



News from the strong interaction and its most difficult aspect

Why measure the pp cross section and its related challenges

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16th June, 2024



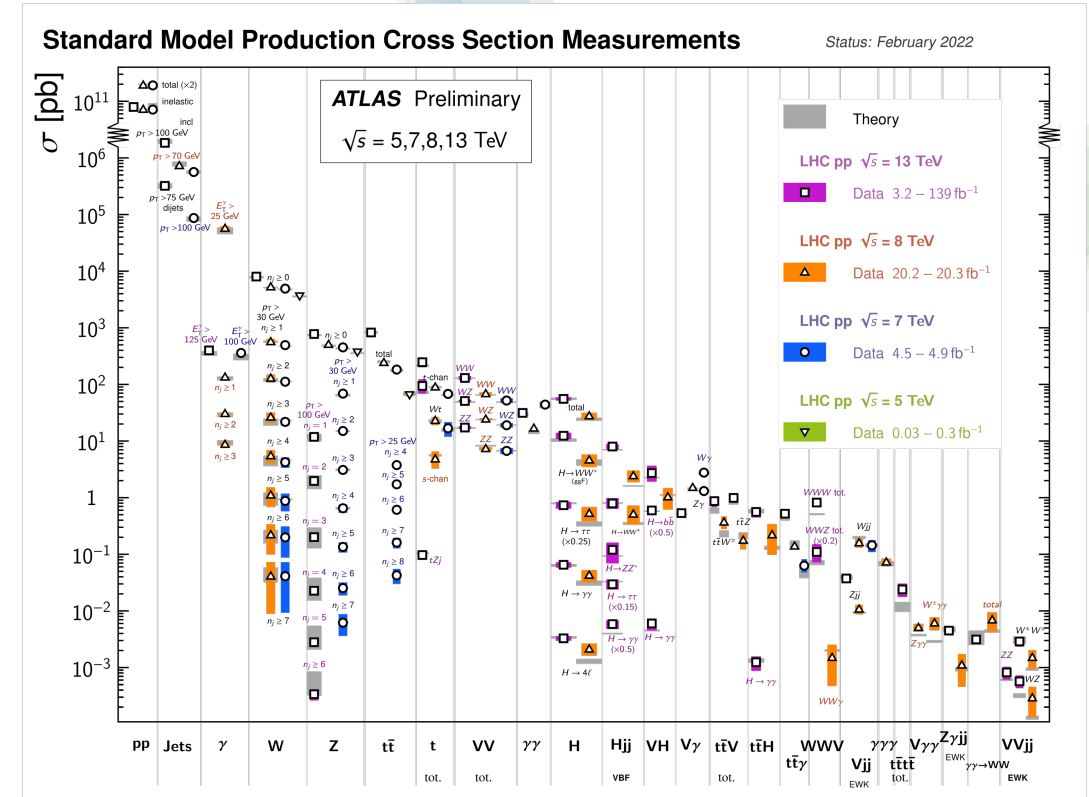
A bit of context...

Typical measurements at LHC

- SM processes (EW, QCD)
- New physics (SUSY, Exotics, DM,...)

→ All these processes account for **~60%**
of the total pp cross section...what about the rest?

- Low p_T diffractive processes (el. scattering, single/double diffractive dissociation)
- Very forward processes → need specialized detectors!



Why is forward physics important?

- ✓ Cross section not-calculable from pQCD → **experimental approach needed!**
- ✓ Crucial for **Monte Carlo simulations** especially at high pile-up
- ✓ We can have predictive power for high energy scales → cosmic ray physics and **FCC!**

Measuring σ_{TOT} and ρ

At ATLAS, we can measure σ_{TOT} via elastic scattering

Optical theorem

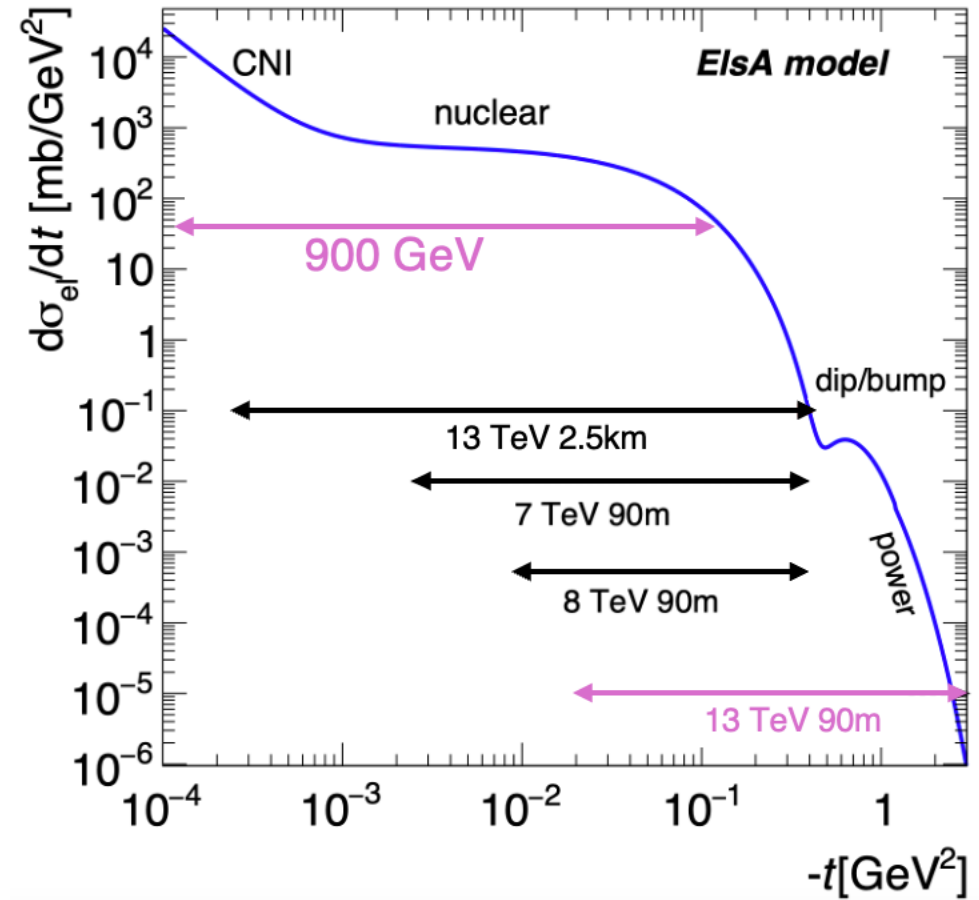
$$\sigma_{tot} = 4\pi \text{Im}[f_{el}(t \rightarrow 0)]$$

$$\sigma_{tot}^2 = \frac{16\pi(\hbar c)^2}{1+\rho^2} \left. \frac{d\sigma_{el}}{dt} \right|_{t \rightarrow 0} \quad \text{and} \quad \rho = \frac{\text{Re}[f_{el}(t)]}{\text{Im}[f_{el}(t)]} \Big|_{t \rightarrow 0}$$

- Measure the differential elastic cross section → get ρ and σ_{TOT}
- Different beam conditions and \sqrt{s} values allow to investigate different regions of the σ_{el} spectrum

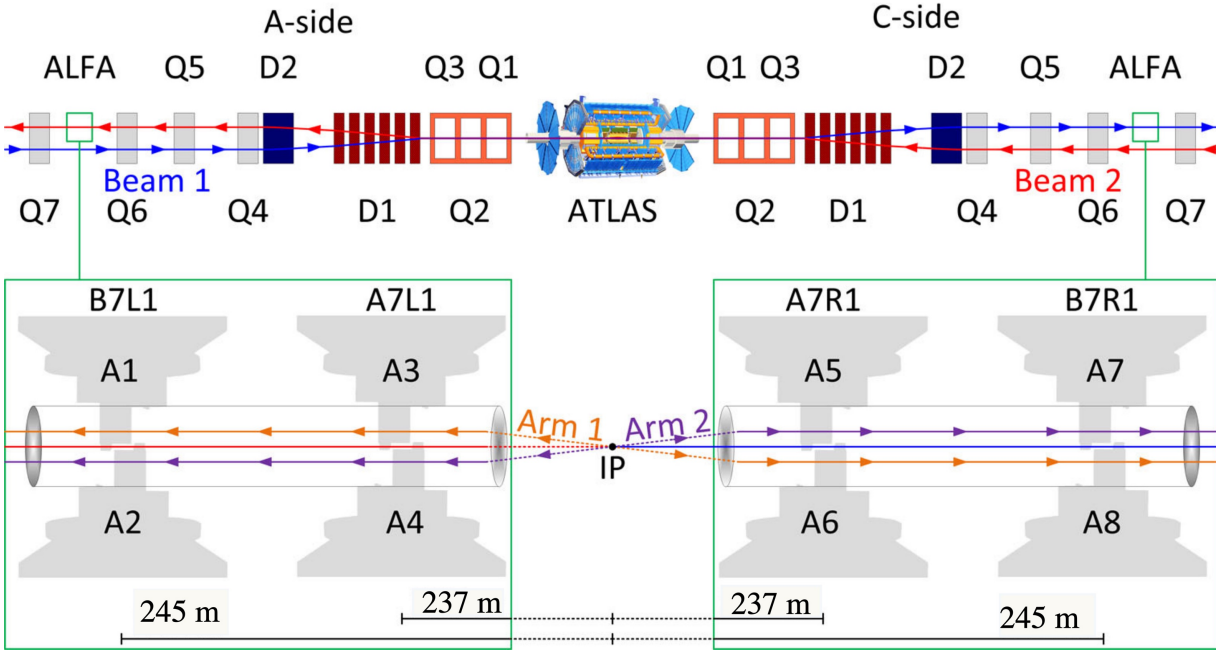
Who performs these measurements?

- ALFA** → designed to measure small-angle proton scattering
- LUCID** + Inner Detector → provide luminosity to normalize σ_{el}



Already 3 measurements published and **2 more** are ongoing!

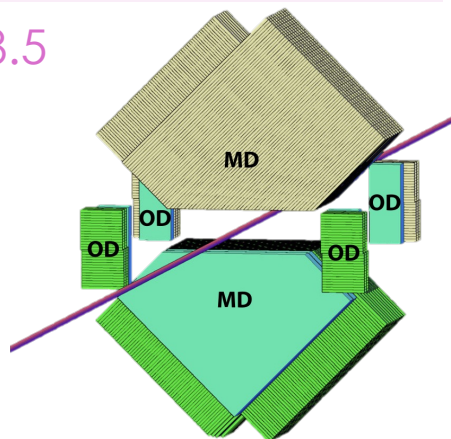
ALFA



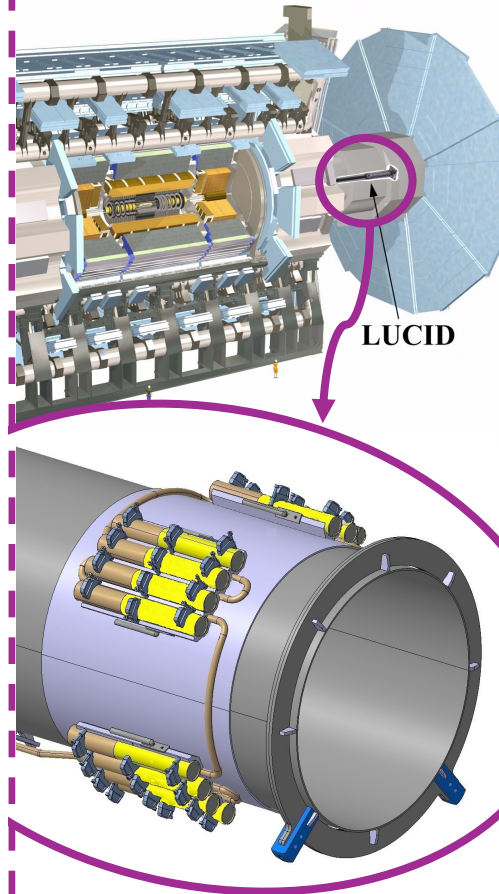
Two tracking stations in vertical Roman Pots

→ detection of protons at $|\eta| > 8.5$

layers of staggered scintillating fibers



LUCID



16 PMTs for each side of ATLAS (A and C) at 17m from IP

- Measure Cherenkov light produced on PMT quartz window
- Gain monitoring system with ^{207}Bi

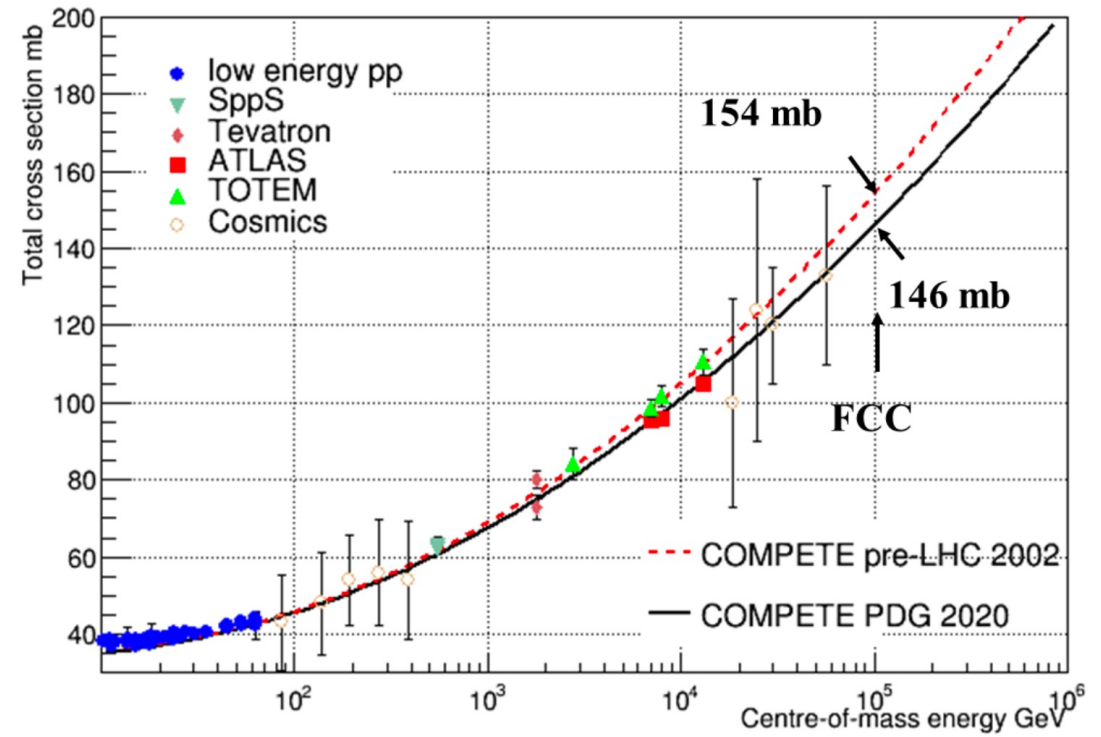
$$\mathcal{L} = \frac{\overset{\text{measured}}{\mu_{vis}} \overset{\text{machine parameters, known}}{n_b f_r}}{\underset{\text{from vdM scans}}{\sigma_{vis}}}$$

Single PMTs act as independent detectors or be combined in **global algorithms**

The total cross-section for FCC

- σ_{tot} cannot grow faster than $\ln^2(s)$ (Froissart-Martin bound)
- ρ at a given energy becomes sensitive to the energy evolution of σ_{tot} beyond that energy (given dispersion relations)

→ We can be sensitive to σ_{tot} at the FCC expected \sqrt{s} !

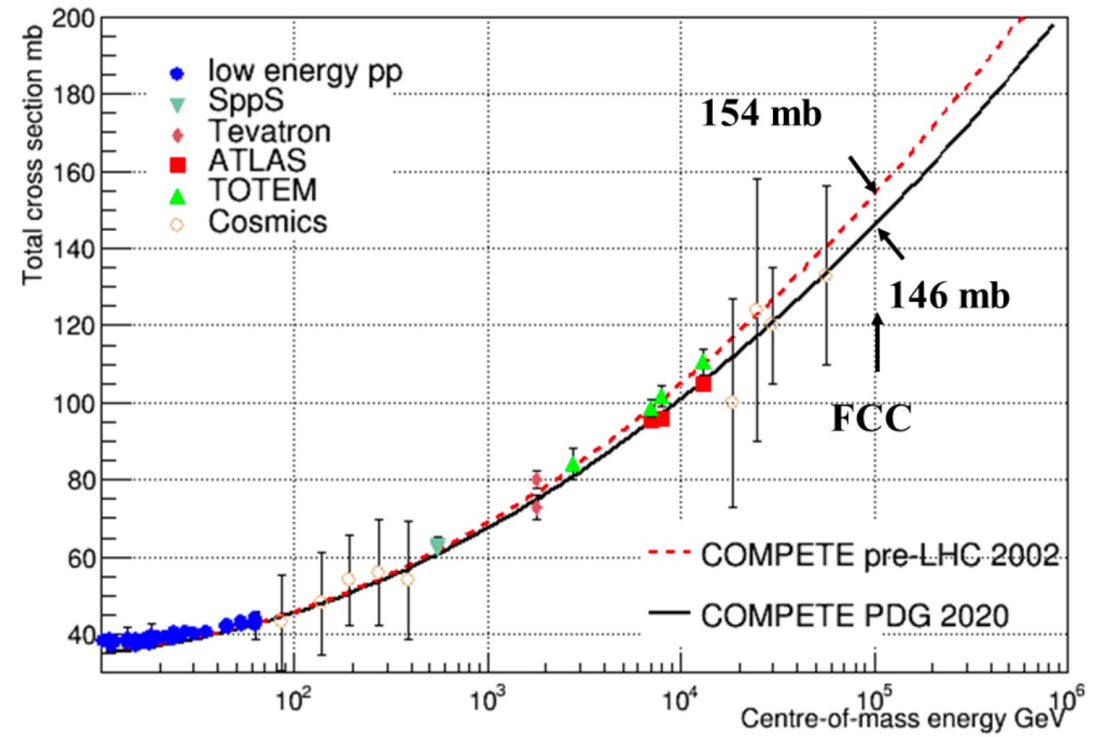


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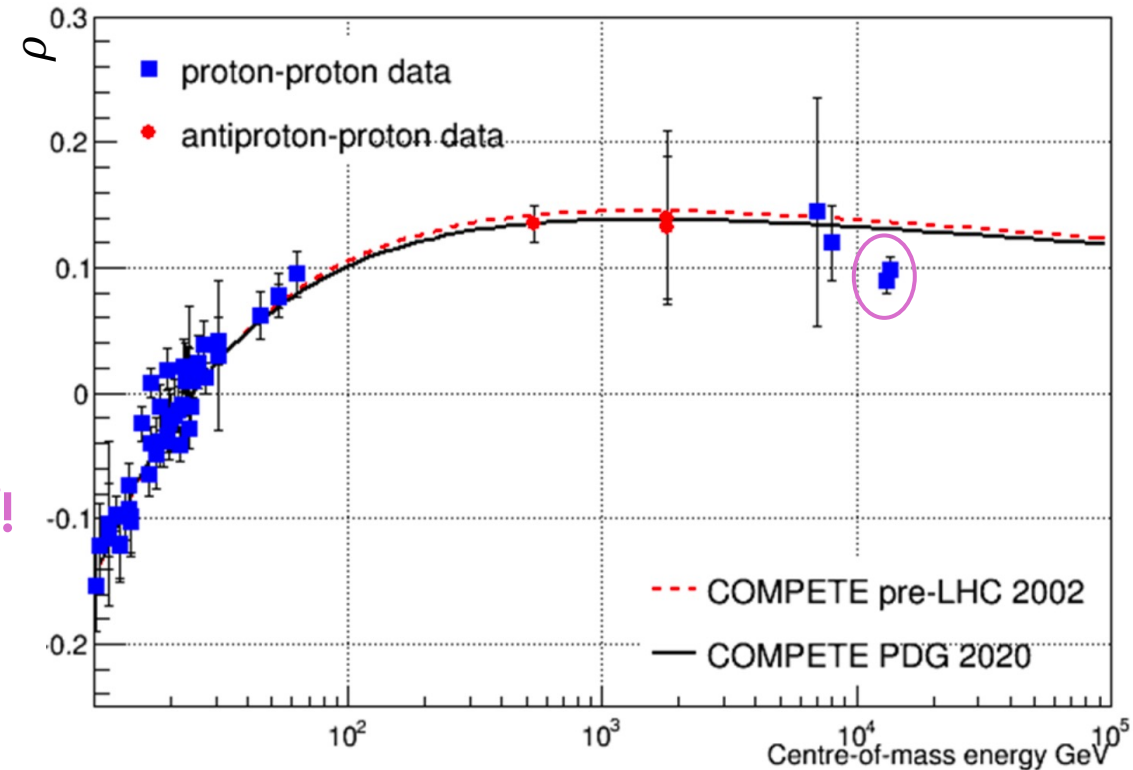
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BUT

Two recent **measurements of ρ** (by TOTEM and ATLAS) **do not agree with predictions** from dispersion relation using the $\ln^2(s)$ parametrisations



→ We need to understand what is the cause of this $\sim 3\sigma$ (!) discrepancy

Understanding the discrepancy: 900 GeV ATLAS/ALFA runs

- 1) σ_{tot} grows slower than predictions at energies beyond LHC
- 2) Possible existence of the Odderon ($CP = - -$ state of 3 gluons)

→ Considering these two scenarios σ_{tot} at FCC energies will lie in the range 130 -155 mb

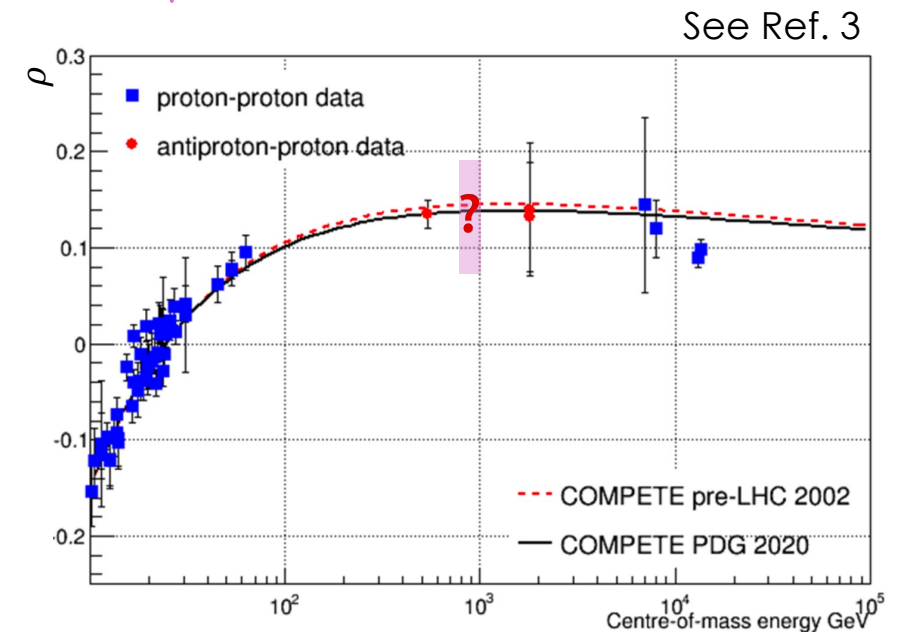
How can we discern between these two cases?

An interesting measurement can be performed by ALFA at $\sqrt{s} = 900$ GeV

If the explanation is 1) → no influence on the ρ value at $\sqrt{s} = 900$ GeV and data would then agree with prediction

If the explanation is 2) → it could affect ρ at this energy and the ρ measurement will be at tension wrt prediction

The smallest possible uncertainty on ρ and σ_{tot} is needed
→ A major – often *the* major – contribution to the systematic uncertainty has been the **luminosity uncertainty**



Luminosity measurement in ALFA runs

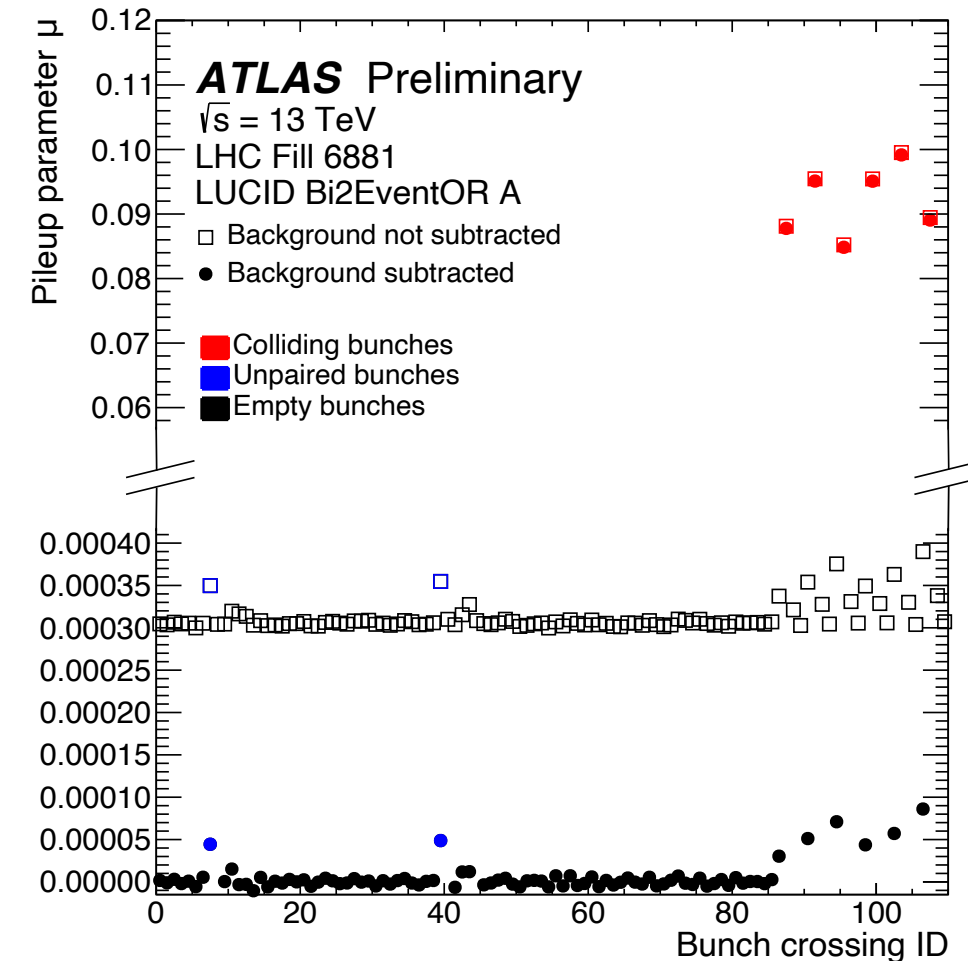
14 runs at low-luminosity and high- β^* (100m vs ~ 25 cm in usual physics runs) done in 2018 at $\sqrt{s} = 900$ GeV

Approach to luminosity measurement in ALFA runs

1. Measure the background-subtracted absolute luminosity (or μ), with various LUCID algorithms, calibrated in vdM scans
2. Compare different detectors and algorithms to account for:
 - Background subtraction uncertainty
 - Stability and algorithms compatibility

Background subtraction

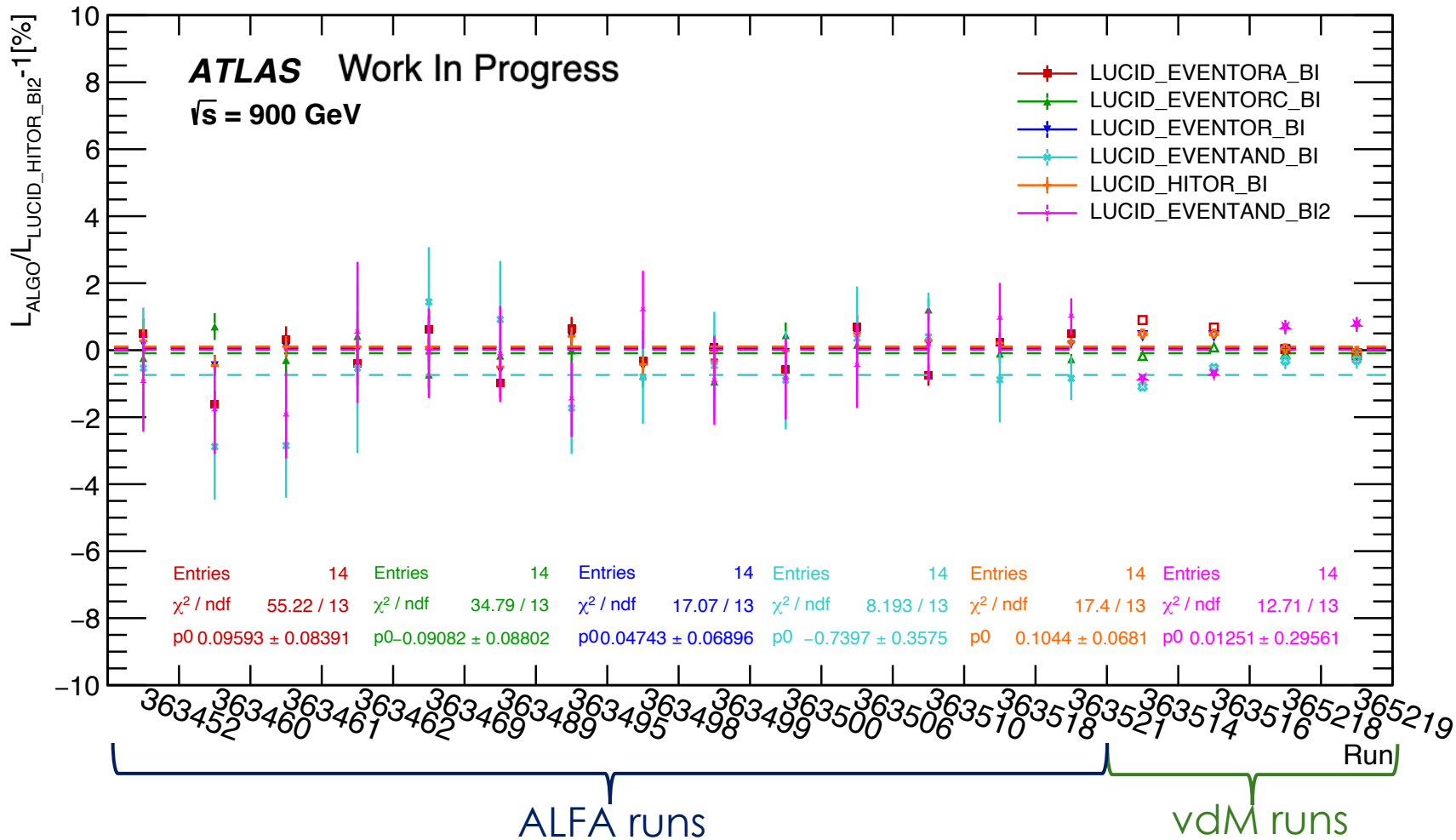
- Constant rate from ^{207}Bi activity
 - Afterglow from nuclear de-excitation after collisions
- + Single-beam (beam-gas) interactions
⇒ To be carefully evaluated using unpaired (non-colliding, filled) bunches



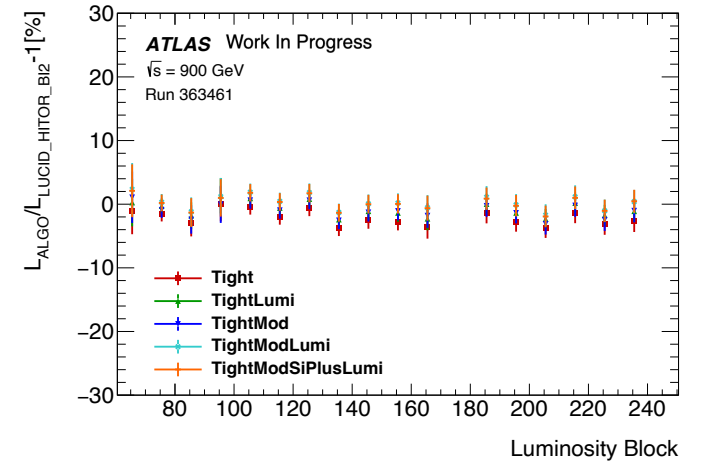
$$\mu = \mu_{vis} \sigma_{tot} / \sigma_{vis}$$

Luminosity measurement at 900 GeV

- Ad-hoc van der Meer scans were needed to provide absolute luminosity calibration → very challenging analysis
- Accurate evaluation of background, whose magnitude can compete with signal



- Relative algorithms stability is compared → input on the systematic uncertainty
- Track Counting luminosity data also considered



Luminosity measurement at 900 GeV

Difficult evaluation of the single-beam background due to the low-luminosity and different beam currents in the filled colliding vs unpaired bunches

Many methods have been tested and developed

- Observe the data looking for clear indications of beam-gas bkg
- Use the nominally empty bunches and compare them with the unpaired ones
- Use the LUCID AND algorithm: a logic AND between the two sides of LUCID allows to cut down on background and obtain a background free algorithm

RESULTS (WORK IN PROGRESS!)

Integrated luminosity and its statistical uncertainty $\mathcal{L} = 1437.58 \pm 0.65_{stat} \mu b^{-1}$

Systematic uncertainty →

Source	Sys. Uncertainty (%)
Stability (LUCID EVENTAND BI)	1.50
vdM Calibration	1.85
Beam Gas	0.74
TOTAL	2.49

WORK IN PROGRESS!

Conclusion

- σ_{tot} is a pivotal parameter for hadron colliders
- There are **open questions regarding σ_{tot} evolution**, which can result from new physics

ATLAS and ALFA have an ongoing **measurement at $\sqrt{s} = 900$ GeV** in order to constrain σ_{tot} and ρ evolution \rightarrow their measurement aims to **discern between two alternative explanations of the disagreement of the ρ measurement** of TOTEM and ATLAS at 13 TeV wrt the expected evolution

The luminosity uncertainty could be the determining factor of this measurement's discriminating power \rightarrow precise estimate required

- **Very challenging beam-conditions affect the luminosity uncertainty evaluation** \rightarrow in-depth beam gas study was required and the use of less-used LUCID algorithms
- Currently the **luminosity measurement is waiting for approval** and the final uncertainty is expected to be of the order of 2.5% total luminosity uncertainty

STAY TUNED! 😊

REFERENCES

1. Marcel Froissart. Asymptotic behavior and subtractions in the mandelstam representation. Phys. Rev., 123:1053–1057, 1961.
2. Andre Martin. Extension of the axiomatic analyticity domain of scattering amplitudes by unitarity-i. Il Nuovo Cimento A (1965-1970), 42(4):930–953, 1966.
3. P. Grafstrom, The total cross section for proton-proton interactions at the FCC, arXiv:2306.15449v1 [hep-ph] 27 Jun 2023
4. ATLAS Collaboration, Luminosity determination in pp collisions at $\sqrt{s} = 13$ TeV using the ATLAS detector at the LHC, (2022), arXiv: 2212.09379
5. ATLAS Collaboration, Measurement of the total cross section from elastic scattering in pp collisions at $\sqrt{s} = 7$ TeV with the ATLAS detector, Nucl. Phys. B 889 (2014) 486
6. ATLAS Collaboration, Measurement of the total cross section from elastic scattering in pp collisions at $\sqrt{s} = 8$ TeV with the ATLAS detector, Phys. Lett. B 761 (2016) 158
7. ATLAS Collaboration, Measurement of the total cross section and ρ -parameter from elastic scattering in pp collisions at $\sqrt{s} = 13$ TeV with the ATLAS detector, Eur. Phys. J. C 83 (2023) 441

BACKUP

More about dispersion relations

Dispersion relations are based upon the Kramers-Kronig theorem.

Let $\chi(\omega) = \chi_1(\omega) + i \chi_2(\omega)$ be a complex analytic function of the complex variable ω where $\chi_1(\omega)$ and $\chi_2(\omega)$ are real

Then:

$$\chi_1(\omega) = \frac{1}{\pi} \mathcal{P} \int_{-\infty}^{\infty} \frac{\chi_2(\omega')}{\omega' - \omega} d\omega'$$

derivation based upon the
Cauchy integral theorem

Thus the Kramers-Kronig theorem gives a relation between the real and imaginary part of a complex analytic function.

Applied in many different field of physics

Rho measurement

When they hold ?

- 3 basic principles:

1. Analyticity (see before)
2. Crossing symmetry \longrightarrow
3. Unitarity \rightarrow from the Optical Theorem

- Very general assumptions

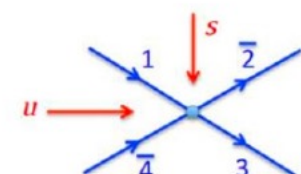
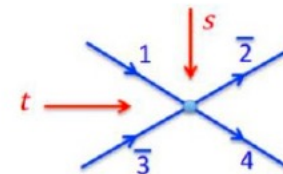
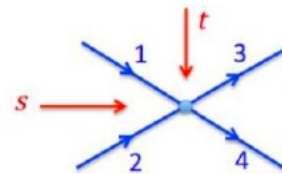
Since $T_{ik}(s, t)$ is a function of kinematical invariants (not on the sign of P_i), the same function describes the following reactions:

$$1+2 \rightarrow 3+4 \text{ for } P_1, P_2, P_3, P_4 > 0 \quad s\text{-channel } (s > 4m^2, t, u < 0)$$

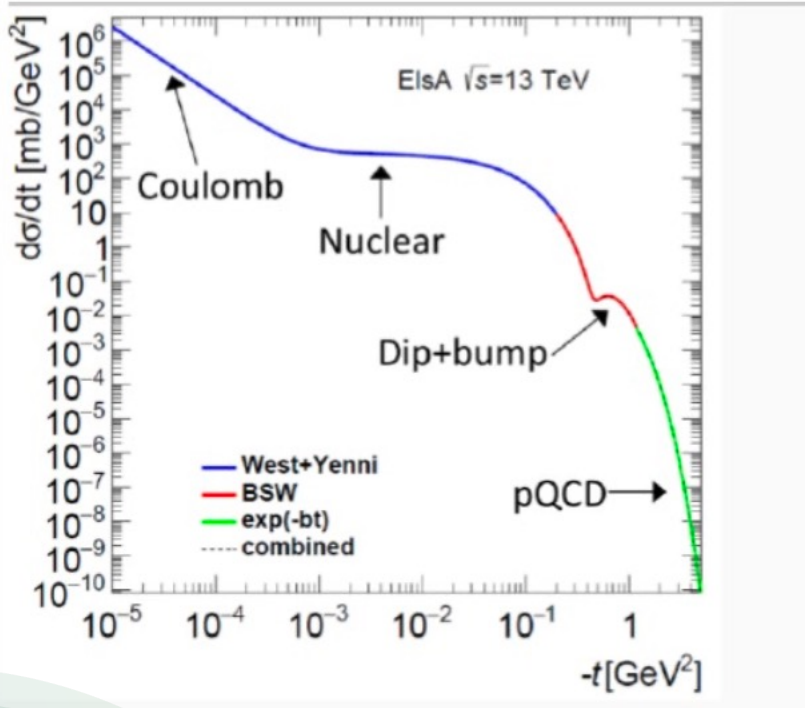
$$1+\bar{3} \rightarrow \bar{2}+4 \text{ for } P_1, P_4 > 0 \text{ and } P_2, P_3 < 0 \quad t\text{-channel } (t > 4m^2, s, u < 0)$$

$$1+\bar{4} \rightarrow \bar{2}+3 \text{ for } P_1, P_3 > 0 \text{ and } P_2, P_4 < 0 \quad u\text{-channel } (u > 4m^2, s, t < 0)$$

$$1 \rightarrow \bar{2} + 3+4 \text{ for unstable particle } (P_1, P_3, P_4 > 0 \text{ and } P_2 < 0)$$



Elastic scattering



- $p + p \longrightarrow p + p$
 - Large range depending on the transferred momentum: $t = (p\theta)^2$
 - Each t -range dominated by different processes
 - Need measurements in each t -range to access the different physics processes involved
1. The Coulomb interaction dominates at very-low t
 2. Coulomb-Nuclear interference region
 3. Pure nuclear region
 4. the dip-region
 5. pQCD region

Disp. Rel in elastic scattering

Analyticity of the elastic scattering amplitude $f_{el}(s,t)$ and **crossing symmetry** \rightarrow

$\text{Re } f_{el}(s,t)$ is related to $\text{Im } f_{el}(s,t)$ via dispersion relations

$$\text{Re } f_{+}(E) = C + \frac{E}{\pi} \int_m^{\infty} dE' \left(\frac{\text{Im } f_{+}(E')}{E'(E'-E)} - \frac{\text{Im } f_{-}(E')}{E'(E'+E)} \right)$$

Note: this relation is valid IF crossing symmetry holds. This implies that pp and pbar-p cross sections are the same asymptotically. If there is Odderon exchange this is no more True (Odderon is CP=--)

where C is real constant and + refers to proton-proton amplitude and - to anti proton-proton amplitude

Unitarity \rightarrow the optical theorem : $\sigma_{\text{tot}} = 4\pi/p \text{ Im } f_{el}(0)$

$$\text{Re } f_{+}(E) = C + \frac{E}{4\pi^2} \int_m^{\infty} dE' p' \left(\frac{\sigma_{+}(E')}{E'(E'-E)} - \frac{\sigma_{-}(E')}{E'(E'+E)} \right)$$

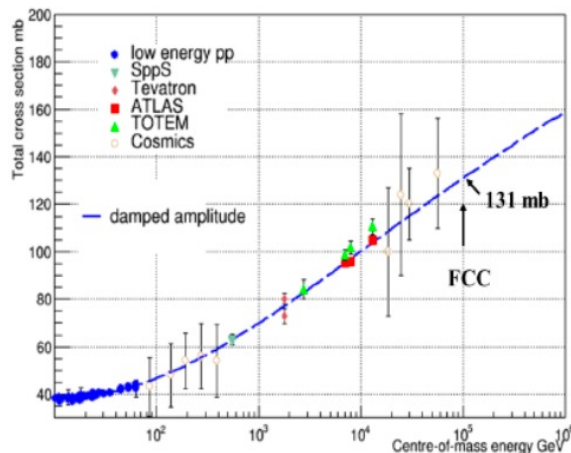
$$\rho_{\pm} \sigma_{\pm} = \frac{B}{p} + \frac{E}{\pi p} P \int_m^{\infty} \left[\frac{\sigma_{\pm}}{E'(E'-E)} - \frac{\sigma_{\mp}}{E'(E'+E)} \right] p' dE'$$

where σ_{+} is the proton-proton total cross section and σ_{-} the anti-proton proton total cross section

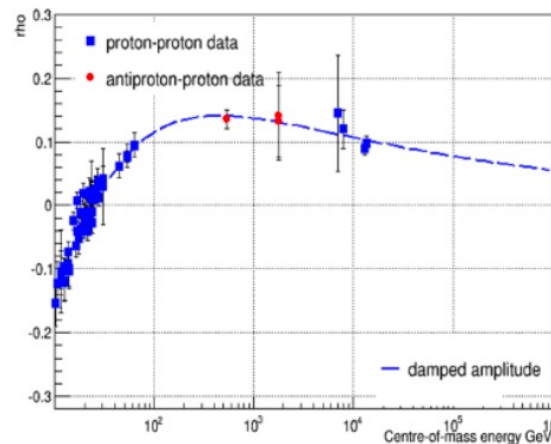
$$\rho = \text{Re } f_{el}(s,t=0) / \text{Im } f_{el}(s,t=0)$$

Predictions at FCC: slowing of sigmaTOT

$$\frac{\ln^2(s)}{1 + \alpha \ln^2(s)}$$



(a) σ_{tot}

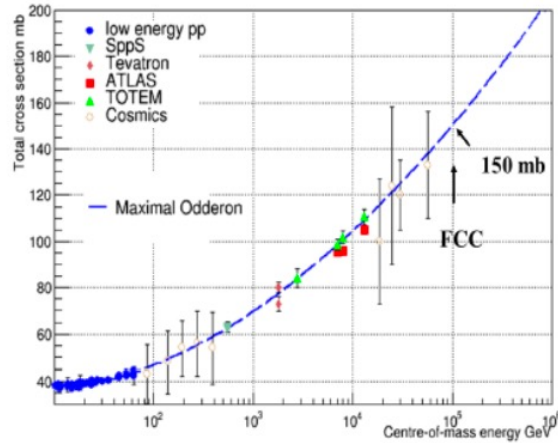


(b) ρ

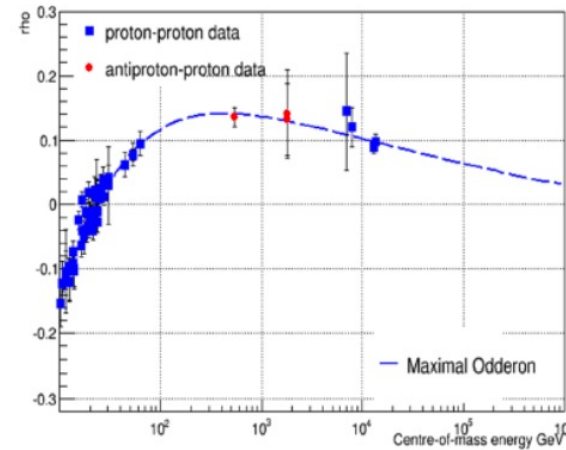
Per Grafstrom
[arXiv:2306.15449](https://arxiv.org/abs/2306.15449)
 [hep-ph]

- α included in the fit $\rightarrow \alpha = 0.0016$
- Good fit of σ_{TOT} and ρ TOTEM and ATLAS data at 13 TeV
- σ_{TOT} flattens out at very high energy (original purpose of the proposed parametrization)
- σ_{TOT} at FCC energy (100 TeV) about 130 mb

Predictions at FCC: odderon



(a) σ_{tot}



(b) ρ

Per Grafstrom

[arXiv:2306.15449](https://arxiv.org/abs/2306.15449)

[hep-ph]

- Use of Maximal Odderon parametrization (see reference)
- Fit to TOTEM data of σ_{TOT} but discarded ATLAS data
- FCC predicted $\sigma_{TOT} = 150$ mb

Analysis di ALFA

differential elastic cross section

$$\frac{d\sigma}{dt} = \frac{1}{16\pi} \left| f_N(t) + f_C(t)e^{i\alpha\phi(t)} \right|^2$$

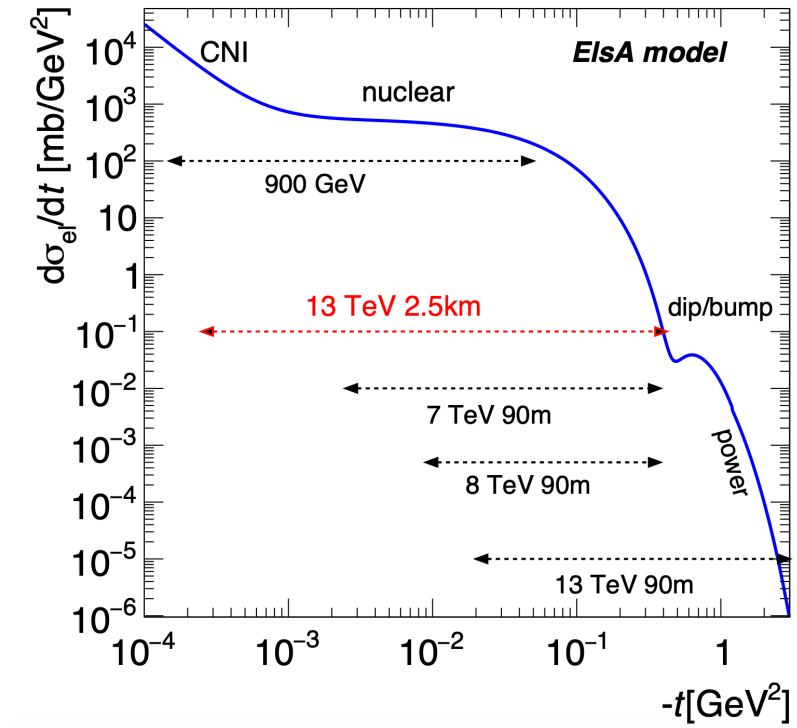
$$f_C(t) = -8\pi\alpha\hbar c \frac{G^2(t)}{|t|},$$

$$f_N(t) = (\rho + i) \frac{\sigma_{\text{tot}}}{\hbar c} e^{-B|t|/2},$$

f_C Coulomb amplitude
 f_N purely strongly interacting amplitude
 G electric form factor of the proton
 B nuclear slope

We can then write

$$\begin{aligned} \frac{d\sigma}{dt} &= \frac{4\pi\alpha^2(\hbar c)^2}{|t|^2} \times G^4(t) && \leftarrow \text{Coulomb interaction} \\ &- \sigma_{\text{tot}} \times \frac{\alpha G^2(t)}{|t|} [\sin(\alpha\phi(t)) + \rho \cos(\alpha\phi(t))] \times \exp\left(\frac{-B|t|}{2}\right) && \leftarrow \text{Coulomb-nuclear interference} \\ &+ \sigma_{\text{tot}}^2 \frac{1 + \rho^2}{16\pi(\hbar c)^2} \times \exp(-B|t|) && \leftarrow \text{Hadronic interaction} \end{aligned}$$



LUMINOSITY in ATLAS

$$\mathcal{L} = \frac{R}{\sigma} = \frac{\mu n_b f_r}{\sigma} = \frac{\mu_{vis} n_b f_r}{\sigma_{vis}}$$

$$\mu_{vis} = \epsilon \mu$$

$$\sigma_{vis} = \epsilon \sigma$$

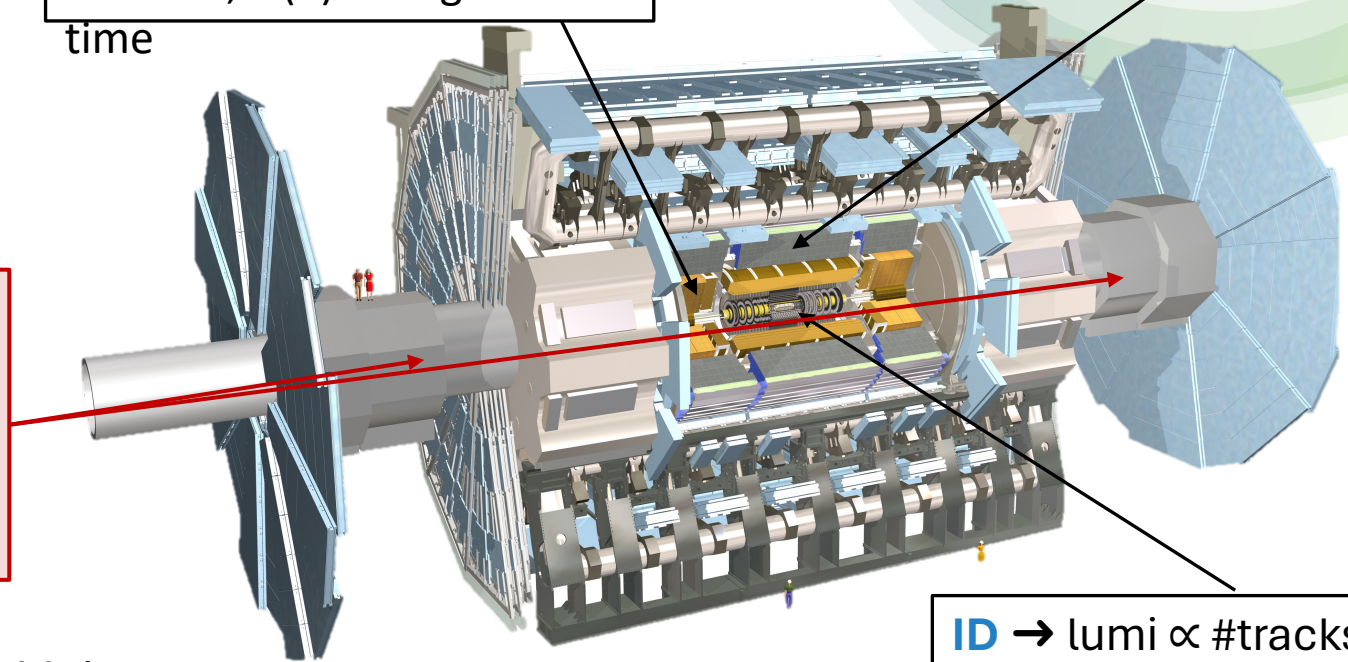
LUCID II → ATLAS reference luminometer

- Only one which provides absolute luminosity measurement → vdM calibration
- Can provide online and offline lumi, both per-bunch and integrated, for any μ range

Except LUCID, in ALFA runs only tracks are available!

LAr (ECAL and FCAL) → read out LAr gap HV currents, O(1)s integration time

Tile → lumi \propto PMT current, integrates over O(10) ms



ID → lumi \propto #tracks, can provide per-bunch lumi

BCM → only for low (μ) and HI runs **TPX** → for radiation monitoring
Z-counting → Cross-check of baseline luminosity vs time and μ

μ = average number of inelastic interactions per bunch crossing
 n_b = bunch pairs colliding per revolution
 f_r = revolution frequency