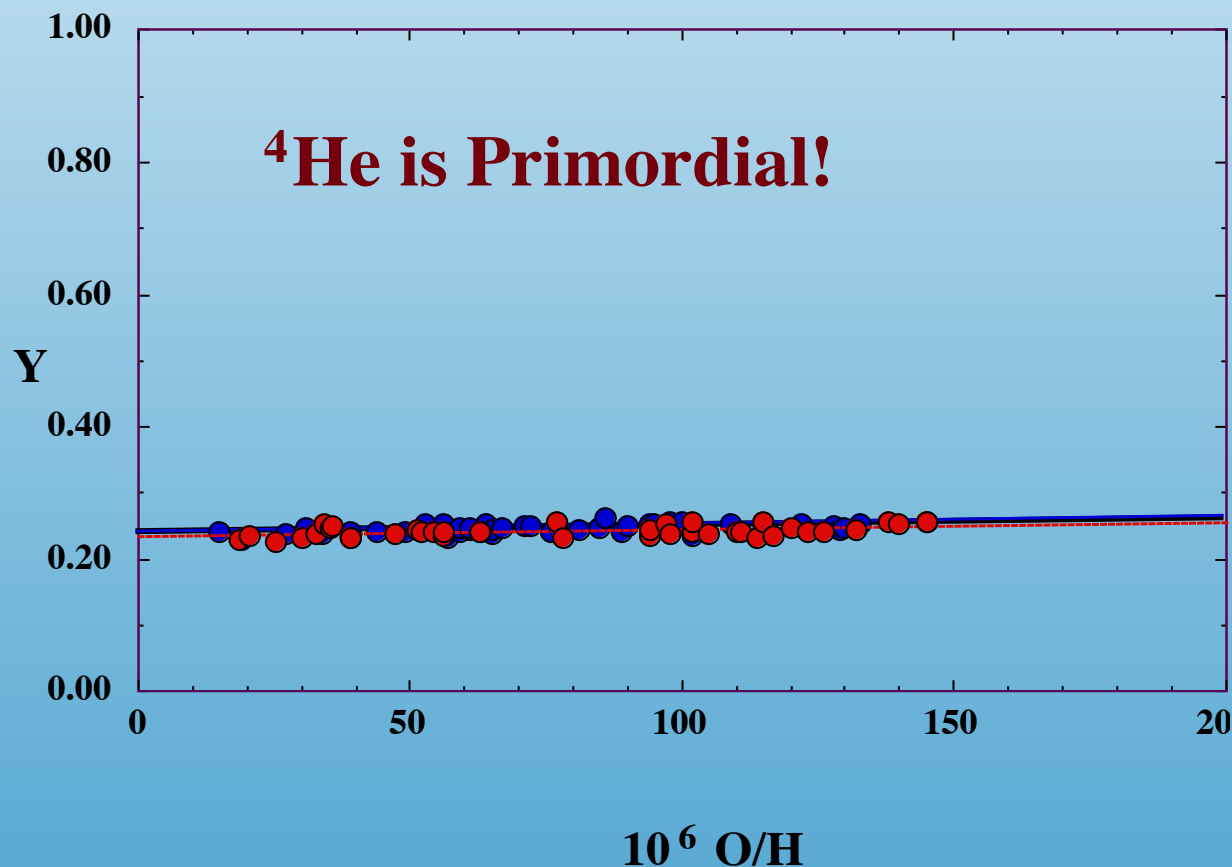


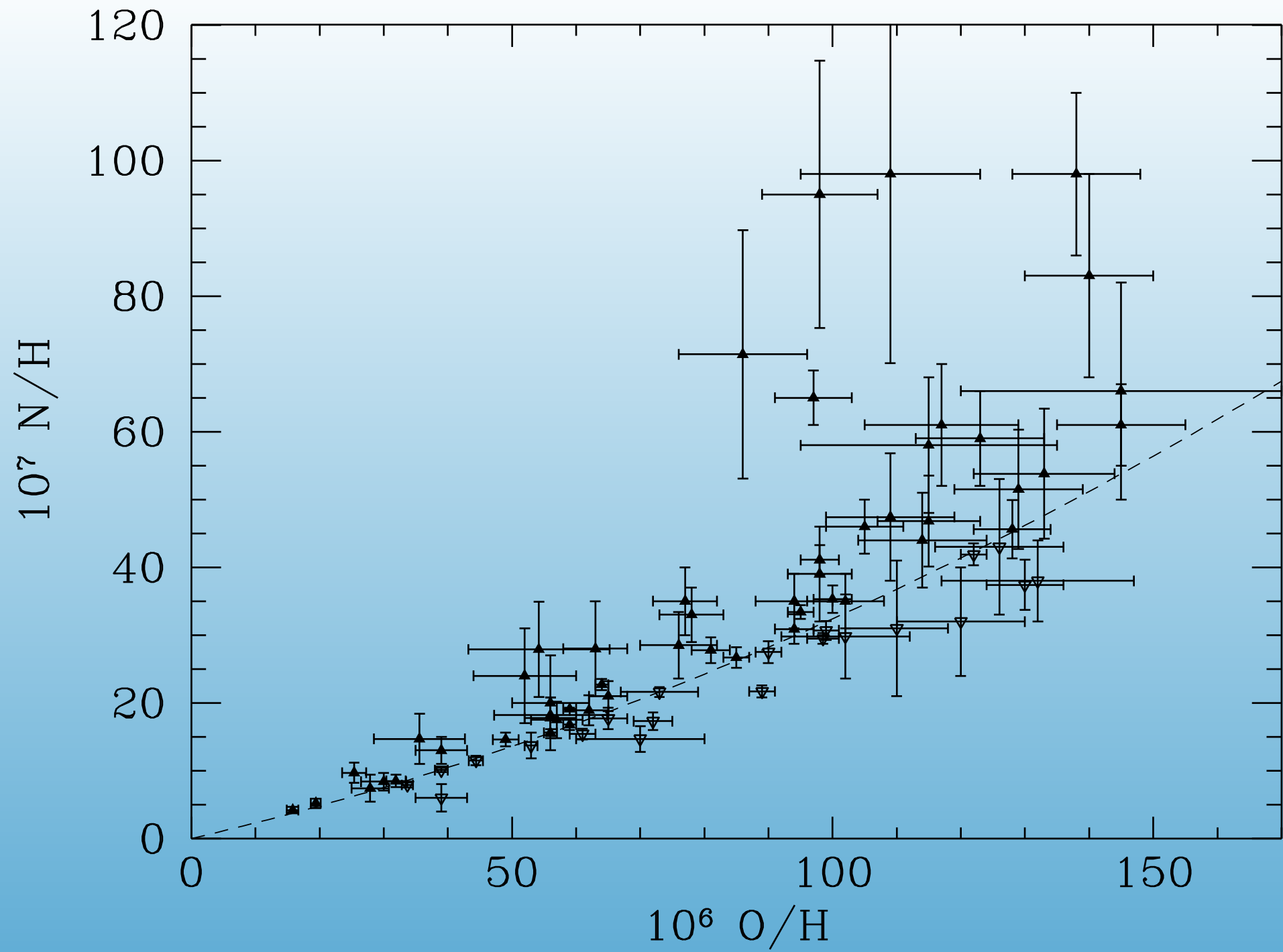


^4He

Measured in low metallicity extragalactic HII regions (~ 100) together with O/H and N/H

$$Y_P = Y(\text{O/H} \rightarrow 0)$$





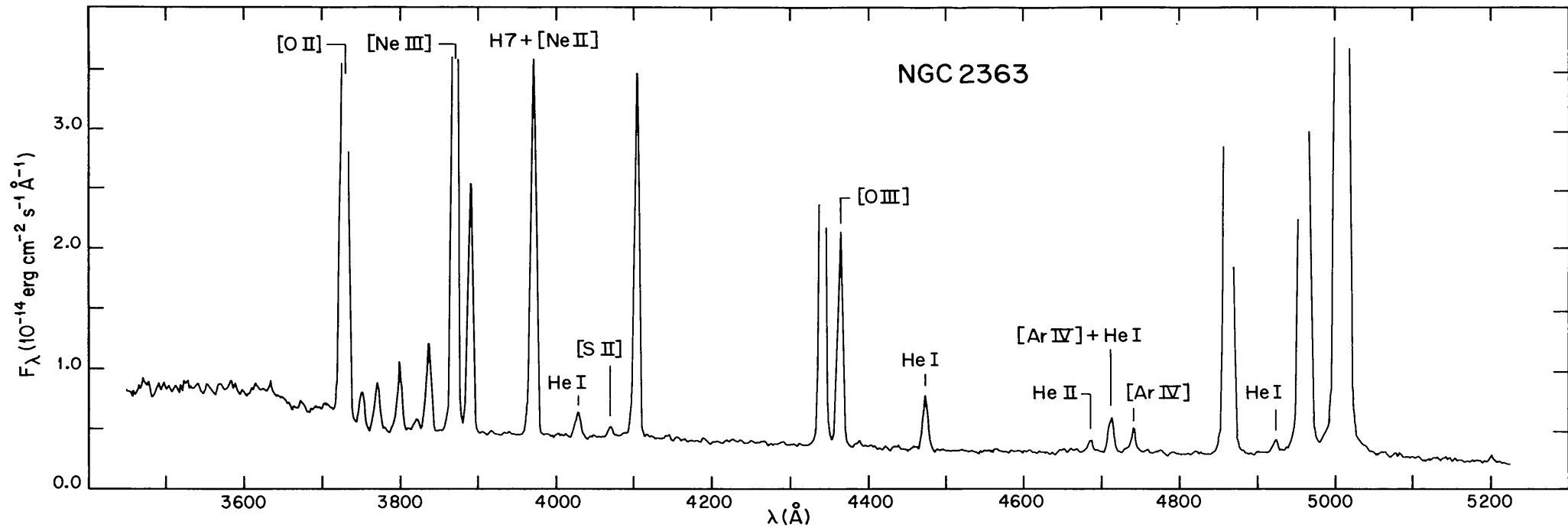


Fig. 1. Low dispersion blue spectrogram of NGC 2363, showing the faintest lines measured

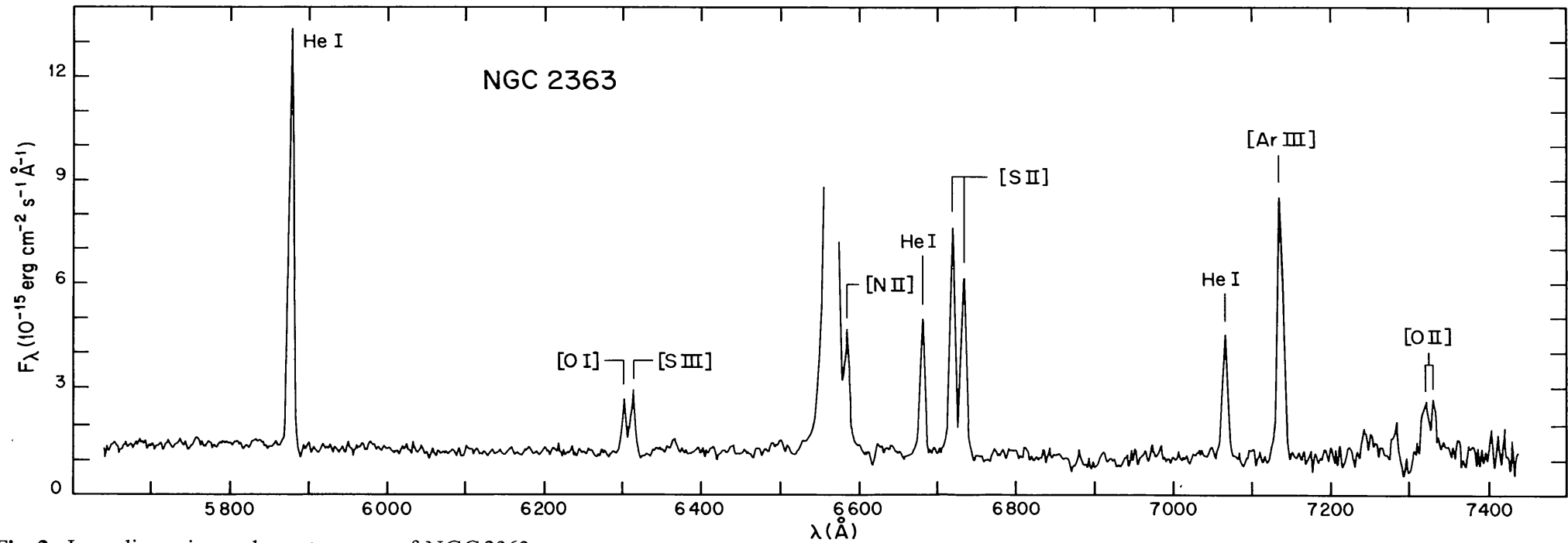
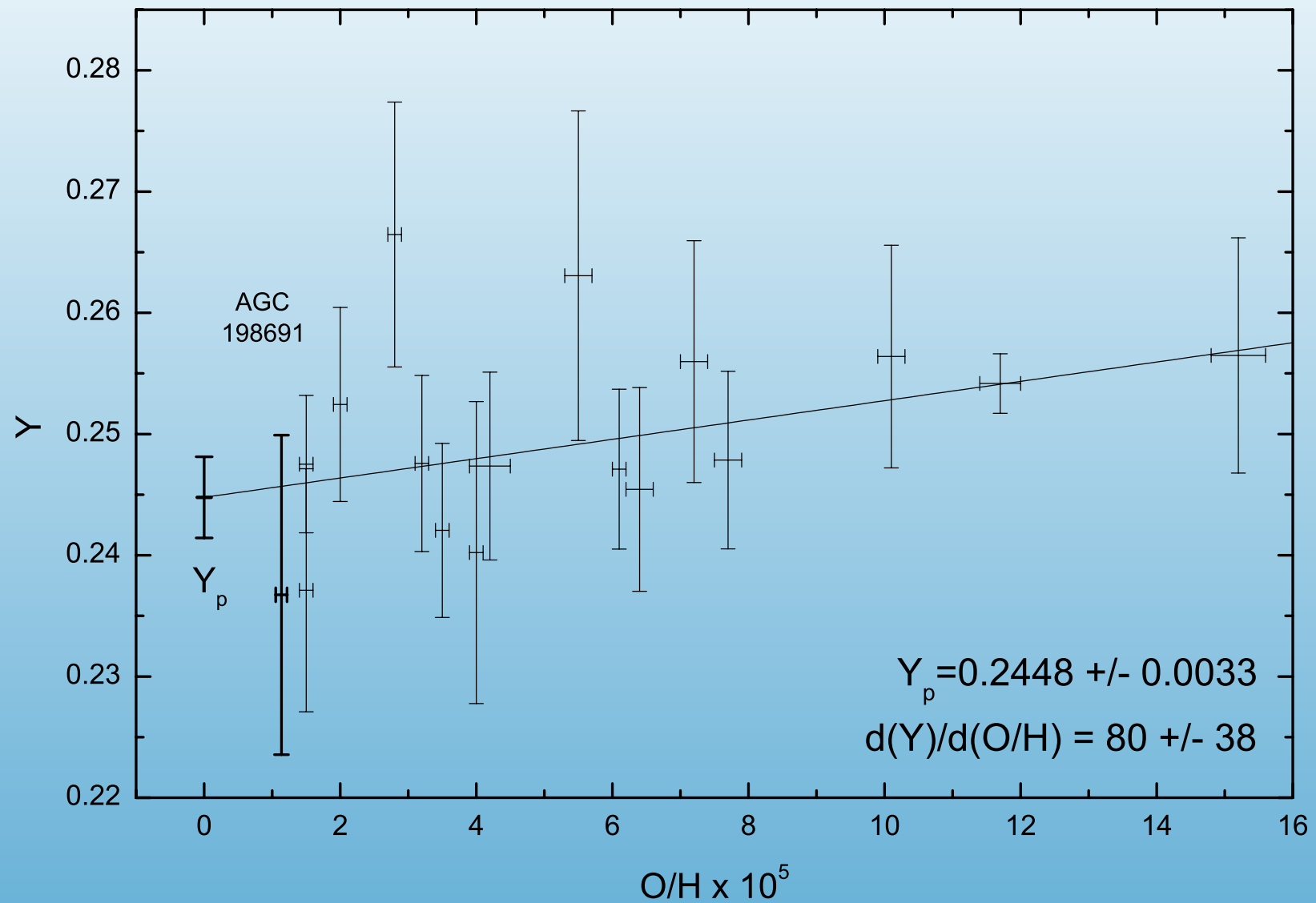


Fig. 2. Low dispersion red spectrogram of NGC 2363

Most recent addition: AGC 198691 (2021)

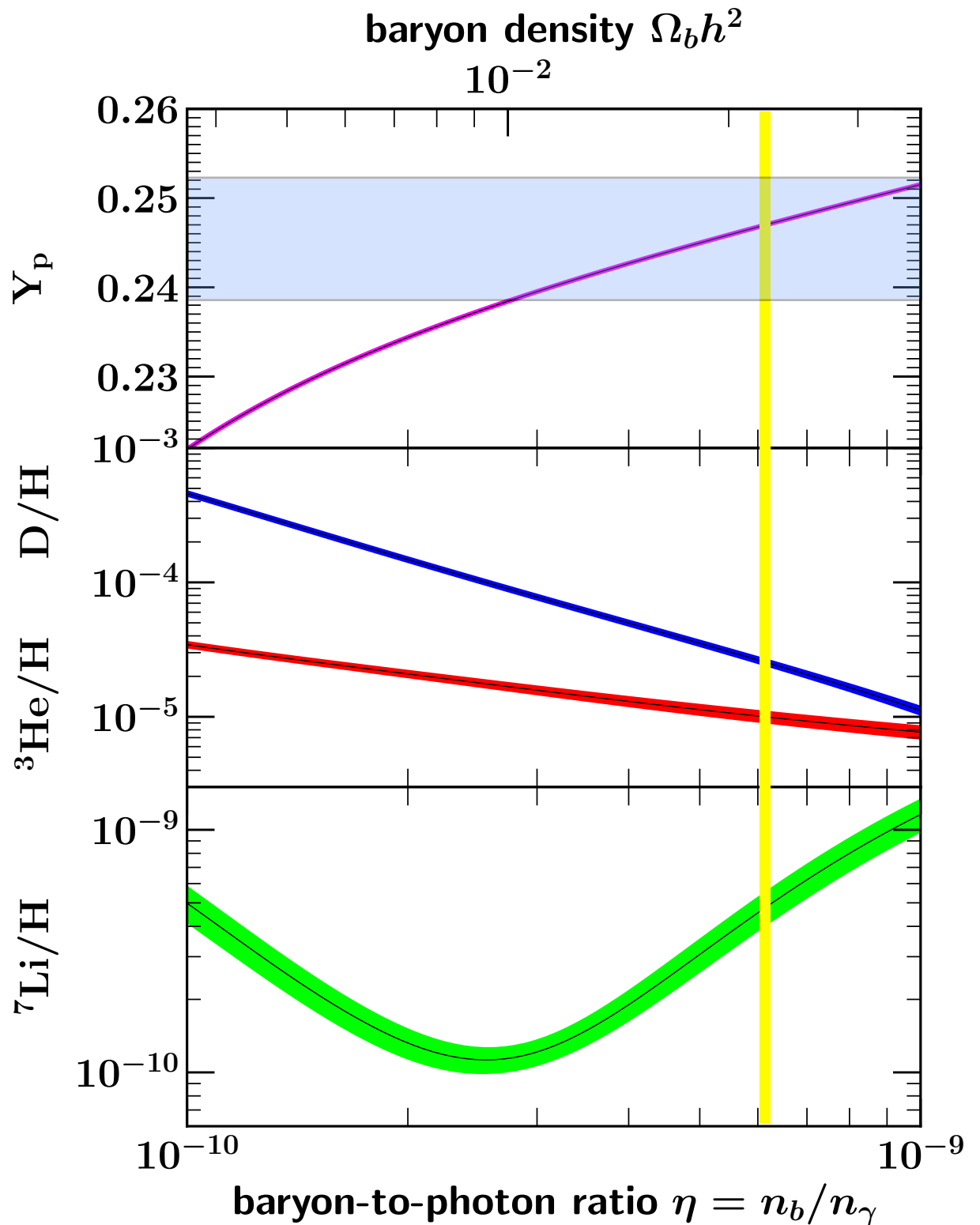


prior: $Y_P = .2453 \pm 0.0034$

Aver, Berg, Hirschauer, Olive,
Pogge, Rogers,
Salzer, Skillman

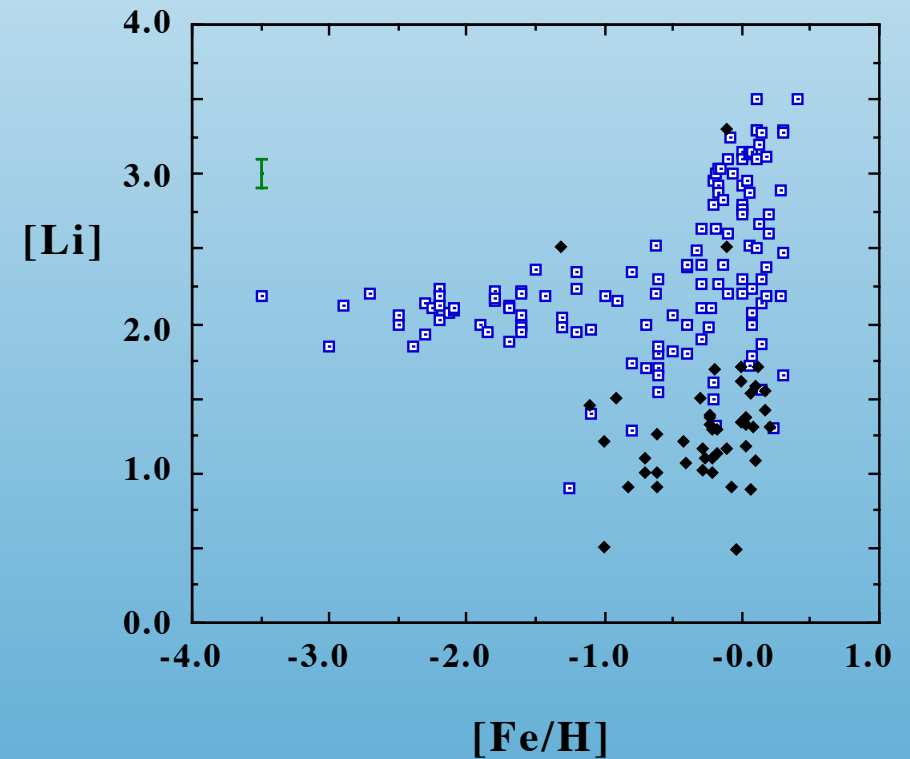
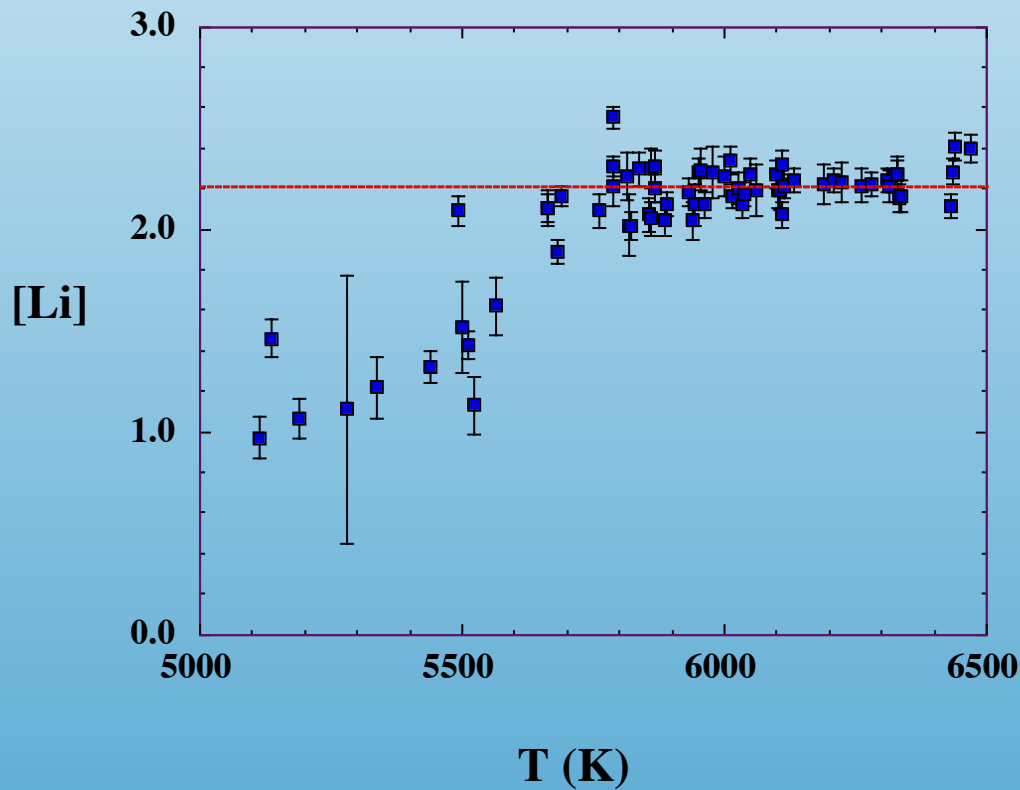
^4He Prediction:
 0.2467 ± 0.0002

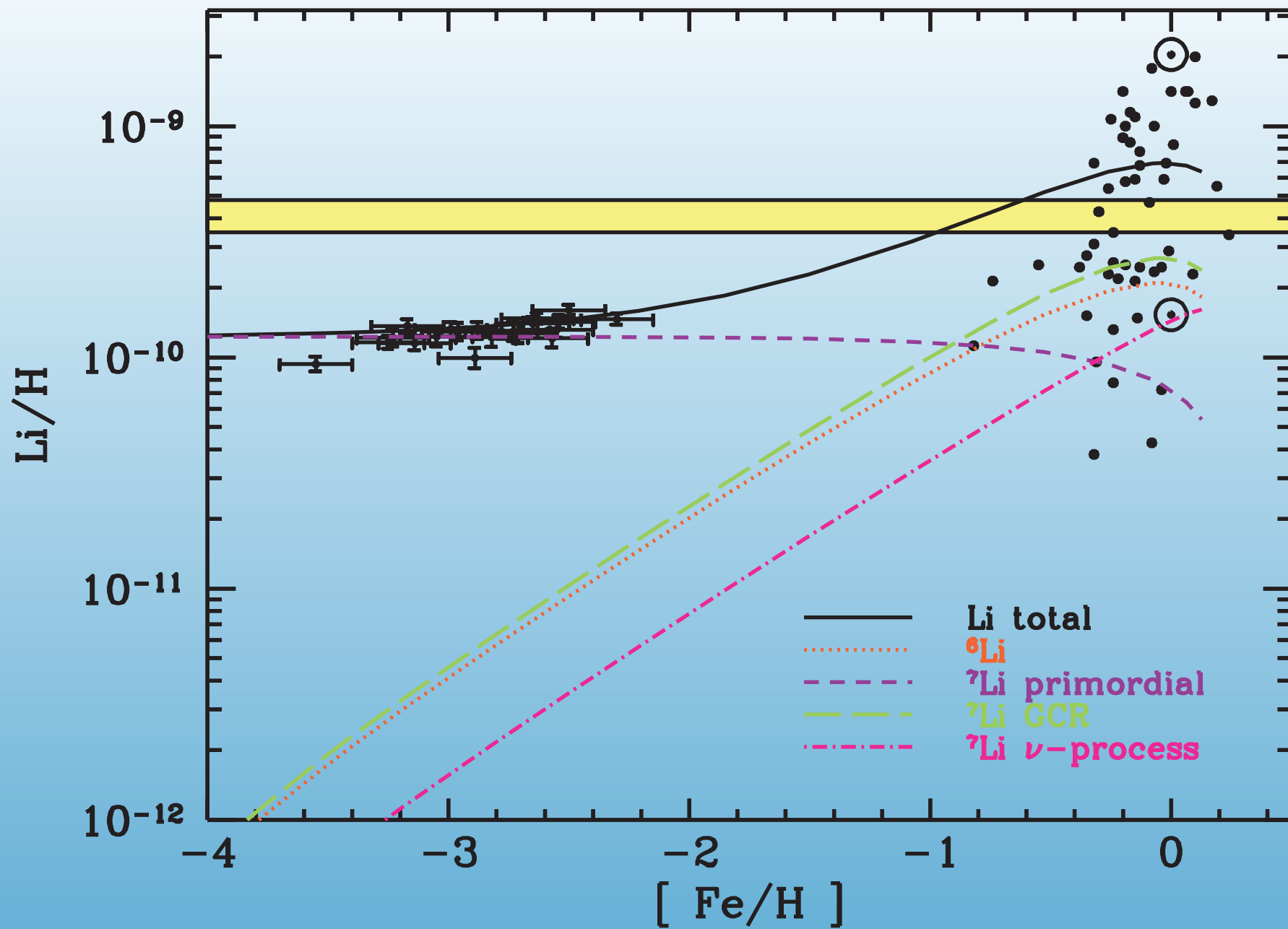
Data: Regression:
 0.2448 ± 0.0033



Li/H

Measured in low metallicity dwarf halo stars
(over 100 observed)





Possible sources for the discrepancy

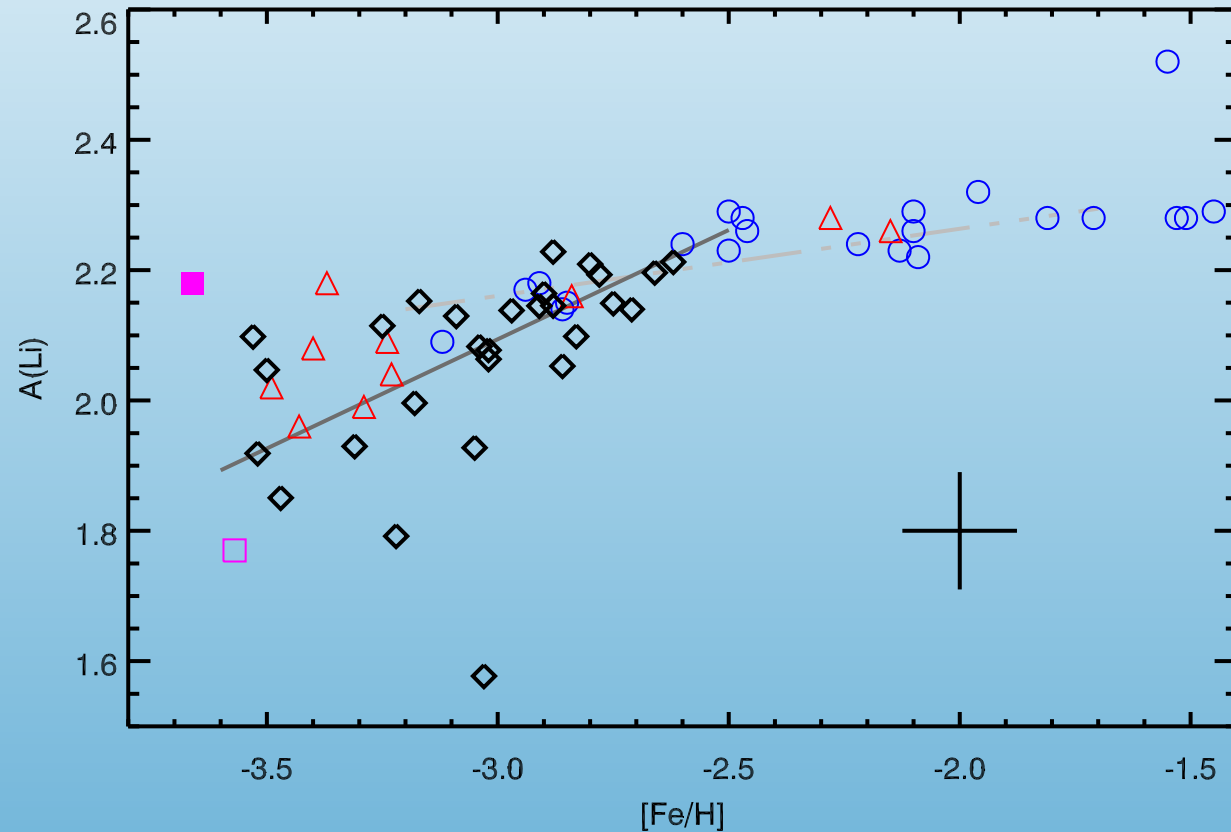
- Nuclear Rates/Resonant reactions
- Stellar parameters
- Stellar Depletion
- Decaying Particles
- Axion Cooling
- Variable Constants

Arguments against stellar depletion

- Lack of dispersion in the plateau
- Observation of ${}^6\text{Li}$

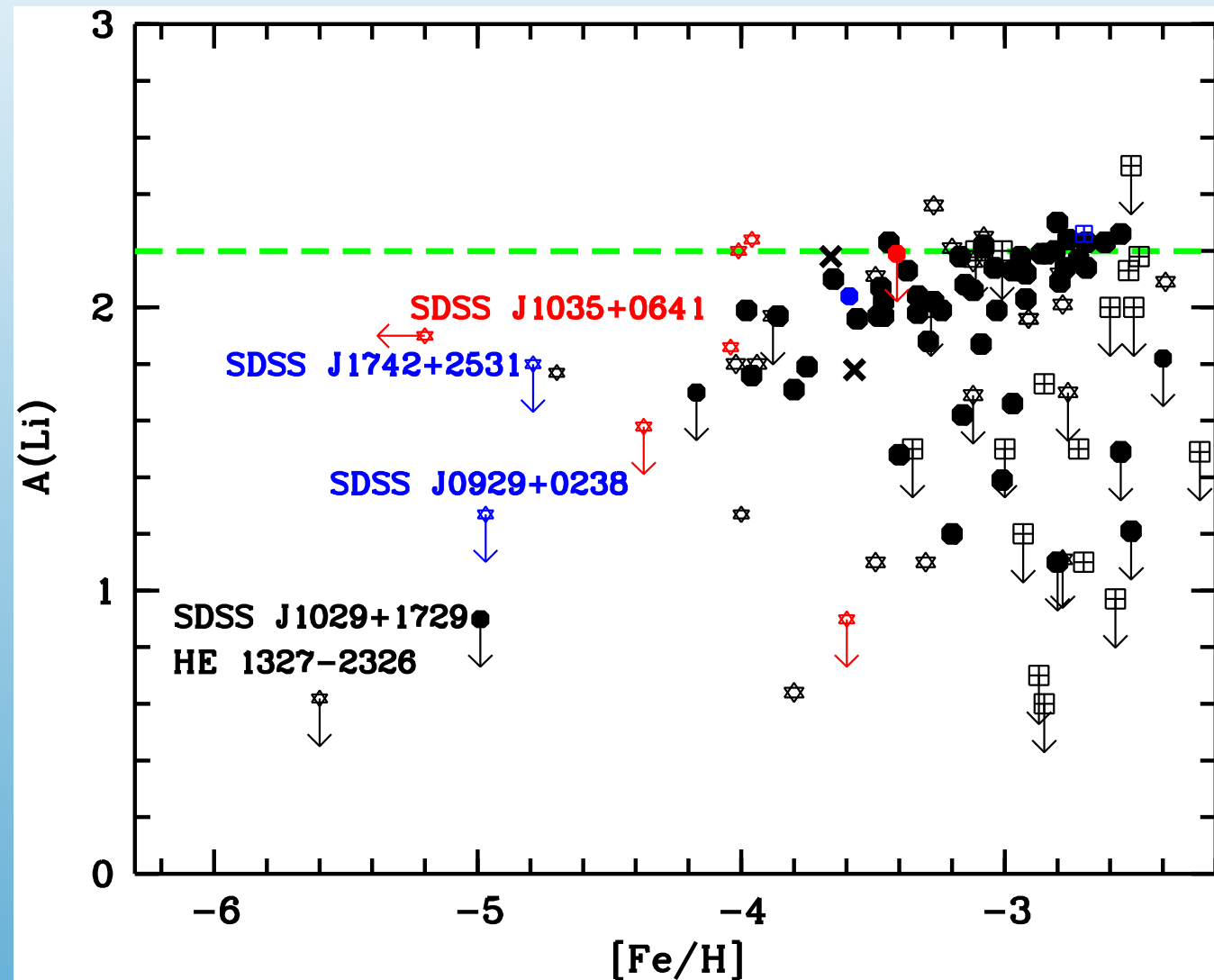
Broken Spite plateau

Note
significant
dispersion



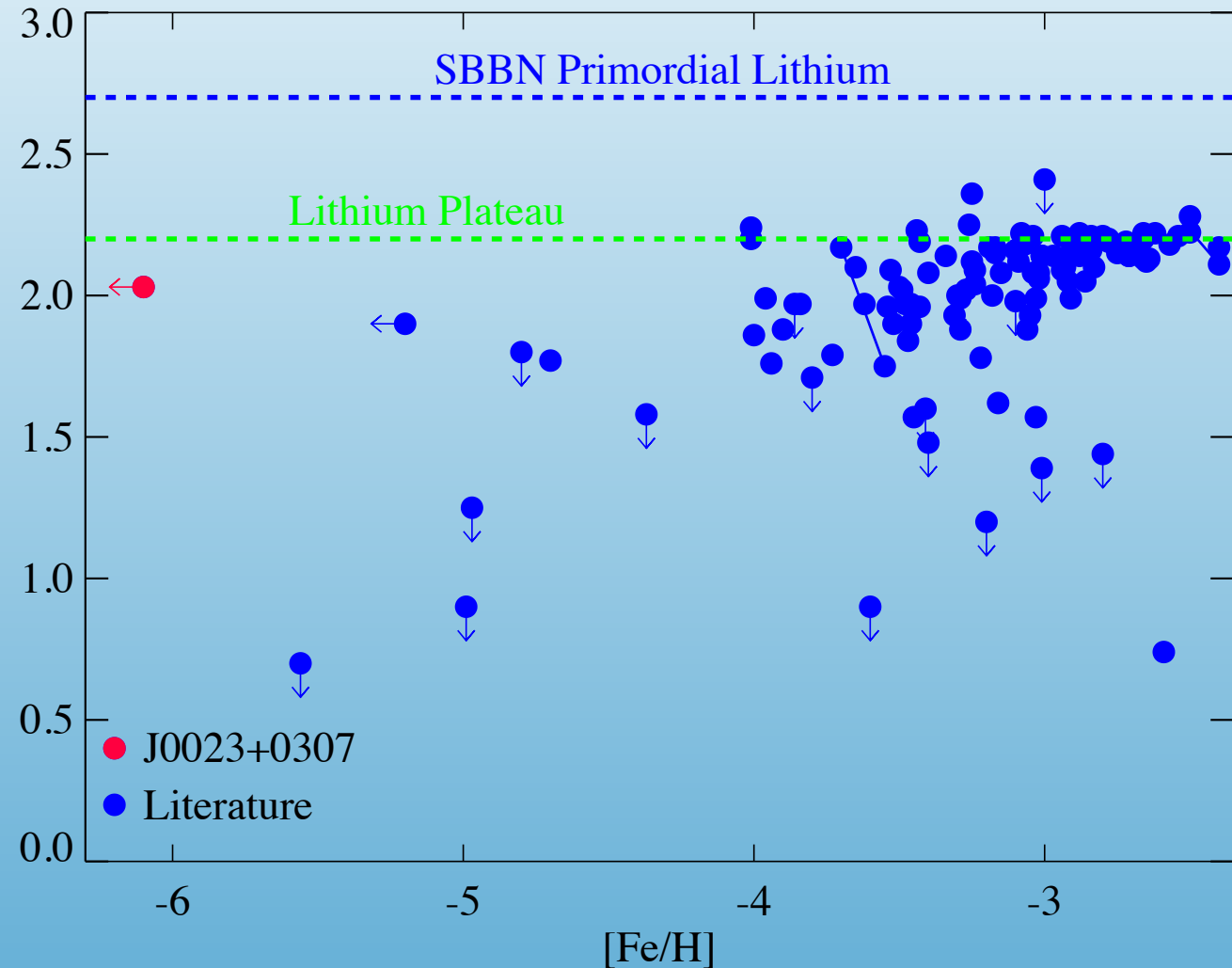
Broken Spite plateau

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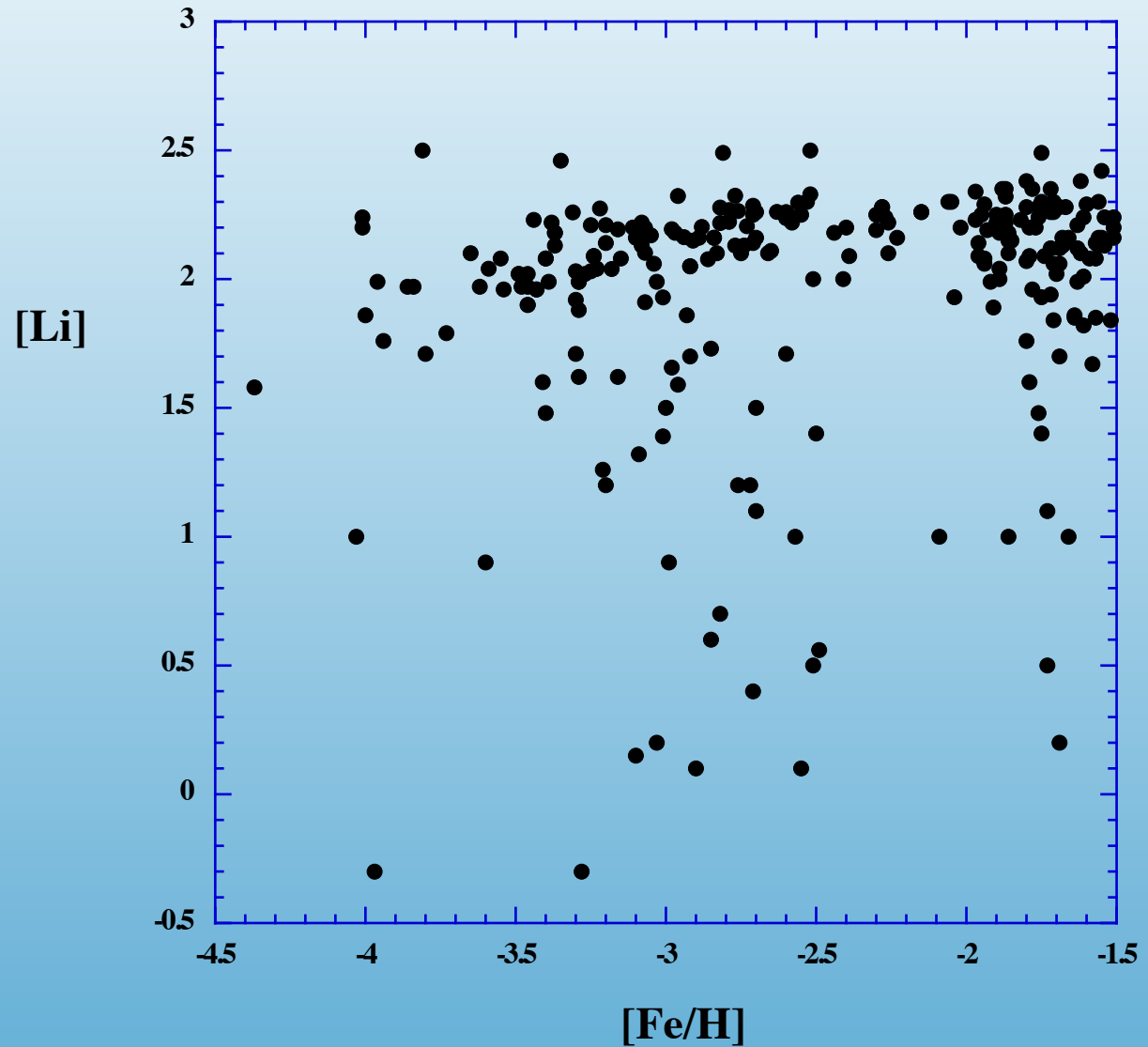
Broken Spite plateau

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Broken Spite plateau

Note
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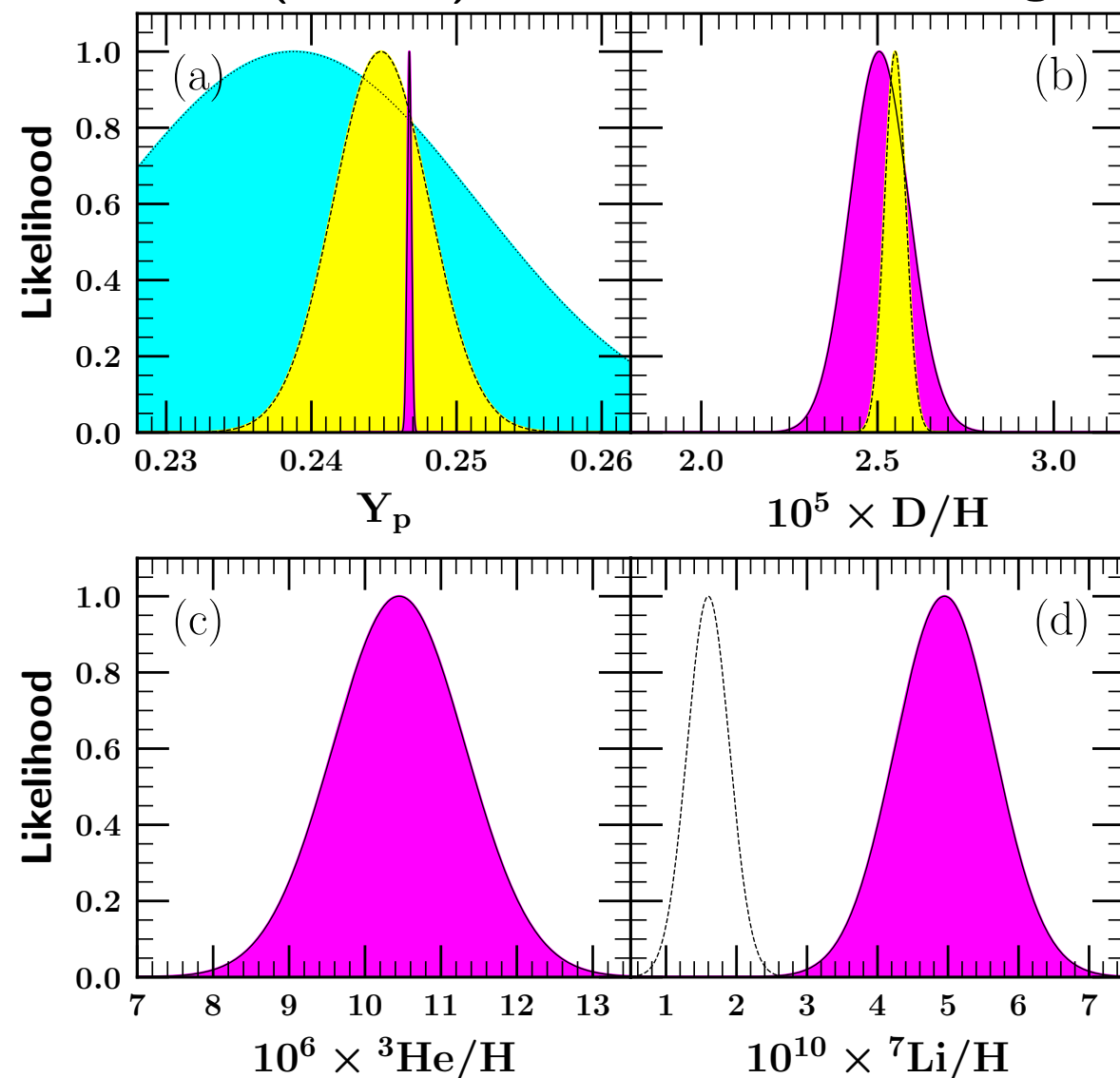


Maybe NO Li Problem

BBN and the CMB

Monte-Carlo approach combining BBN rates, observations and CMB

Planck ($N_\nu = 3$) + BBN + PDG22 average



$\mathcal{L}_{\text{OBS}}(X)$ Yellow

$$\mathcal{L}_{\text{CMB}}(Y_p) \propto \int \mathcal{L}_{\text{CMB}}(\eta, Y_p) d\eta.$$

Cyan

$$\mathcal{L}_{\text{CMB-BBN}}(X_i) \propto$$

$$\int \mathcal{L}_{\text{CMB}}(\eta, Y_p) \mathcal{L}_{\text{BBN}}(\eta; X_i) d\eta$$

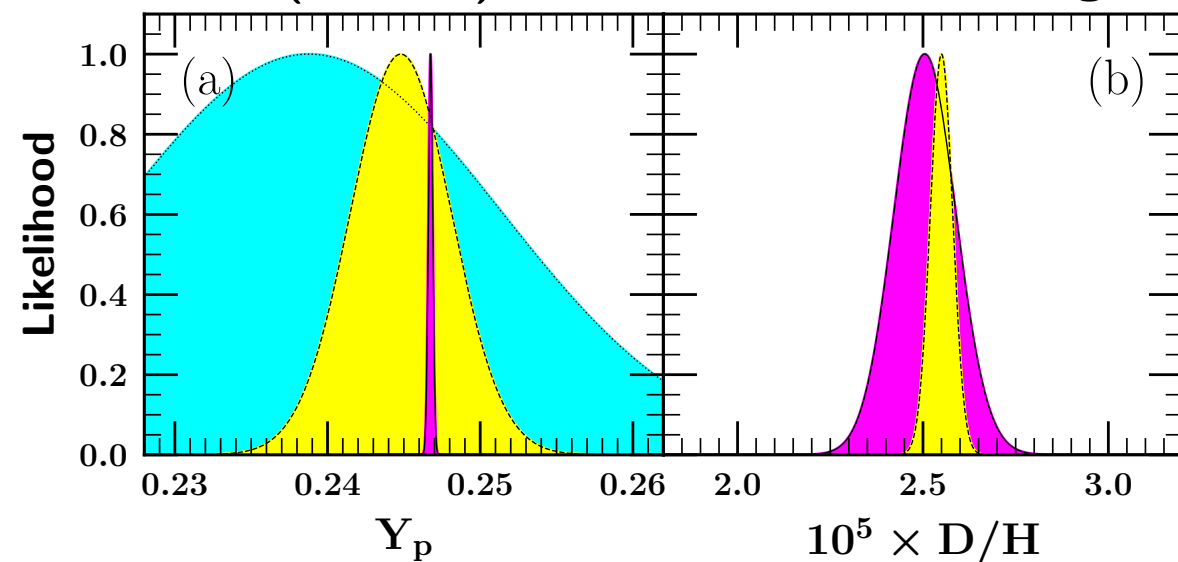
Purple

Fields, Olive, Yeh, Young

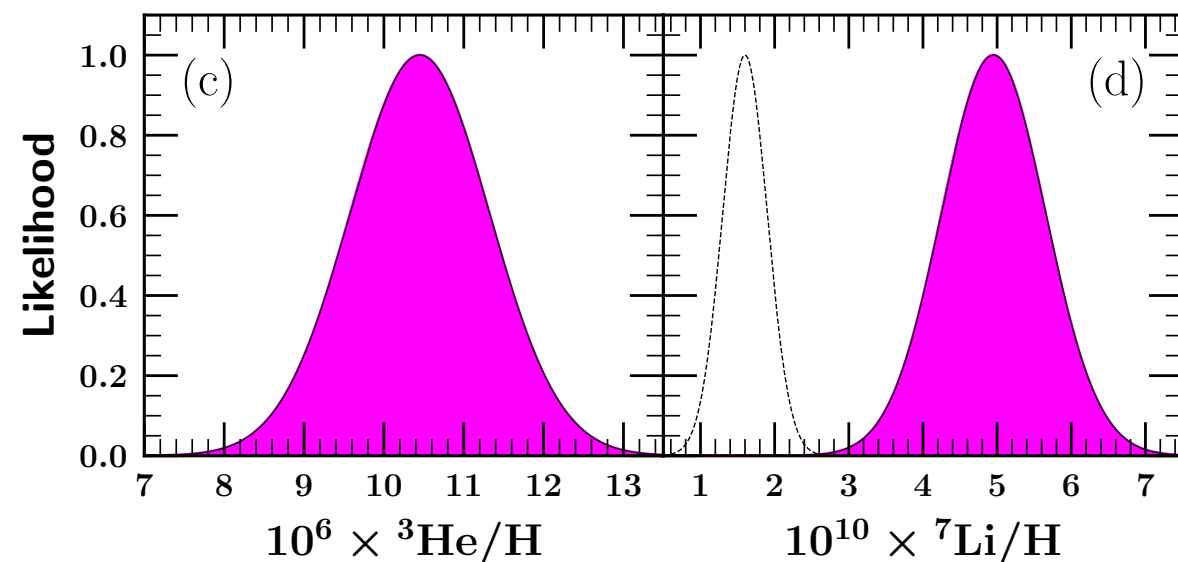
BBN and the CMB

Monte-Carlo approach combining BBN rates, observations and CMB

Planck ($N_\nu = 3$) + BBN + PDG22 average



$$\begin{aligned}
 Y_p &= 0.2467 \pm 0.0002 & (0.2467) \\
 D/H &= (2.506 \pm 0.083) \times 10^{-5} & (2.505 \times 10^{-5}) \\
 {}^3\text{He}/H &= (10.45 \pm 0.87) \times 10^{-6} & (10.45 \times 10^{-6}) \\
 {}^7\text{Li}/H &= (4.96 \pm 0.70) \times 10^{-10} & (4.95 \times 10^{-10})
 \end{aligned}$$

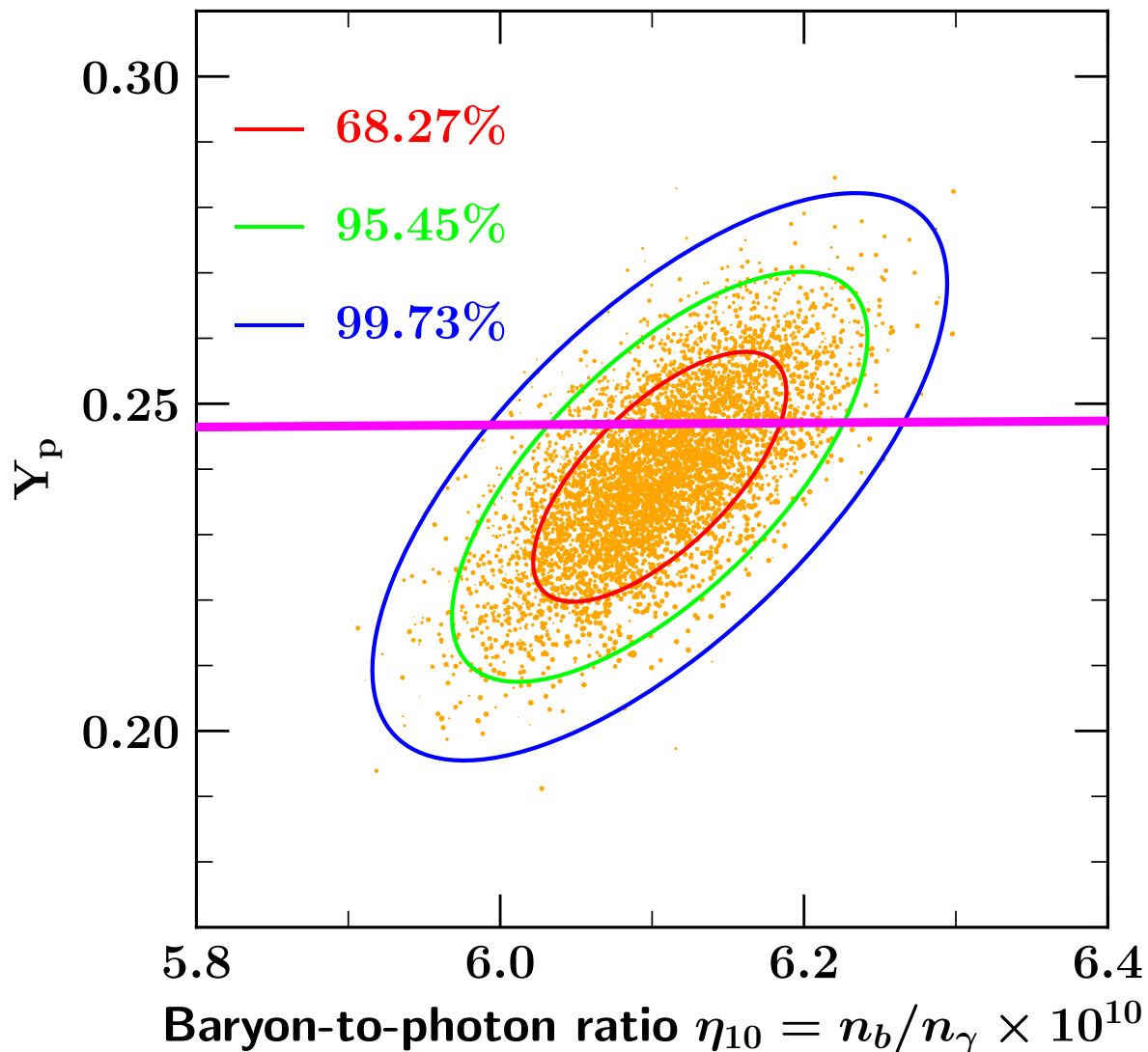


Yeh, Olive, Fields

BBN and the CMB

$$N_v = 3$$

CMB only determination
of η and Y_p



3σ BBN Prediction

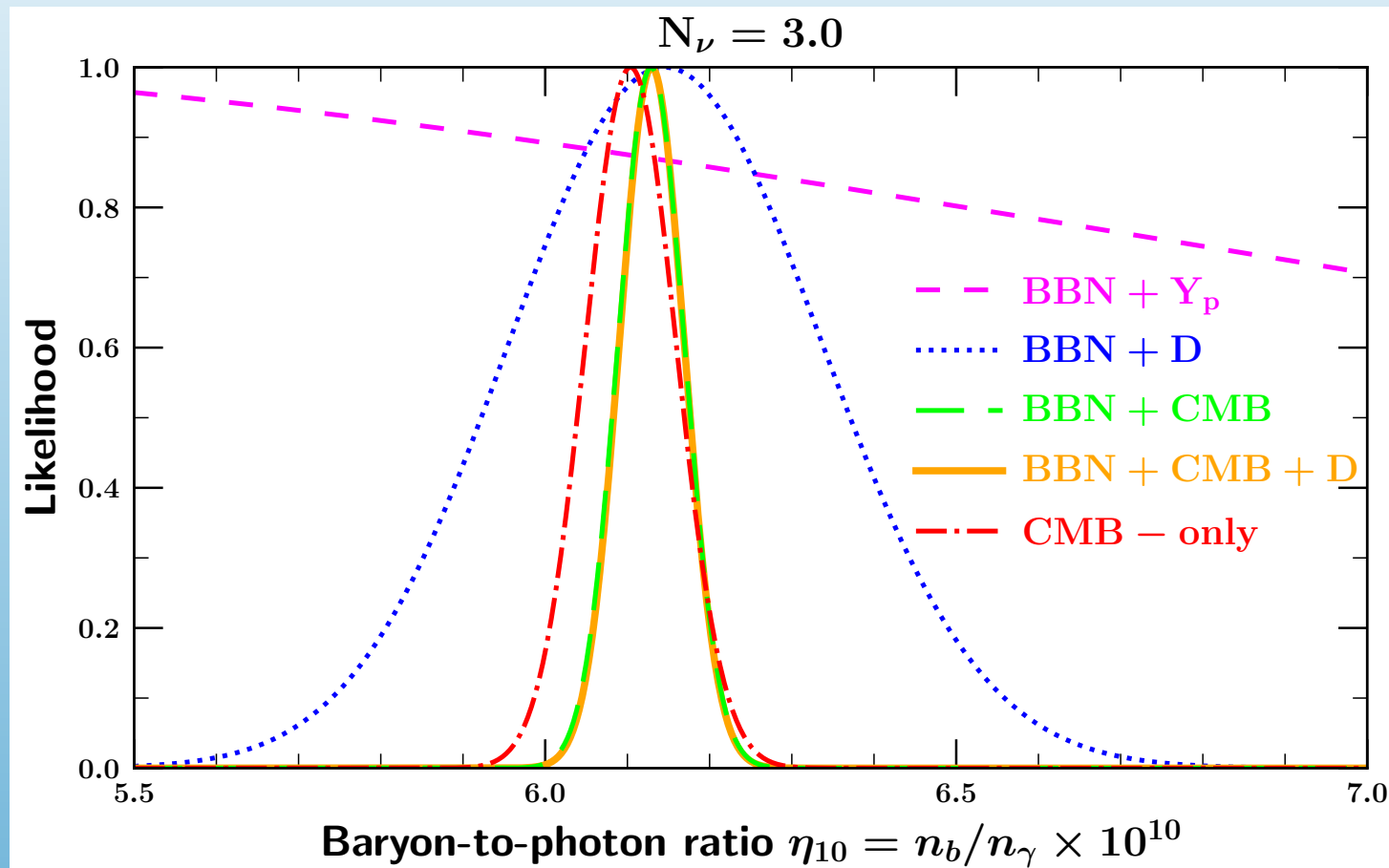
Fields, Olive, Yeh, Young

BBN and the CMB

$$\mathcal{L}_{\text{CMB}}(\eta) \propto \int \mathcal{L}_{\text{CMB}}(\eta, Y_p) dY_p.$$

$$\mathcal{L}_{\text{CMB-BBN}}(\eta) \propto \int \mathcal{L}_{\text{CMB}}(\eta, Y_p) \mathcal{L}_{\text{BBN}}(\eta; Y_p) dY_p$$

Convolved Likelihoods



Determination of η

$$\mathcal{L}_{\text{BBN-OBS}}(\eta) \propto \int \mathcal{L}_{\text{BBN}}(\eta; X_i) \mathcal{L}_{\text{OBS}}(X_i) dX_i$$

$$\mathcal{L}_{\text{CMB-BBN-OBS}}(\eta) \propto \int \mathcal{L}_{\text{CMB}}(\eta, Y_p) \mathcal{L}_{\text{BBN}}(\eta; X_i) \mathcal{L}_{\text{OBS}}(X_i) \prod_i dX_i$$

Fields, Olive, Yeh, Young

BBN and the CMB

Fields, Olive, Yeh, Young

Results for η_{10}

Constraints Used	mean η_{10}	peak η_{10}
CMB-only	6.104 ± 0.055	6.104
BBN+ Y_p	$6.741^{+1.220}_{-3.524}$	4.920
BBN+D	6.148 ± 0.191	6.145
BBN+ Y_p +D	6.143 ± 0.190	6.140
CMB+BBN	6.129 ± 0.041	6.129
CMB+BBN+ Y_p	6.128 ± 0.041	6.128
CMB+BBN+D	6.130 ± 0.040	6.129
CMB+BBN+ Y_p +D	6.129 ± 0.040	6.129

Convolved Likelihoods

$$\mathcal{L}_{\text{CMB}}(\eta) \propto \int \mathcal{L}_{\text{CMB}}(\eta, Y_p) \, dY_p.$$

$$\mathcal{L}_{\text{CMB+BBN}}(\eta) \propto \int \mathcal{L}_{\text{CMB}}(\eta, Y_p) \, \mathcal{L}_{\text{BBN}}(\eta; Y_p) \, dY_p$$

$$\mathcal{L}_{\text{BBN+OBS}}(\eta) \propto \int \mathcal{L}_{\text{BBN}}(\eta; X_i) \, \mathcal{L}_{\text{OBS}}(X_i) \, dX_i$$

$$\mathcal{L}_{\text{CMB+BBN+OBS}}(\eta) \propto \int \mathcal{L}_{\text{CMB}}(\eta, Y_p) \mathcal{L}_{\text{BBN}}(\eta; X_i) \, \mathcal{L}_{\text{OBS}}(X_i) \prod_i dX_i$$

Limits on Particle Properties

$$G_F^2 T^5 \sim \Gamma_{\text{wk}}(T_f) = H(T_f) \sim G_N^{1/2} T^2,$$

$$H^2 = \frac{8\pi}{3} G_N \rho$$

$$\rho = \frac{\pi^2}{30} \left(2 + \frac{7}{2} + \frac{7}{4} N_\nu \right) T^4,$$

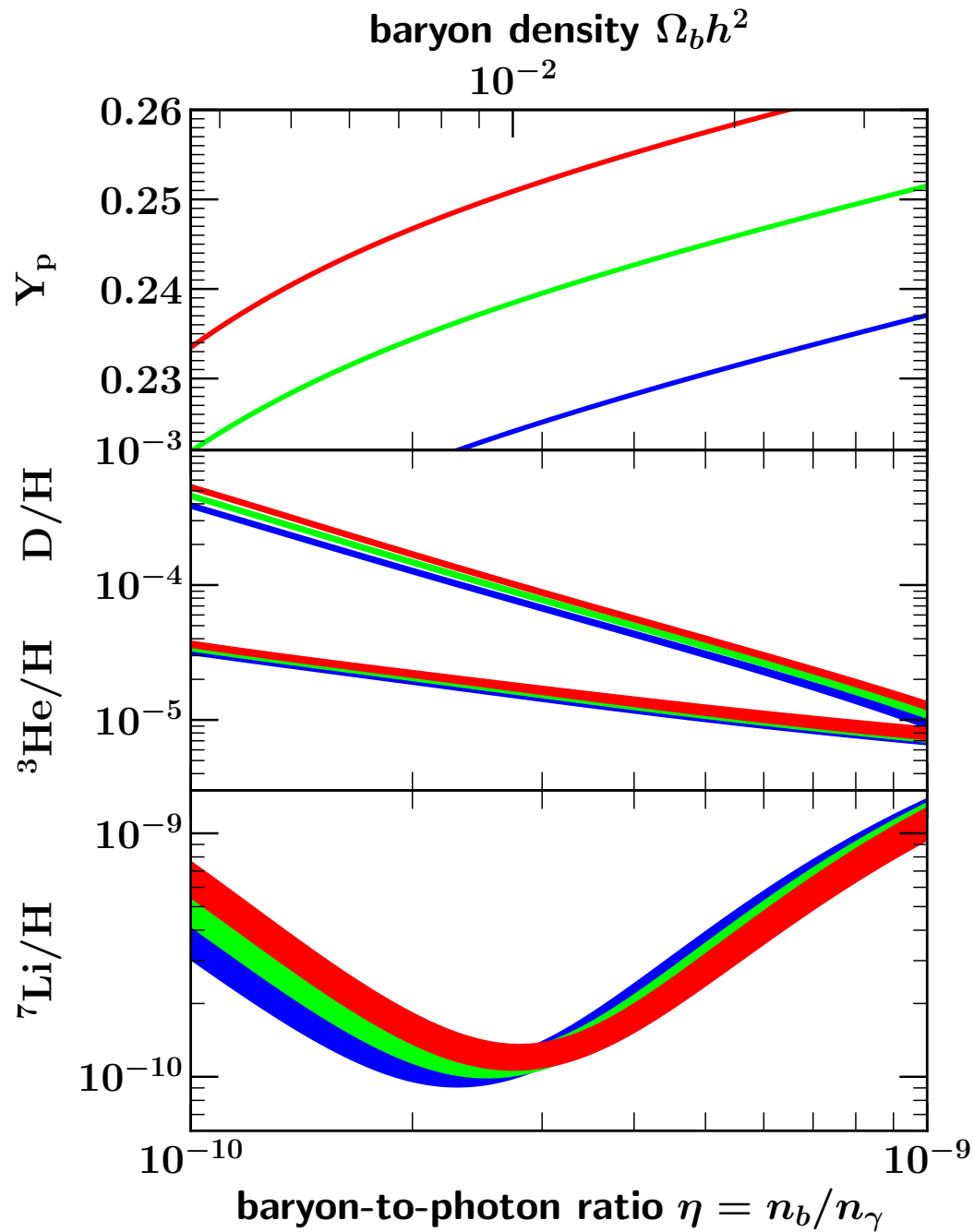
$$\frac{n}{p} \sim e^{-\Delta m/T}$$

$$Y \sim \frac{2(n/p)}{1 + (n/p)}$$

- **BBN Concordance rests on balance between interaction rates and expansion rate.**
- **Allows one to set constraints on:**
 - Particle Types
 - Particle Interactions
 - Particle Masses
 - Fundamental Parameters: G_N , G_F , α

e.g. $\frac{\Delta\alpha}{\alpha} < \text{few} \times 10^{-4}$

BBN and the CMB

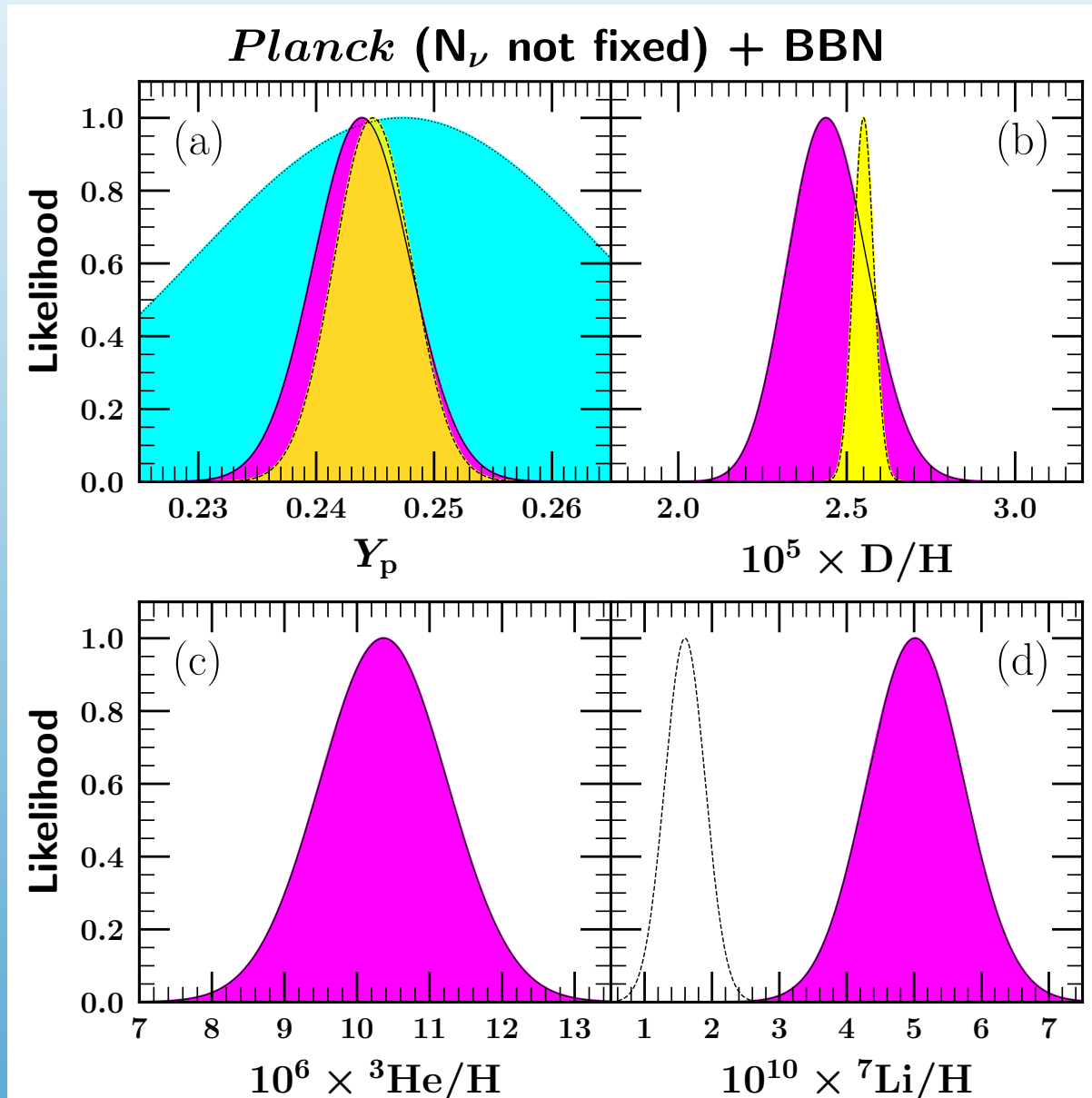


Sensitivity to N_v

Fields, Olive, Yeh, Young

BBN and the CMB

Monte-Carlo approach combining BBN rates, observations and CMB



$\mathcal{L}_{\text{OBS}}(X)$ Yellow

$$\mathcal{L}_{\text{NCMB}}(\eta) \propto \int \mathcal{L}_{\text{NCMB}}(\eta, Y_p, N_\nu) dY_p dN_\nu,$$

Cyan

$$\mathcal{L}_{\text{NCMB-NBBN}}(\eta) \propto$$

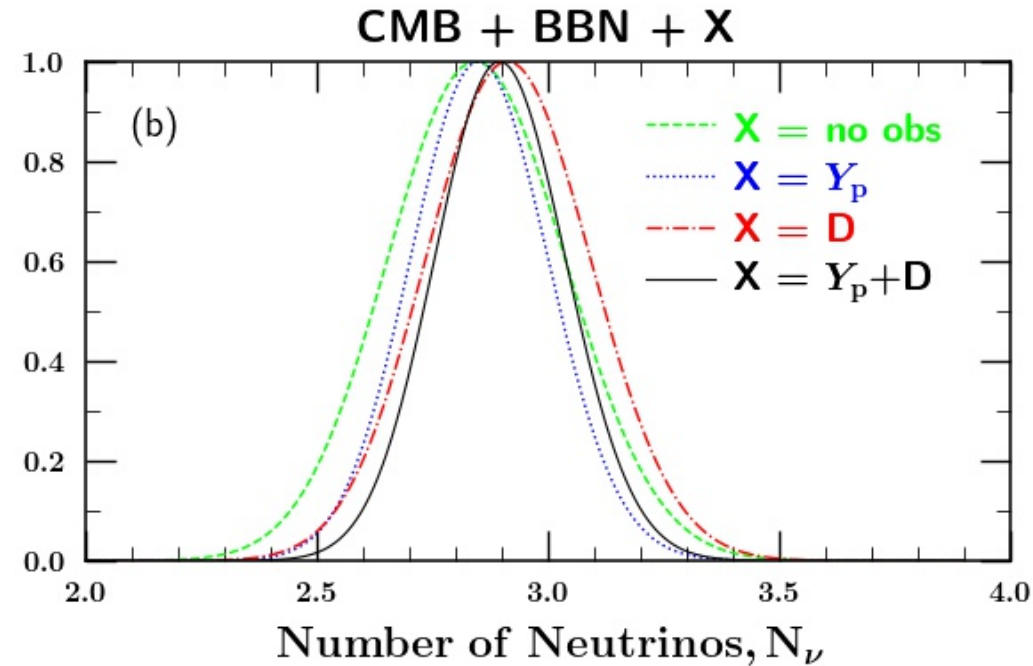
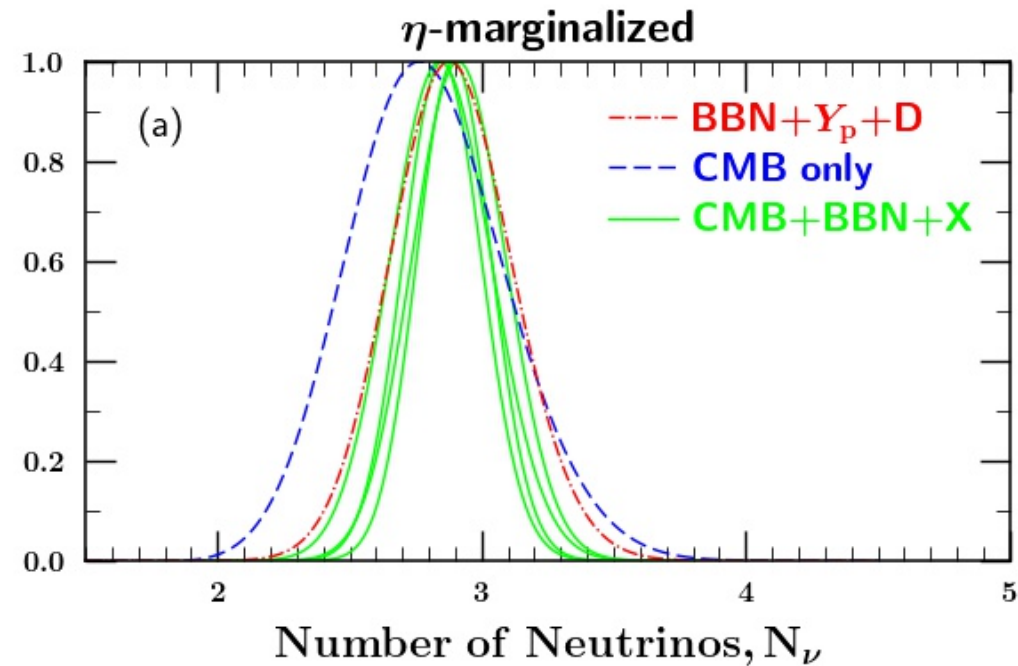
$$\int \mathcal{L}_{\text{NCMB}}(\eta, Y_p, N_\nu) \mathcal{L}_{\text{NBBN}}(\eta, N_\nu; X_i) dY_p dN_\nu,$$

Purple

Fields, Olive, Yeh, Young

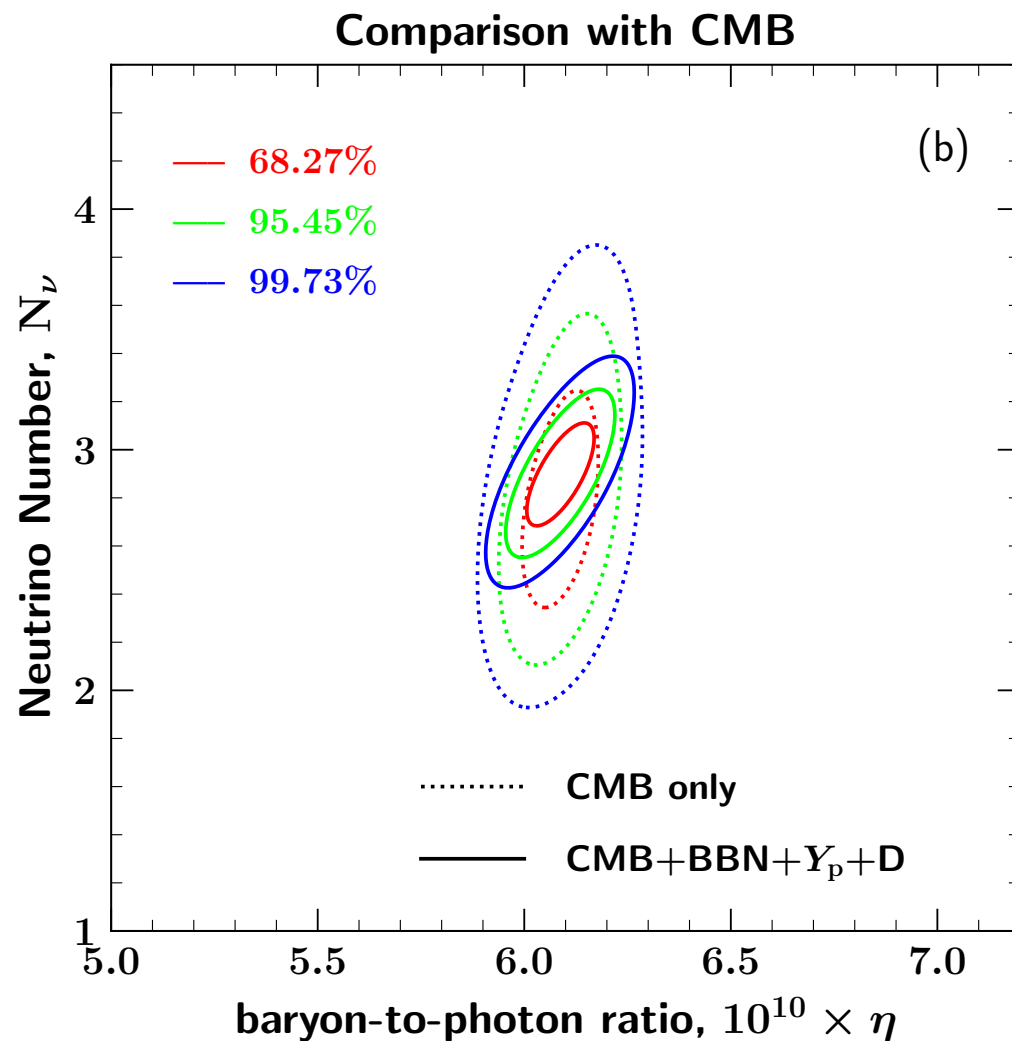
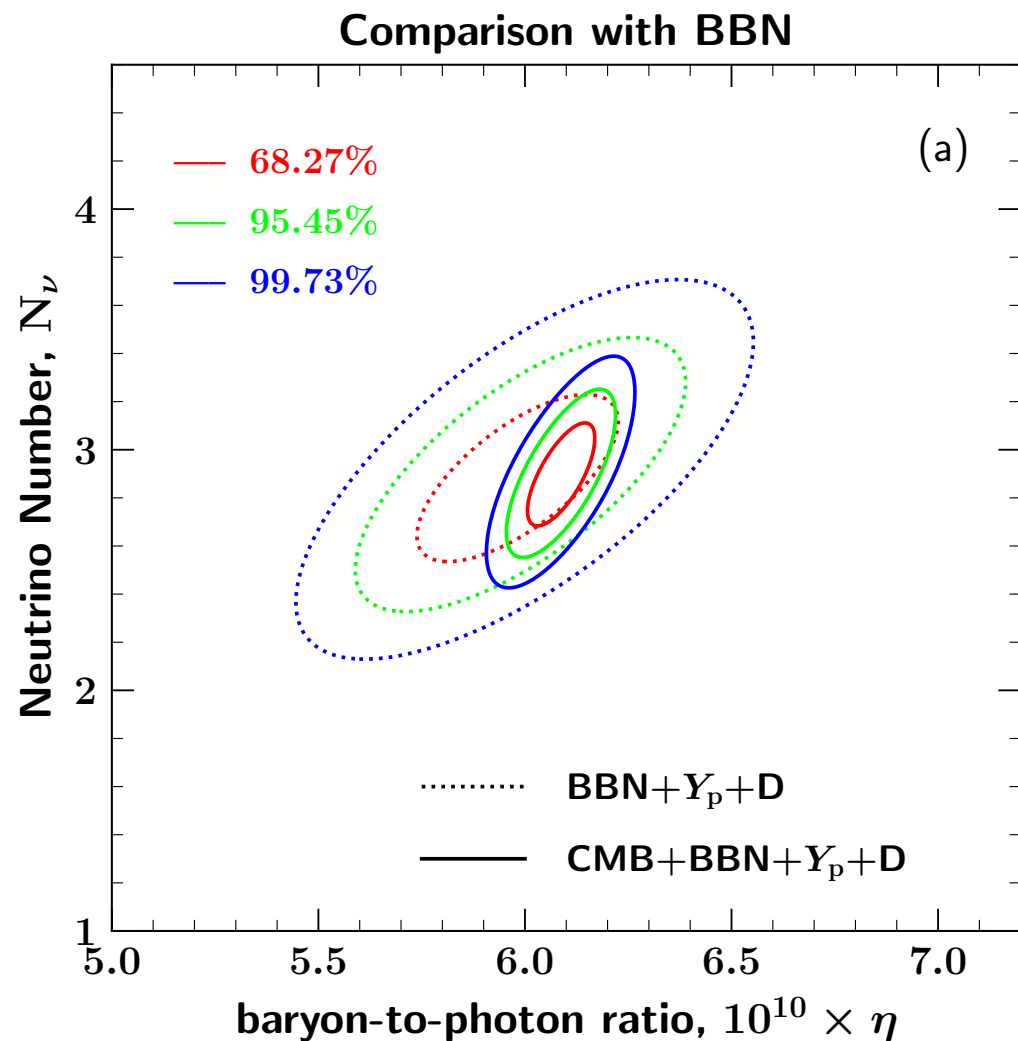
BBN and the CMB

CMB and BBN determination
of N_ν



BBN and the CMB

CMB and BBN determination
of η and N_ν



BBN and the CMB

Convolved Likelihoods

Results for η (N_ν)

Constraints Used	mean η_{10}	peak η_{10}	mean N_ν	peak N_ν	δN_ν
CMB-only	6.090 ± 0.061	$6.090^{+0.061}_{-0.062}$	2.800 ± 0.294	$2.764^{+0.308}_{-0.282}$	0.513
BBN+ Y_p +D	5.986 ± 0.161	$5.980^{+0.163}_{-0.159}$	2.889 ± 0.229	$2.878^{+0.232}_{-0.226}$	0.407
CMB+BBN	6.087 ± 0.061	$6.088^{+0.061}_{-0.062}$	2.848 ± 0.190	$2.843^{+0.192}_{-0.189}$	0.296
CMB+BBN+ Y_p	6.089 ± 0.053	$6.089^{+0.054}_{-0.054}$	2.853 ± 0.148	$2.850^{+0.149}_{-0.148}$	0.221
CMB+BBN+D	6.092 ± 0.060	$6.093^{+0.061}_{-0.060}$	2.916 ± 0.176	$2.912^{+0.178}_{-0.175}$	0.303
CMB+BBN+ Y_p +D	6.088 ± 0.054	$6.088^{+0.054}_{-0.054}$	2.898 ± 0.141	$2.895^{+0.142}_{-0.141}$	0.226

Yeh, Shelton, Olive, Fields

BBN and the CMB

Convolved Likelihoods

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$N_\nu < 3.180$ (95% CL)

Yeh, Shelton, Olive, Fields

BBN and the CMB

Convolved Likelihoods

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$N_\nu < 3.180$ (95% CL)

1-sided limit assuming $N_\nu \geq 3$ $N_\nu < 3.226$ (95% CL)

Yeh, Shelton, Olive, Fields

Limits:

- Right-handed neutrinos and extra gauge boson masses
- Dark Radiation
- Stochastic Gravitational Wave Background
- Vacuum Energy - Trackers
- Primordial Magnetic Fields
- Limits on Changes in η and N_ν between BBN and CMB
- Changes in Fundamental Constants

Summary

- BBN and CMB are in excellent agreement wrt D and He
- Li: Was Problematic
 - Most certainly now due to stellar depletion
- Wish list:
 - New cross sections measurements for $D(D,p)$ and $D(D,n)$
 - New high precision measurements of He
- Standard Model ($N_v = 3$) is looking good!

Neutrino Temperature

- At $T \sim 1 \text{ MeV}$ neutrinos decouple
- At $T \sim 1/2 \text{ MeV}$ $e^+ e^-$ annihilate to photons
- Entropy of “ γ ’s” and ν ’s conserved separately
- Prior to annihilation, $T_\gamma = T_\nu = T_>$

$$s_> = \frac{4\rho_>}{3T_>} = \frac{4}{3}\left(2 + \frac{7}{2}\right)\left(\frac{\pi^2}{30}\right)T_>^3$$

- After annihilation, $T_\gamma = T_<$ but, $T_\nu = T_>$

$$s_< = \frac{4\rho_<}{3T_<} = \frac{4}{3}(2)\left(\frac{\pi^2}{30}\right)T_<^3$$

$$T_\nu = (4/11)^{1/3}T_\gamma \simeq 1.9K$$

What does $N > 3$ mean?

If limit on $\Delta N < 0.226$

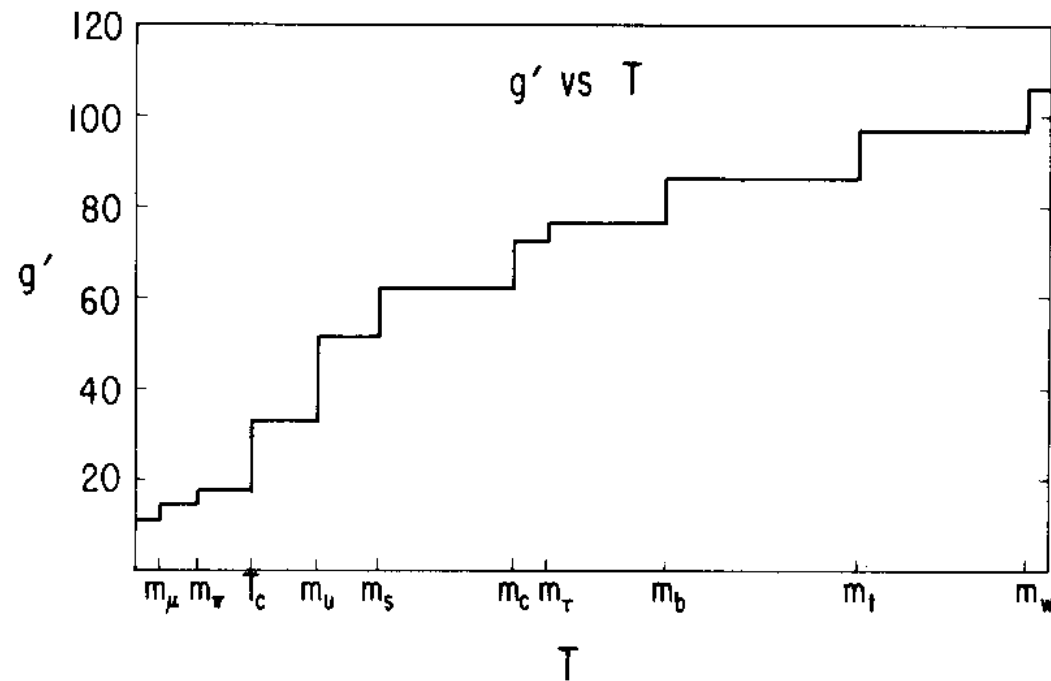
and $\Delta N_\nu = 3$

$$3 \left(\frac{T_{\Delta N}}{T_\nu} \right)^4 < .226 \Rightarrow \left(\frac{T_{\Delta N}}{T_\nu} \right)^3 < 0.14$$

$$\left(\frac{T_{\Delta N}}{T_\nu} \right)^3 = \frac{43}{4g^*}$$

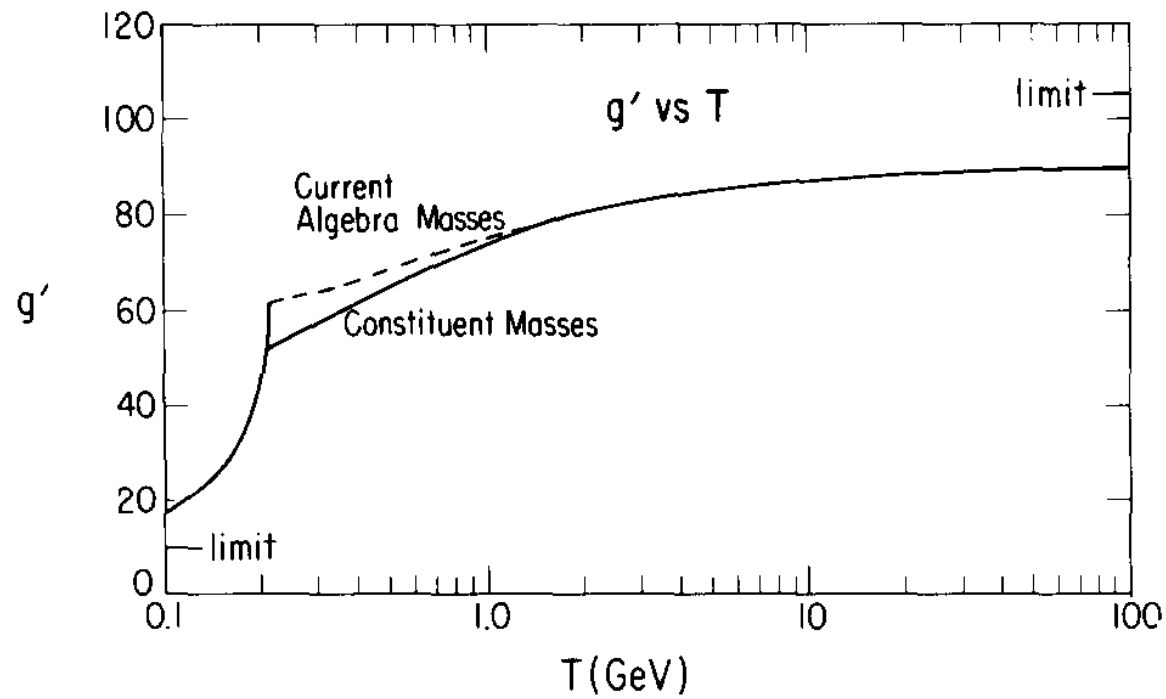
$$g^* > 75$$

What does $N > 3$ mean?

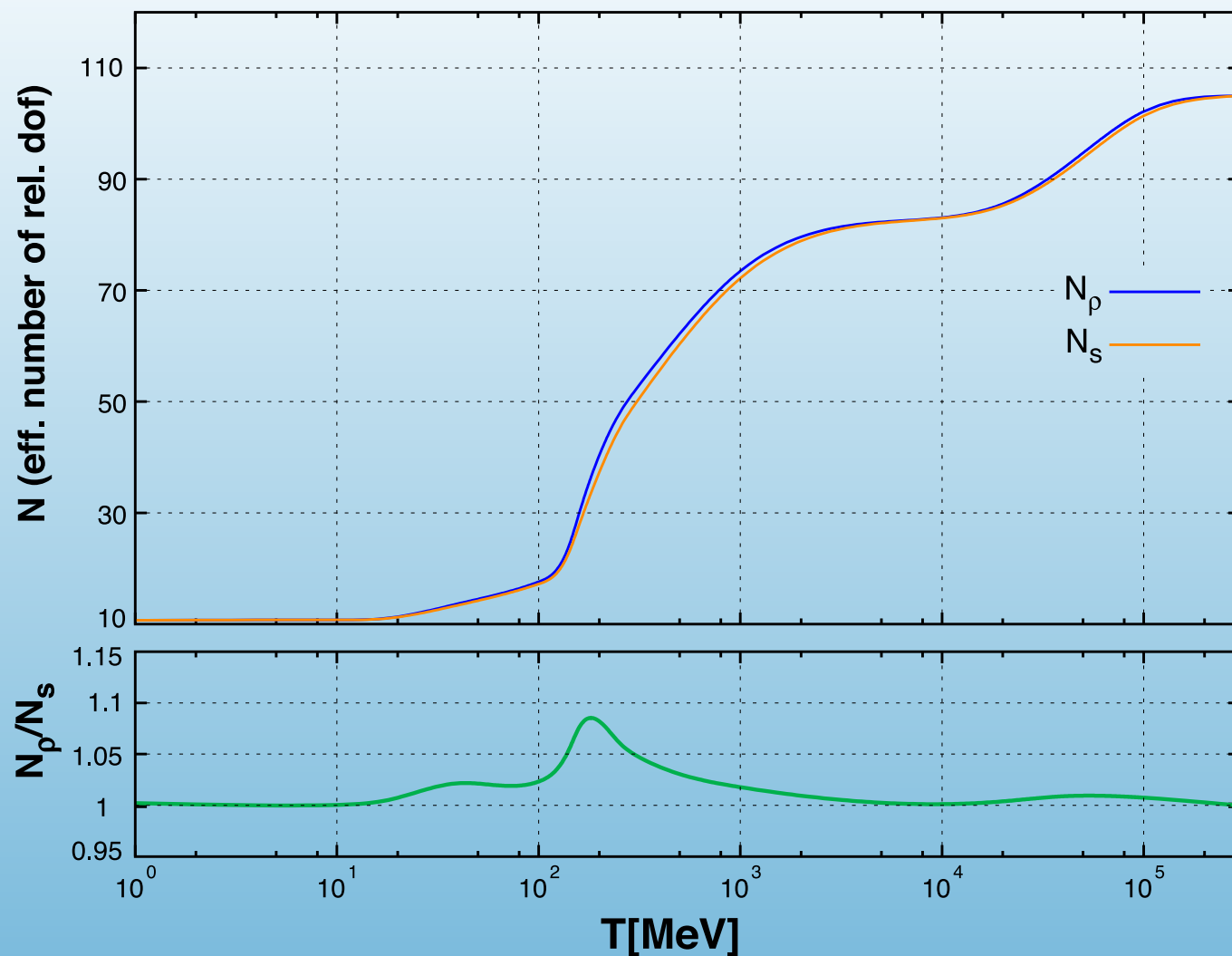


Need $T_f > m_\tau$

What does $N > 3$ mean?



What does $N > 3$ mean?



Need $T_f > 1.2$ GeV

What does $N > 3$ mean?

Today,

$$\rho_{rad} = \frac{\pi^2}{30} \left(2 + \frac{7}{4} N_\nu \left(\frac{T_\nu}{T_\gamma} \right)^4 \right) T_\gamma^4$$

$$= \frac{\pi^2}{30} \left(2 + \frac{21}{4} \left(\frac{4}{11} \right)^{4/3} + \frac{7}{4} \Delta N \left(\frac{T_{\Delta N}}{T_\gamma} \right)^4 \right) T_\gamma^4$$

Scalars: $\Delta N = 4/7$

Dirac Fermion:
 $\Delta N = 2$